

# Scaled Pearson's Correlation Coefficient for Evaluating Text Similarity Measures

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## Abstract

Despite the ever-increasing interest in the field of text similarity methods, the development of adequate text similarity methods is lagging. Some methods are decent in entailment while others are reasonable to the degree to which two texts are similar. Very often, these methods are compared using Pearson's correlation; however, Pearson's correlation is bound to outliers that could affect the final correlation coefficient figure. As a result, the Pearson correlation is inadequate to find which text similarity method is better in situations where data items are very similar or are unrelated. This paper borrows the scaled Pearson correlation from the finance domain and builds a metric that can evaluate the performance of similarity methods over cross-sectional datasets. Results showed that the new metric is fine-grained with the benchmark dataset scores range as a promising alternative to Pearson's correlation. Moreover, extrinsic results from the application of the System Usability Scale (SUS) questionnaire on the scaled Pearson correlation revealed that the proposed metric is attaining attention from scholars which implicate its usage in the academia.

**Keywords:** Pearson, semantic similarity, performance metric, correlation metrics

## 1. Introduction

Semantic Textual Similarity (STS) determines the degree of which two texts are similar. It is active research, part of which in the SemEval workshop series (Agirre et al., 2012; D. M. Cer, Diab, Agirre, Lopez-Gazpio, & Specia, 2017). The STS has many applications in the field of automatic essay grading (Ratna, Luhurkinanti, Ibrahim, Husna, & Purnamasari, 2018), anti-plagiarism detection (Abdi, Idris, Alguliyev, & Aliguliyev, 2015; Meuschke, Siebeck, Schubotz, & Gipp, 2017), automated text summarization (Fang, Mu, Deng, & Wu, 2017), web page duplication detection (Manku, Jain, & Das Sarma, 2007), and other domain-specific tasks (Atoum, 2018, 2019; Ayyagari & Atoum, 2019).

Typically, an STS system computes the similarity between two texts as a score between 0 to 5, where 0 indicates dissimilarity and 5 indicates equivalence. Consequently, the relationship between human rating scores and STS system scores is used as the foundation for STS system assortment, often using Pearson Correlation (e.g., Šarić, Glavaš, Karan, Šnajder, & Bašić, 2012). The Pearson correlation finds the degree of association between the STS system and human scores, which is a value in the range of -1 to a +1. When the magnitude of the value is close to 1, it implies a high correlation with the human rating; consequently, the similarity method becomes promising.

Text similarity measures performance depends on many factors, including the underlying semantic features that might be affected by the domain of the text, the length of text, and the text-similarity algorithm itself. Such factors and many others could inject noise to the regression line of the Pearson Correlation. Therefore, under such noise conditions, extracting the correlation coefficient between two sets of stochastic variables is not trivial (Moriya, 2008). One major problem of the Pearson correlation is the outliers that influence the slope of the regression line, and accordingly, the value of the correlation coefficient. The Pearson correlation uses the mean and standard deviation of scores regardless of the STS task under consideration. Therefore, it is possible to get a high Pearson correlation for scores even though there is no actual relationship between the outputs and human judgments. This problem reconciles with Anscombe's quartet (Anscombe, 1973). According to Anscombe's quartet, the same Pearson correlation score might be obtained even the dataset is showing a visually nonlinear relationship due to outliers, as shown in Figure 1.

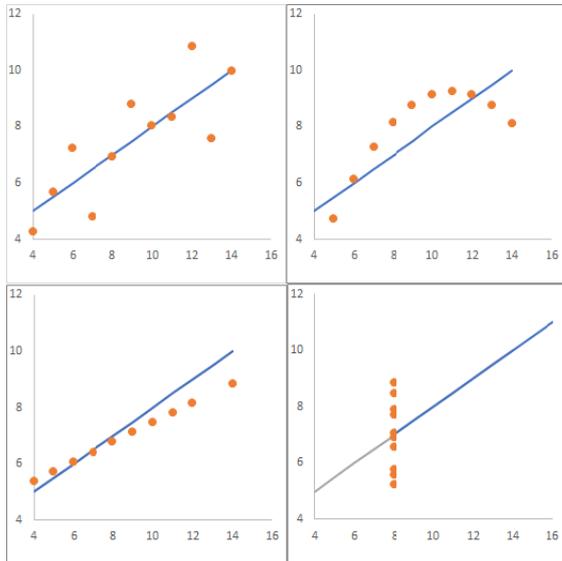


Figure 1. Effect of outliers on Pearson's correlation

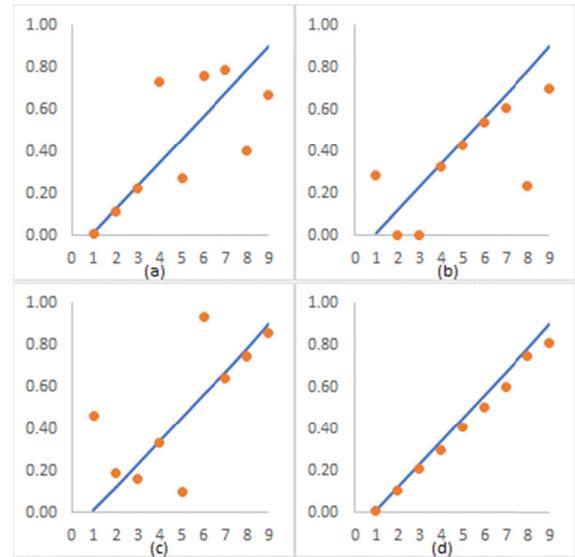


Figure 2. Effect of Similarity method on Pearson's

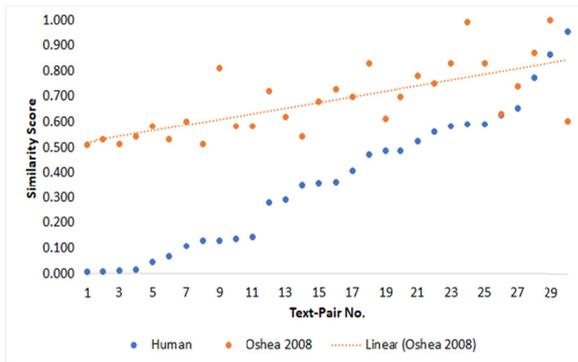


Figure 3. LSA method on STS-65 Dataset( $r=0.84$ )

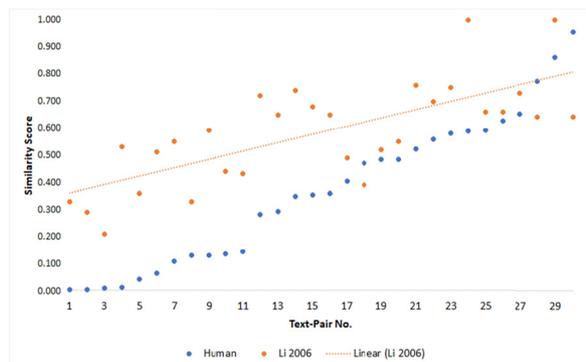


Figure 4. Li method on STS-65 Dataset( $r=0.81$ )

This research aims to discover an STS system that works for every *group* of the dataset pairs. A useful benchmark dataset has adequate examples of numerous text pairs that include pairs that are dissimilar, moderately similar, and almost similar pairs. These groups could resemble STS tasks of web page duplication detection, automatic essay grading, and text summarization. Therefore, it is essential to map the STS task to the suitable performance metric (such as Pearson correlation). Figure 2 shows three different systems named a) *perfect\_for\_low*, b) *perfect\_for\_medium*, c) *perfect\_for\_high*, and d) *perfect\_for\_all* that resembles a similarity measure that works perfectly for low similar pairs, moderately similar pairs, high similar pairs, and the perfect method that work with all cases. The set of human pairs were constructed for illustration purposes. Figure 2a is when the low similar pairs match the target similarity method, where the first three pairs are close to human ratings. The same can be applied to the figures 2b-2c. The optimal goal is to find a method that works well on all data pairs similar to Figure 2d. Therefore, based on the Pearson correlation alone, it is not clear wither a similarity measure (STS system) appropates similar, dissimilar, or moderate similar text pairs. Therefore, relying on the Pearson correlation is misleading (Reimers, Beyer, & Gurevych, 2016) and is inappropriate for every semantic similarity task (Wilson & Mihalcea, 2017).

The problem of the similarity groups is further illustrated with the STSS-65 dataset that consists of 30 text pairs (Li, McLean, Bandar, O'Shea, & Crockett, 2006). The human ratings shown in Figure 3 and Figure 4, demonstrate that the first arbitrary 12 pairs are dissimilar, 13<sup>th</sup> to 20<sup>th</sup> pairs are moderately similar, and 21<sup>st</sup> to 30<sup>th</sup> pairs are almost similar. Therefore, some similarity measures are reasonable to measure low similarity texts, while others are significantly performing better with high similarity traits. The LSA measure of O'Shea et al. (2008) shown in Figure 3 reveal similarity scores of more than 0.50 for all compared text pairs. Therefore, the reported LSA method is not suitable for low similarity texts as the figure shows that the LSA has higher scores than expected. The reported percentage absolute relative error of LSA to human rating is ranging from 53- 80%; accordingly, the

author calls the LSA method an overestimating method that gives a moderate Pearson correlation. Figure 4 shows the behavior of Li method (Li et al., 2006); relatively, the same symptom as the LSA method with percentage absolute relative error of human ratings to Li method is ranging from 61-98%. Therefore, these methods suffer from Anscombe's quartet problem, and an alternative metric should tackle their outliers.

Although there are many alternatives to the Pearson correlation, they are domain-specific (Bogolyubova, Panicheva, Tikhonov, Ivanov, & Ledovaya, 2018; Dikbaş, 2018; Smarandache, 2009; Wu, Pang, Lin, & Pei, 2013). The Spearman's rank correlation is more robust than Pearson; however, Pearson remains the most popular correlation measure (Serin, Nijveen, Hilhorst, & Ligterink, 2016). Compared to Pearson's correlation, Kendall's Tau is robust to outliers (M. Kendall & Gibbons, 1990); however, it suits data that is ranked by nature. Several evaluation methods were combined in (Reimers et al., 2016); however, they concentrate on the STS systems' ranking instead of particular properties of the benchmark dataset.

Therefore, to solve the problem, the author borrows the scaled Pearson correlation from the finance domain (Nikolić, Murešan, Feng, & Singer, 2012). The scaled Pearson correlation method is used to reveal correlations between test and human scores in various data segments. If the dataset is arbitrary grouped into three segments, three Pearson correlations scores are obtained. The author averages the scores over segments; therefore, getting a single scaled Pearson score. For the overall computation of many datasets with different distributions, the Fisher z-scores (Fisher, 1921) is used to convert scaled Pearson scores to a single Pearson correlation score; therefore, providing a quantitative one value that could be used to compare datasets of different sizes.

The scaled Pearson score reduce skewness, and therefore, this research could evaluate the STS system in different data range scores (different STS tasks). The proposed metric can be used to identify the effectiveness of a similarity method over a specific semantic task. Consequently, discovering significant pitfalls of semantic similarity methods and allowing better STS method selection.

The remainder of the paper is structured as follows. Section 2 summarizes the related works. In Section 3, this paper explains the proposed metric. In Section 4, this research evaluates the proposed metric, while Section 6 provides conclusions, followed by implications and conclusions.

## 2. Related Works

This section covers the Pearson's correlation as applied to the semantic similarity domain, ranking methods, information retrieval methods, and standard error methods.

### 2.1 Pearson Correlation

Pearson's correlation coefficient,  $r$ , has many formulas (Lee Rodgers & Nicewander, 1988). Equation (1) shows one by substituting estimates of the covariances and variances in the STS dataset. The benchmark datasets have a set of scores  $\{g_1, \dots, g_n\}$  that represent the human gold standard scores of a list of text pairs  $\{(P_1, Q_1), \dots, (P_n, Q_n)\}$  and another list  $\{t_1, \dots, t_n\}$  containing  $n$  values of scores obtained from a text similarity method.

$$r = \frac{\sum_{i=1}^n (g_i - \bar{g})(t_i - \bar{t})}{\sqrt{\sum_{i=1}^n (g_i - \bar{g})^2} \cdot \sqrt{\sum_{i=1}^n (t_i - \bar{t})^2}}, \quad (1)$$

where  $n$  is the number of text pairs,  $g_i$ ,  $t_i$  are the  $i^{\text{th}}$  score of the gold standard and test pairs scores, respectively. The  $\bar{g}_i$  and  $\bar{t}_i$  are the mean of the gold standard and test scores.

### 2.2 Ranking Methods

The Spearman correlation is a non-parametric measure (Spearman, 1904) that assesses the relationship between two text pairs as a monotonic function. Although the Spearman's coefficient is appropriate for a linear and non-linear relationship, it is less adopted in the semantic similarity domain. The Kendall tau rank correlation coefficient (M. G. Kendall, 1938) is a measure of the portion of ranks that match between two data sets; however, it is suitable for data that is ranked by nature (M. Kendall & Gibbons, 1990). The normalized Cumulative Gain (nCG) can be used to evaluate the ranking quality of STS scores (Järvelin & Kekäläinen, 2000). The normalized Discounted Cumulative Gain (nDCG) applies a discount factor to the normalized Cumulative Gain (Kekäläinen, 2005). It measures the advantage of a document based on its position in the result list, which is accrued from the top of the result list to the bottom. The difference is that the nCG does not include the position of a result in consideration of the usefulness of a result set. An enhanced version of nCG resolves the problems of rank ties and lower bound (Katerenchuk & Rosenberg, 2018). Since semantic similarity scores are scaled, ordinal ranking methods (e.g., Goodman & Kruskal, 1979) are not suitable for STS tasks. Therefore, rank methods have the problem of ties when more than one values get the same rank.

### 2.3 Error Methods

One of the most cited error methods is the absolute error which calculates the magnitude of an error in an experiment. An extension to the absolute error is the relative error that expresses how large the absolute error compared with the total size of data. Relative errors are usually calculated in percentage value comparing observed values to actual values such as the mean absolute percentage error (MAPE), a percentage measure of prediction accuracy. Relative error methods are easy-to-use, easy-to-understand, and domain-independent (Wang & Bovik, 2009); however, they have the problem of undefined mean and infinite variance.

### 2.4 Information Retrieval Methods

Traditional information retrieval methods such as accuracy, precision, and F-measure could be used for evaluating the effectiveness of STS systems; however, it is unclear how to compute them in the STS domain. The evaluation requires to know the maximum and minimum values of compared STS systems and the arbitrary boundary of grouped bins (Reimers et al., 2016).

## 3. Proposed Metric

The scaled Pearson correlation was initially used in the time series application (Nikolić et al., 2012). Equation (2) defines the number of segments ( $K$ ) that can fit into the total number of text pairs ( $N$ ) for a given set of cases ( $n$ ). Accordingly, the scaled Pearson correlation ( $\bar{r}_n$ ) for all text segments  $K$  is given by equation (3), where  $r_k$  is the Pearson's coefficient of correlation for segment  $k$ . The best number of segments  $K$  is dependent on the dataset distribution of scores and the required level of confidence. If the objective is to split the dataset into three cross-sections then ( $K$ ) will be assigned the value three; therefore, the number of cases ( $n$ ) will be the number of test pairs in each segment or bin. According to the third equation, mathematically the number of bins can grow from 2 to  $N - 1$ ; however, it is essential to split the dataset based on the STS task under consideration and provide a high confidence Pearson correlation  $r_k$  such that  $K$  is an integer value.

Equation (3) will provide one correlation for each dataset; therefore, a distribution-independent comparison with more than one dataset is needed. Therefore, the Fisher z-scores (Fisher, 1921) is used. The Fisher Z-score tells how far a score is from the mean in units of the standard deviation. This research converts the scaled Pearson scores to Fisher z-scores, then the z-scores are averaged and converted back to Pearson scores to provide a quantitative unbiased comparison between datasets of different sizes. Consequently, Fisher transformation is a way to transform the sampling distribution of Pearson's  $r$  (for each dataset) so that it becomes normally-distributed.

$$K = \frac{N}{n} \quad (2)$$

$$\bar{r}_n = \frac{1}{K} \sum_{k=1}^K r_k \quad (3)$$

$$z = \frac{1}{2} \ln \frac{1+\bar{r}_n}{1-\bar{r}_n} = \operatorname{arctanh}(\bar{r}_n) \quad (4)$$

$$\bar{r}_n = \tanh(z) \quad (5)$$

Equation (4) shows how the Pearson correlation is converted to z-scores, where  $\ln$  is the natural logarithm function, and  $\operatorname{arctanh}$  is the inverse hyperbolic tangent function. Equation (5) converts the same results back to Pearson correlation by using the  $\tanh$  of z-scores. As a result, we have one scaled Pearson value for comparison.

## 4. Evaluation and Discussion

### 4.1 Evaluation Methodology

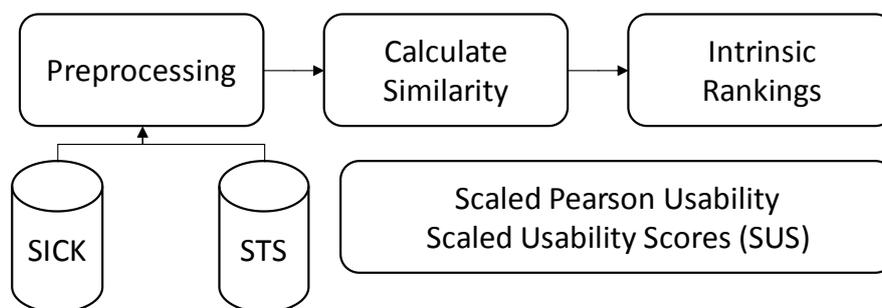


Figure 5. Evaluation Methodology

Figure 5 shows the evaluation methodology in the research experiments. The methodology consists of preprocessing, calculating similarity, ranking similarity methods, and extrinsic evaluation of the proposed scaled Pearson correlation. The author uses two primary datasets in this experiment, the STS (D. M. Cer et al., 2017) and the SICK (Sentences Involving Compositional Knowledge) datasets. The STS benchmark dataset comprises a selection of the English datasets used in the STS tasks organized in the context of SemEval series between 2012 and 2017. The selection of datasets includes text from image captions, news headlines, and user forums. The SICK dataset (Marelli et al., 2014) consists of about 10,000 English sentence pairs, generated starting from two existing sets: the 8K ImageFlickr data set and the SemEval 2012 STS MSR-Video Description dataset. This research selects the DEV and TEST datasets of SICK (5427 sentences).

The *calculate similarity* process in the evaluation methodology scores selected methods based on its underlying techniques. Then, the methods are ranked using intrinsic rankings of Pearson, Mean Absolute error, Spearman, nDCG, and Rank DCG methods. The extrinsic ranking is accomplished based on the usability of the proposed scaled Pearson method.

#### 4.2 Selected Text Similarity Methods

We applied the proposed metric on a set of text similarity methods that use different approaches (Arora, Liang, & Ma, 2017; Atoum & Ootom, 2016; Conneau, Kiela, Schwenk, Barrault, & Bordes, 2017; Kusner, Sun, Kolkin, & Weinberger, 2015; Li et al., 2006; Zarif et al., 1994). The Word Mover's Distance (WMD) uses the word embeddings of the words in two texts to measure the minimum amount that the words in one text need to *travel* in semantic space to reach the words of the other text (Kusner et al., 2015). The Smooth Inverse Frequency (SIF) gives less weight to wholly inappropriate words, and so word embeddings are weighted based on the estimated relative frequency of a word in a reference corpus and common component analysis technique (Arora et al., 2017). InferSent (INF for shorthand) is a sentence embedding trained on fastText vectors of Facebook research (Conneau et al., 2017). It is a BiLSTM with max-pooling that was trained on the SNLI dataset, 570k English sentence pairs labeled with one of three categories: entailment, contradiction, or neutral. Similar to InferSent, Google Sentence Encoder (GSE) provides sentence embeddings based on trained deep learning network semantic vectors (D. Cer et al., 2018). Traditional semantic similarity methods calculate the semantic similarity of two sentences using information from a structured lexical database and corpus statistics (e.g., Atoum & Ootom, 2016; Atoum, Ootom, & Kulathuramaiyer, 2016; Li et al., 2006).

The experiments exclude stopwords from the datasets using the *nlTK* list of stop words. For GSE, the paper uses the Encoder 2 from Google TensorFlow Hub. The author uses the pre-trained word vectors of Glove (840B tokens x 300 dimensions) from Stanford's, fastText word vectors W2V (2 million-word vectors x 300 dimensions).

Table 1 shows the Pearson correlation of the list of compared methods, where GSE and InferSent are the leaders while Li method (Li et al., 2006) is lagging. According to the results the usage of GLOVE or W2V pre-trained word vectors affects the performance of SIF and WMD methods by 2-4%. The author argues that the Pearson correlation is not enough for method selection. Therefore, this research ran and evaluated the same methods on other ranking metrics, as shown in Figure 6.

4.3 Intrinsic Evaluation

Table 1. Pearson Correlation of Compared Methods.

| <b>SICK Dataset</b> |                        |                         |  |
|---------------------|------------------------|-------------------------|--|
| Method              | Pearson <sup>Dev</sup> | Pearson <sup>Test</sup> |  |
| GSE                 | <b>0.84</b>            | <b>0.82</b>             |  |
| INF                 | 0.77                   | 0.76                    |  |
| SIF+W2V             | 0.73                   | 0.73                    |  |
| SIF+GLOVE           | 0.70                   | 0.72                    |  |
| WMD+GLOVE           | 0.64                   | 0.64                    |  |
| WMD+W2V             | 0.64                   | 0.64                    |  |
| Li                  | 0.62                   | 0.62                    |  |
| <b>STS Dataset</b>  |                        |                         |  |
| GSE                 | <b>0.79</b>            | <b>0.76</b>             |  |
| INF                 | 0.78                   | 0.71                    |  |
| SIF+W2V             | 0.77                   | 0.69                    |  |
| SIF+GLOVE           | 0.76                   | 0.68                    |  |
| WMD+W2V             | 0.72                   | 0.66                    |  |
| WMD+GLOVE           | 0.71                   | 0.62                    |  |
| Li                  | 0.70                   | 0.59                    |  |

Note. Dev= Development Dataset; Test= Test Dataset;

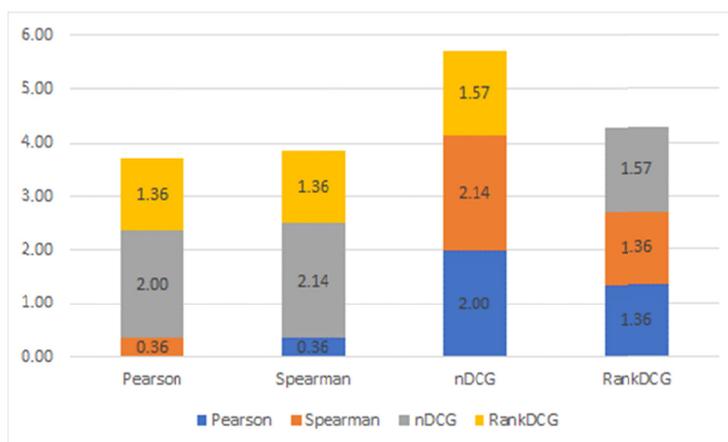


Figure 6. Mean Absolute Error between Pearson and other ranking methods

Table 2. Scaled Pearson Correlations for STS and SICK datasets

| <b>SICK Dataset</b> |               |                              |                               |
|---------------------|---------------|------------------------------|-------------------------------|
|                     | <b>Method</b> | <b>Pearson<sup>Dev</sup></b> | <b>Pearson<sup>Test</sup></b> |
|                     | GSE           | <b>0.50</b>                  | 0.42                          |
|                     | INF           | 0.44                         | 0.41                          |
|                     | SIF+W2V       | 0.42                         | 0.41                          |
|                     | SIF+GLOVE     | 0.51                         | 0.35                          |
|                     | WMD+GLOVE     | 0.46                         | <b>0.50</b>                   |
|                     | WMD+W2V       | 0.46                         | <b>0.50</b>                   |
|                     | Li            | 0.46                         | 0.40                          |
| <b>STS Dataset</b>  |               |                              |                               |
|                     | GSE           | <b>0.46</b>                  | <b>0.46</b>                   |
|                     | INF           | 0.45                         | 0.38                          |
|                     | SIF+W2V       | 0.41                         | 0.36                          |
|                     | SIF+GLOVE     | 0.41                         | 0.37                          |
|                     | WMD+W2V       | 0.39                         | 0.35                          |
|                     | WMD+GLOVE     | 0.38                         | 0.32                          |
|                     | Li            | 0.29                         | 0.25                          |

Note. Dev= Development Dataset; Test= Test Dataset;

Figure 6 shows the Mean Absolute Error (MAE) between the rank of the methods presented in Table 1 (using Pearson) and ranks of the same methods using other ranking methods discussed in Section 2.2. The STS methods used in Table 1 could get different rank if another evaluation metric was used. The nearest rank was with Spearman evaluation metric, and highest error was with RankDCG method. Moreover, the ranks were different with different datasets. Therefore, Spearman could be used as an auxiliary evaluation metric to Pearson correlation; however, it does not give enough information about STS tasks (dataset distributions).

Based on different types of STS tasks and current datasets, each benchmark dataset was split into three bins were the first bin represent the set of dissimilar text pairs, the middle bin represents moderately similar text, and the last bin is highly similar or equivalent text pairs. For the STS-TEST and STS-DEV datasets, bin number one with text pairs of human scores less than 1.66, bin number two with scores between 1.66 and 3.33 and bin number three with scores higher than 3.33. The bin coverage for STS-TEST and STS-DEV datasets were (0.295,0.318,0.387) and (0.355,0.344,0.301) respectively. For the SICK-TEST and SICK-DEV datasets, three bins were used according to the dataset labels (contradiction, neutral, entailment) respectively. The bin coverage for SICK-TEST and SICK-DEV datasets were (0.148,0.288,0.564) and (0.146,0.287,0.567) respectively.

Table 2 shows the scaled Pearson correlations. All reported scores were significant ( $p < 0.05$ ). The scores are almost 30% lower than the reported Pearson scores, which indicate the effectiveness of the proposed metric by removing outliers. Based on scaled correlations, the rank of similarity methods could be used for a general-purpose STS task; however, it is essential to use methods that complete others on a specific STS task.

Selecting the best metric is context-dependent on the similarity task. Figure 7 and Figure 8 show the scaled Pearson of each method over three bins for the combined test and training datasets. The author converted scaled Pearson scores of test and training to z-scores, then the z-scores were averaged and converted back to Pearson scores. Most of the compared similarity methods in STS dataset are getting low scaled Pearson scores in the moderately similar text due to either overestimating or underestimating scores. The similar symptom was also shown for the SICK dataset in the first low similarity bin. The figures show that although GSE got the highest Pearson score, it gets a lower scaled score due to overestimating text pairs. To justify GSE performance, the author runs the experiment on the SemEval benchmark dataset 2012-2017, a list of 1500 sentence pairs development dataset (D. M. Cer et al., 2017). This research found that 139 sentence pairs (around 9%) that were scored zero by humans are overestimated by Google's Encoder (0.644 on average). A sentence pair from the benchmark dataset is shown:

*3 killed, 4 injured in Los Angeles shootings*

*Five killed in Saudi Arabia shooting.*

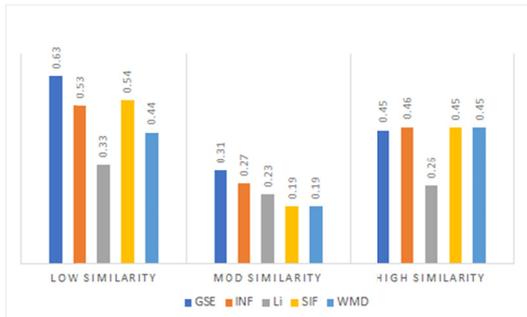


Figure 7. Scaled Pearson Correlations-STS

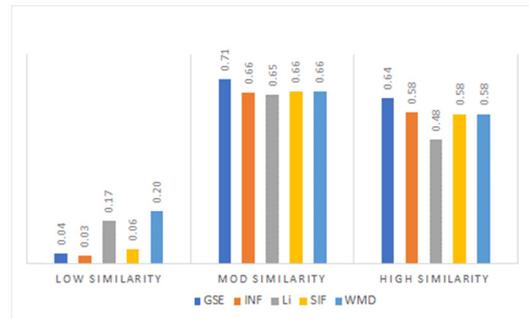


Figure 8. Scaled Pearson Correlations-SICK

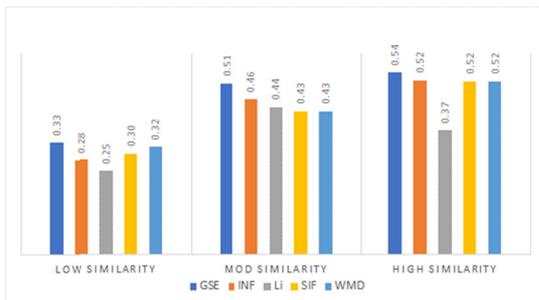


Figure 9. Scaled Pearson Correlations (STS, SICK)

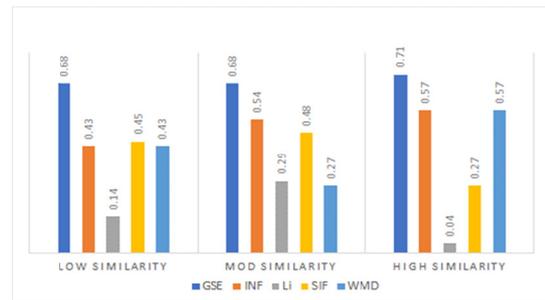


Figure 10. Ranked Scaled Pearson Correlation

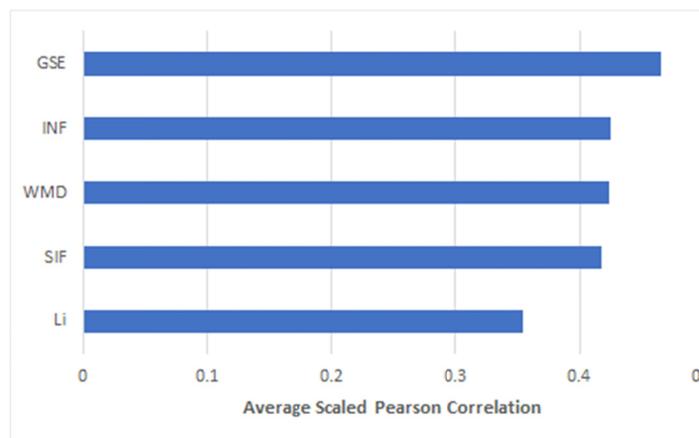


Figure 11. Overall Scaled Pearson's Ranked Systems

The sentence-pair score is 0.89, 89% higher than human due to the existence of one-word match (*killed*) and related word (*injured*). However, for the SIF method, it gets better scaled Pearson since it depends on existing words rather than embeddings. Therefore, if the STS tasks are related to detecting dissimilar text, then GSE or even WMD method will do the job.

The scaled Pearson performance of the SICK dataset is relatively different. The SICK dataset involves difficulties of active or passive sentences, the impact of negation, determiners, and other grammatical elements. Therefore, it is considered more difficult than STS. Moreover, this research's experiments aim similarity, not relatedness and entailment as described in the SICK dataset. Furthermore, during the experiment, this research excluded stop words with no lexical analysis. Therefore, the SICK scores are affected in the "contradiction" bin, as shown in Figure 8.

Figure 9 combines the results of STS, and SICK dataset were the scores in Figure 7, and Figure 8 are converted to z-scored, averaged, then converted back to Pearson scored. The figure shows that it is hard for systems to find dissimilar pairs as shown in the first bin, while most of the time it was getting relatively good results when text

pairs are similar (bin number 3). This paper runs the previous experiment over the scaled Pearson ranks instead of scaled Pearson scores to assure that scores are not squandered during the conversation from Pearson to Fisher Z scores and vice versa. The paper report the rank of the scaled Pearson averaged over the four datasets, as shown in Figure 10. Scores were normalized between 0 and 1 to elevate proper comparison. The figure shows relatively similar behavior, as shown in Figure 9.

Figure 11 combines the scaled Pearson correlation in Figure 9 to one Pearson correlation figure per method. The scores in Figure 9 were first converted to z-scores, then they were averaged and converted back to Pearson correlation. Notably that all methods were getting relatively low scaled Pearson correlation, which indicates that the methods were not doing well in all cases as illustrated by Figure 7-9. Therefore, contrary to the previous scholars’ findings that such methods achieved high correlation as shown in Table 1 and Table 2, they still need improvement to provide more accurate results in medium similarity location for STS dataset and low similarity location for the SICK dataset. Moreover, although the WMD method was not getting high Pearson correlation, it gets relatively high scaled Pearson correlation, which implies that the method was doing well based on its underlining word embeddings. Consequently, the proposed metric is capable of detection of overestimating or underestimating of similarity in compared text pairs; therefore, scholars could replace performance metrics with the proposed scaled Pearson metric if they want a rank similarity method over cross-sectional datasets.

4.4 Extrinsic Evaluation

Although the scaled Pearson metric is giving interpretable results, it is essential to evaluate the Scaled Pearson metric when applied in the STS Sem-Eval context. Since the scaled Pearson has not been adopted, it is essential to borrow views of the metric from scholars. This section runs the System Usability Scale (SUS) questionnaire (Brooke, 1996) to quantify the usability of the proposed metric by input from 10 scholars from those who have experience in the STS domain. The SUS model provides a reliable tool for measuring the usability of products or services. It has a 10-item questionnaire with Likert responses scale. The SUS scores are calculated based on a simple formula: subtract one from the odd question answers, and subtract the value of the even question answers from 5. Then add up the total score and multiply it by 2.5. A result is a number on a scale of 1 – 100 (Lewis & Sauro, 2017), where 100 is excellent user experience, equivalent to an “A”; 68 is considered average (“C” grade). The author is aware that the extrinsic approach is not comprehensive and is limited due to many external factors; however, the goal of this experiment is to see if scholars are interested in adopting the proposed metric in their research. The proposed scaled Pearson and the SUS questionnaire was shared with the scholars over email with details on how to run the experiment. Table 3 shows the results of the SUS questionnaire.

Table 3. SUS Questionnaire for (Scaled Pearson correlation =system).

| Qtn# | Question   | Total |
|------|--|-------|
| 1    | I think that I would like to use this system frequently.                                   | 40    |
| 2    | I found the system unnecessarily complex.  | 24    |
| 3    | I thought the system was easy to use.  | 38    |
| 4    | I think that I would need the support of a technical person to be able to use this system. | 18    |
| 5    | I found the various functions in this system were well integrated.                         | 33    |
| 6    | I thought there was too much inconsistency in this system.                                 | 23    |
| 7    | I would imagine that most people would learn to use this system very quickly.              | 40    |
| 8    | I found the system very cumbersome to use.   | 19    |
| 9    | I felt very confident using the system.  | 40    |
| 1    | I needed to learn a lot of things before I could get going with this system.               |       |
| 0    |  | 40    |
|      | Total (Even)   | 101   |
|      | Total (Odd)  | 191   |
|      | Average SUS  | 72.5  |

Table 4. Participants SUS scores.

| Participant | SUS Score |
|-------------|-----------|
| p1          | 72.5      |
| p2          | 72.5      |
| p3          | 65.0      |
| p4          | 75.0      |
| p5          | 70.0      |
| p6          | 82.5      |
| p7          | 72.5      |
| p8          | 77.5      |
| p9          | 72.5      |
| p10         | 65.0      |

The Calculation of SUS figures was carried out using SUS guidelines (Lewis & Sauro, 2017). Therefore, Table 3 reports a score of 72.5 usability score, which is considered the “C+ Okay” acceptable model. The participants of SUS ratings, as shown in Table 4, shows that the scores of each participant are within the distribution with a standard deviation of 5.3. Therefore, the scaled Pearson was acceptable by scholars when compared to the traditional Pearson correlation. Although the SUS can work with a limited number of participants according to a study by Tullis and Thomas over usability models (Tullis & Stetson, 2004), this evaluation remains limited for a limited number of participants who did not see the proposed scaled Pearson metric in practice. Moreover, the proposed metric depends intensely on the similarity task under consideration.

## 5. Implications

On the overall, the semantic similarity method is dependent on the semantic task (Atoum, 2016, 2018; Ayyagari & Atoum, 2019) or the bins (categories) in our case. The interpretation of these findings is that a high Pearson correlation does not always indicate a *top* semantic similarity measure. Similarity methods that have low scaled Pearson correlation errors have high absolute errors and are either overestimating or underestimating the similarity between compared text pairs.

The implications from the previous findings draw attention to scholars to take into consideration the STS task under consideration and provide an enhanced system that matches the similarity task. Moreover, academic competitions may adopt a smarter way of comparing similarity methods aside from the traditional Pearson correlation. Although the number of bins was chosen arbitrarily to be three bins, there are other possibilities of the best number of bins that could be used to fine-tune the proposed metric which implies that the dataset designers should also take care of dataset distributions during data gathering. Although the proposed metric was used in the text-similarity domain, it could be used in any domain where variable correlation could be measured, such as image similarity.

While many datasets are similar, the proposed method was tested on single STS datasets. One implication of the new method is that it could affect various applications that depend on Pearson’s correlation alone. Moreover, the reliable of the proposed metric will finally depend on researchers who would like to adopt the new measure.

## 6. Conclusion

This paper proposes a new similarity performance evaluation metric, scaled Pearson correlation, which was borrowed from the finance domain. The proposed metric provides decision-making information about the compiled dataset that was not being implied by the Pearson correlation alone. The measure could be used to replace Pearson’s correlation when comparing text similarity measures over a cross-sectional benchmark dataset. The System Usability Score showed that the proposed metric is deemed applicable under dataset restrictions. In the future, the author will formalize the measure and apply it to other datasets and run other simulations to find the best number of bins.

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