

Folding of the Chaotic General Tree and it's Chains

Mabrouk El-Ghoul (Corresponding author)

Mathematics department, Faculty of Science, Tanta University, Tanta, Egypt

Tel: 20-10-468-4812 E-mail: m_elghoul_2009@hotmail.com

Shereen Adel Mousa

Mathematics department, Faculty of Girl, Ain shams University, Egypt

Tel: 20-16-6014-9898 E-mail: shereen.3010@hotmail.com

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Abstract

In this paper, we will introduce the folding of the chaotic general tree and it's chains. The variation of the adjacent, incidence, area, volume, edge area, edge volume, area volume matrices of the chaotic general tree under the folding are discussed. The relation between the folding of the chaotic general tree and it's chains will be deduced.

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1. Definitions and Background

1.1 Folding

Let $f : G \rightarrow G'$ be a map between any two graphs G and G' (not necessary to be simple) such that if $(u, v) \in G$, $(f(u), f(v)) \in G'$. Then f is called a "topological folding" of G into G' provided that $d(f(u), f(v)) \leq d(u, v)$. [M. El-Ghoul and T. Homoda, 2006].

1.2 Chaotic chains

Let G be a graph with vertices $V = \{v^1, v^2, \dots, v^i\}$, edges $E = \{e^1, e^2, \dots, e^j\}$, areas $A = \{a^1, a^2, \dots, a^m\}$, and volumes $L = \{l^1, l^2, \dots, l^n\}$ carries infinite number of

chaotics [M. El-Ghoul and Sh.A.Mousa, under press].

*The 0-chaotic chains on G is a system of a formal sum

$$\left\{ \begin{array}{c} \lambda_1^{1h} v_{1h}^1 + \lambda_2^{1h} v_{1h}^2 + \dots + \lambda_j^{1h} v_{1h}^j \\ \lambda_1^{2h} v_{2h}^1 + \lambda_2^{2h} v_{2h}^2 + \dots + \lambda_j^{2h} v_{2h}^j \\ \vdots \\ \lambda_1^{\infty h} v_{\infty h}^1 + \lambda_2^{\infty h} v_{\infty h}^2 + \dots + \lambda_j^{\infty h} v_{\infty h}^j \end{array} \right\}$$

where each λ_i^{rh} is an integer.

*A 1-chaotic chain on G is a system of a formal sum

$$\left\{ \begin{array}{c} \lambda_1^{1h} e_{1h}^1 + \lambda_2^{1h} e_{1h}^2 + \dots + \lambda_j^{1h} e_{1h}^j \\ \lambda_1^{2h} e_{2h}^1 + \lambda_2^{2h} e_{2h}^2 + \dots + \lambda_j^{2h} e_{2h}^j \\ \vdots \\ \lambda_1^{\infty h} e_{\infty h}^1 + \lambda_2^{\infty h} e_{\infty h}^2 + \dots + \lambda_j^{\infty h} e_{\infty h}^j \end{array} \right\}$$

where each λ_j^{rh} is an integer.

*A 2-chaotic chain on G is a system of a formal sum

$$\left\{ \begin{array}{c} \lambda_1^{\overline{1h}} a_{1h}^1 + \lambda_2^{\overline{1h}} a_{1h}^2 + \dots + \lambda_m^{\overline{1h}} a_{1h}^m \\ \lambda_1^{\overline{2h}} a_{2h}^1 + \lambda_2^{\overline{2h}} a_{2h}^2 + \dots + \lambda_m^{\overline{2h}} a_{2h}^m \\ \vdots \\ \lambda_1^{\overline{\infty h}} a_{\infty h}^1 + \lambda_2^{\overline{\infty h}} a_{\infty h}^2 + \dots + \lambda_m^{\overline{\infty h}} a_{\infty h}^m \end{array} \right\}, \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^1 + \lambda_2^{1h} a_{1h}^2 + \dots + \lambda_m^{1h} a_{1h}^m \\ \lambda_1^{2h} a_{2h}^1 + \lambda_2^{2h} a_{2h}^2 + \dots + \lambda_m^{2h} a_{2h}^m \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^1 + \lambda_2^{\infty h} a_{\infty h}^2 + \dots + \lambda_m^{\infty h} a_{\infty h}^m \end{array} \right\}$$

such that each λ_m^{rh} is an integer and the upper bar denote that the chaotics are up and the lower bar denote that the chaotics are down the area.

*A 3-chaotic chain on G is a system of a formal sum

$$\left\{ \begin{array}{c} \lambda_1^{\overline{1h}} l_{1h}^1 + \lambda_2^{\overline{1h}} l_{1h}^2 + \dots + \lambda_n^{\overline{1h}} l_{1h}^n \\ \lambda_1^{\overline{2h}} l_{2h}^1 + \lambda_2^{\overline{2h}} l_{2h}^2 + \dots + \lambda_n^{\overline{2h}} l_{2h}^n \\ \vdots \\ \lambda_1^{\overline{\infty h}} l_{\infty h}^1 + \lambda_2^{\overline{\infty h}} l_{\infty h}^2 + \dots + \lambda_n^{\overline{\infty h}} l_{\infty h}^n \end{array} \right\}, \left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^1 + \lambda_2^{1h} l_{1h}^2 + \dots + \lambda_n^{1h} l_{1h}^n \\ \lambda_1^{2h} l_{2h}^1 + \lambda_2^{2h} l_{2h}^2 + \dots + \lambda_n^{2h} l_{2h}^n \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^1 + \lambda_2^{\infty h} l_{\infty h}^2 + \dots + \lambda_n^{\infty h} l_{\infty h}^n \end{array} \right\}$$

such that each λ_n^{rh} is an integer and the upper bar denote that the chaotics are outside the volume and the lower bar denote that the chaotics are inside the volume.

1.3 Chaotic General Tree

A "Chaotic general tree" is a general tree that carries many physical characters.[M. El-Ghoul and Sh.A.Mousa, under press].

See Fig.(1).

Where the chaotic adjacent matrix is

$$A_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix},$$

the chaotic edge matrix

$$E_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} \\ 1_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix},$$

the chaotic area matrix

$$R_h(G_h) = [0_{012\dots\infty h}],$$

the chaotic volume matrix

$$V_h(G_h) = [0_{012\dots\infty h}],$$

the chaotic incidence matrix

$$I_h(G_h) = \begin{bmatrix} 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} \end{bmatrix},$$

the chaotic vertex area matrix

$$M_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix},$$

the chaotic vertex volume matrix

$$N_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \\ 0_{012\dots\infty h} \end{bmatrix},$$

the chaotic edges area matrix

$$H_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix},$$

the chaotic edge volume matrix

$$J_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \\ 0_{012\dots\infty h} \end{bmatrix},$$

and the chaotic area volume matrix

$$U_h(G_h) = [0_{012\dots\infty h}]$$

where the lower suffix (012... ∞h) refers to the existence of the chaotics, also its

$$0\text{-chaotic chains are } \left\{ \begin{array}{c} \lambda_1^{1h} v_{1h}^0 + \lambda_2^{1h} v_{1h}^1 + \lambda_3^{1h} v_{1h}^2 + \lambda_4^{1h} v_{1h}^3 \\ \lambda_1^{2h} v_{2h}^0 + \lambda_2^{2h} v_{2h}^1 + \lambda_3^{2h} v_{2h}^2 + \lambda_4^{2h} v_{2h}^3 \\ \vdots \\ \lambda_1^{\infty h} v_{\infty h}^0 + \lambda_2^{\infty h} v_{\infty h}^1 + \lambda_3^{\infty h} v_{\infty h}^2 + \lambda_4^{\infty h} v_{\infty h}^3 \end{array} \right\},$$

$$\text{the 1- chaotic chains are } \left\{ \begin{array}{c} \lambda_1^{1h} e_{1h}^0 + \lambda_2^{1h} e_{1h}^1 + \lambda_3^{1h} e_{1h}^2 \\ \lambda_1^{2h} e_{2h}^0 + \lambda_2^{2h} e_{2h}^1 + \lambda_3^{2h} e_{2h}^2 \\ \vdots \\ \lambda_1^{\infty h} e_{\infty h}^0 + \lambda_2^{\infty h} e_{\infty h}^1 + \lambda_3^{\infty h} e_{\infty h}^2 \end{array} \right\},$$

$$\text{the 2- chaotic chains are } \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^0 \end{array} \right\}, \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^0 \end{array} \right\},$$

and the 3- chaotic chains are $\left\{ \begin{pmatrix} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^0 \end{pmatrix}, \begin{pmatrix} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^0 \end{pmatrix} \right\}.$

2. The main results

Aiming to our study, we will introduce the Folding of the chaotics of the chaotic general tree :

2.1 Folding of the chaotics of the chaotic general tree

Case(1) :

In this case, the folding gives the original chaotic general tree without any change. All it's matrices and chaotic chains will remain as it is. It is the identity folding.

See Fig.(2).

Case(2) :

In this case, the folding acts on the chaotics of the vertices v^0, v^1, v^2, v^3 , edges e^0, e^1, e^2 , area a^0 , and volume l^0 . The limit of the foldings is the 1-chaotic general tree (fuzzy general tree).

See Fig.(3).

Where

$$\begin{aligned} * A_h(G_h) &= \begin{bmatrix} 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 0_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \end{bmatrix} \xrightarrow{F_{21}} \\ A_h(F_{21}(G_h)) &= \begin{bmatrix} 0_{012...(\infty-1)h} & 1_{012...(\infty-1)h} & 0_{012...(\infty-1)h} & 0_{012...(\infty-1)h} \\ 1_{012...(\infty-1)h} & 0_{012...(\infty-1)h} & 1_{012...(\infty-1)h} & 1_{012...(\infty-1)h} \\ 0_{012...(\infty-1)h} & 1_{012...(\infty-1)h} & 0_{012...(\infty-1)h} & 0_{012...(\infty-1)h} \\ 0_{012...(\infty-1)h} & 1_{012...(\infty-1)h} & 0_{012...(\infty-1)h} & 0_{012...(\infty-1)h} \end{bmatrix} \\ \dots \lim_{\longrightarrow} F_{2n} A_h(\lim F_{2n}(G_h)) &= \begin{bmatrix} 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \\ 1_{01h} & 0_{01h} & 1_{01h} & 1_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \end{bmatrix}, \\ * E_h(G_h) &= \begin{bmatrix} 0_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 1_{012... \infty h} & 0_{012... \infty h} & 1_{012... \infty h} \\ 1_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} \end{bmatrix} \xrightarrow{F_{21}} \\ E_h(F_{21}(G_h)) &= \begin{bmatrix} 0_{012...(\infty-1)h} & 1_{012...(\infty-1)h} & 1_{012...(\infty-1)h} \\ 1_{012...(\infty-1)h} & 0_{012...(\infty-1)h} & 1_{012...(\infty-1)h} \\ 1_{012...(\infty-1)h} & 1_{012...(\infty-1)h} & 0_{012...(\infty-1)h} \end{bmatrix} \\ \dots \lim_{\longrightarrow} F_{2n} E_h(\lim F_{2n}(G_h)) &= \begin{bmatrix} 0_{01h} & 1_{01h} & 1_{01h} \\ 1_{01h} & 0_{01h} & 1_{01h} \\ 1_{01h} & 1_{01h} & 0_{01h} \end{bmatrix}, \\ * R_h(G_h) &= [0_{012... \infty h}] \xrightarrow{F_{21}} R_h(F_{21}(G_h)) = [0_{012...(\infty-1)h}] \\ \dots \lim_{\longrightarrow} F_{2n} R_h(\lim F_{2n}(G_h)) &= [0_{01h}], \\ * V_h(G_h) &= [0_{012... \infty h}] \xrightarrow{F_{21}} V_h(F_{21}(G_h)) = [0_{012...(\infty-1)h}] \end{aligned}$$

$$\dots \lim_{\longrightarrow} F_{2n} V_h(\lim F_{2n}(G_h)) = [0_{01h}],$$

$$*I_h(G_h) = \begin{bmatrix} 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{21}}$$

$$I_h(F_{21}(G_h)) = \begin{bmatrix} 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \end{bmatrix}$$

$$\dots \lim_{\longrightarrow} F_{2n} I_h(\lim F_{2n}(G_h)) = \begin{bmatrix} 1_{01h} & 0_{01h} & 0_{01h} \\ 1_{01h} & 1_{01h} & 1_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} \\ 0_{01h} & 0_{01h} & 1_{01h} \end{bmatrix},$$

$$*M_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{21}} M_h(F_{21}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \end{bmatrix}$$

$$\dots \lim_{\longrightarrow} F_{2n} M_h(\lim F_{2n}(G_h)) = \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 0_{01h} \\ 1_{01h} \end{bmatrix},$$

$$*N_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \\ 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{21}} N_h(F_{21}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \end{bmatrix}$$

$$\dots \lim_{\longrightarrow} F_{2n} N_h(\lim F_{2n}(G_h)) = \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 1_{01h} \\ 0_{01h} \end{bmatrix},$$

$$*H_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{21}} H_h(F_{21}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \end{bmatrix}$$

$$\dots \lim_{\longrightarrow} F_{2n} H_h(\lim F_{2n}(G_h)) = \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 1_{01h} \end{bmatrix},$$

$$*J_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \\ 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{21}} J_h(F_{21}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \end{bmatrix}$$

$$\dots \lim_{\longrightarrow} F_{2n} J_h(\lim F_{2n}(G_h)) = \begin{bmatrix} 0_{01h} \\ 1_{01h} \\ 0_{01h} \end{bmatrix},$$

$$*U_h(G_h) = [0_{012\dots\infty h}] \xrightarrow{F_{21}} U_h(F_{21}(G_h)) = [0_{012\dots(\infty-1)h}]$$

$$\dots \lim_{\longrightarrow} F_{2n} U_h(\lim F_{2n}(G_h)) = [0_{01h}],$$

and the 0-chaotic chain are

$$\left\{ \begin{array}{c} \lambda_1^{1h} v_{1h}^0 + \lambda_2^{1h} v_{1h}^1 + \lambda_3^{1h} v_{1h}^2 + \lambda_4^{1h} v_{1h}^3 \\ \lambda_1^{2h} v_{2h}^0 + \lambda_2^{2h} v_{2h}^1 + \lambda_3^{2h} v_{2h}^2 + \lambda_4^{2h} v_{2h}^3 \\ \vdots \\ \lambda_1^{\infty h} v_{\infty h}^0 + \lambda_2^{\infty h} v_{\infty h}^1 + \lambda_3^{\infty h} v_{\infty h}^2 + \lambda_4^{\infty h} v_{\infty h}^3 \end{array} \right\} \xrightarrow{F_{21}} \left\{ \begin{array}{c} \lambda_1^{1h} v_{1h}^0 + \lambda_2^{1h} v_{1h}^1 + \lambda_3^{1h} v_{1h}^2 + \lambda_4^{1h} v_{1h}^3 \\ \lambda_1^{2h} v_{2h}^0 + \lambda_2^{2h} v_{2h}^1 + \lambda_3^{2h} v_{2h}^2 + \lambda_4^{2h} v_{2h}^3 \\ \vdots \\ \lambda_1^{(\infty-1)h} v_{(\infty-1)h}^0 + \lambda_2^{(\infty-1)h} v_{(\infty-1)h}^1 \\ \quad + \lambda_3^{(\infty-1)h} v_{(\infty-1)h}^2 + \lambda_4^{(\infty-1)h} v_{(\infty-1)h}^3 \end{array} \right\}$$

$$\dots \lim_{\longrightarrow} F_{2n} \lambda_1^{1h} v_{1h}^0 + \lambda_2^{1h} v_{1h}^1 + \lambda_3^{1h} v_{1h}^2 + \lambda_4^{1h} v_{1h}^3,$$

the 1- chaotic chains are

$$\left\{ \begin{array}{c} \lambda_1^{1h} e_{1h}^0 + \lambda_2^{1h} e_{1h}^1 + \lambda_3^{1h} e_{1h}^2 \\ \lambda_1^{2h} e_{2h}^0 + \lambda_2^{2h} e_{2h}^1 + \lambda_3^{2h} e_{2h}^2 \\ \vdots \\ \lambda_1^{\infty h} e_{\infty h}^0 + \lambda_2^{\infty h} e_{\infty h}^1 + \lambda_3^{\infty h} e_{\infty h}^2 \end{array} \right\} \xrightarrow{F_{21}} \left\{ \begin{array}{c} \lambda_1^{1h} e_{1h}^0 + \lambda_2^{1h} e_{1h}^1 + \lambda_3^{1h} e_{1h}^2 \\ \lambda_1^{2h} e_{2h}^0 + \lambda_2^{2h} e_{2h}^1 + \lambda_3^{2h} e_{2h}^2 \\ \vdots \\ \lambda_1^{(\infty-1)h} e_{(\infty-1)h}^0 + \lambda_2^{(\infty-1)h} e_{(\infty-1)h}^1 + \lambda_3^{(\infty-1)h} e_{(\infty-1)h}^2 \end{array} \right\}$$

$$\dots \lim_{\longrightarrow} F_{2n} \lambda_1^{1h} e_{1h}^0 + \lambda_2^{1h} e_{1h}^1 + \lambda_3^{1h} e_{1h}^2$$

the 2- chaotic chains are

$$\left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^0 \end{array} \right\} \xrightarrow{F_{21}} \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} a_{(\infty-1)h}^0 \end{array} \right\} \dots \lim_{\longrightarrow} F_{2n} \lambda_1^{1h} a_{1h}^0$$

and

$$\left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^0 \end{array} \right\} \xrightarrow{F_{21}} \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} a_{(\infty-1)h}^0 \end{array} \right\} \dots \lim_{\longrightarrow} F_{2n} \lambda_1^{1h} a_{1h}^0,$$

and the 3- chaotic chains are

$$\left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^0 \end{array} \right\} \xrightarrow{F_{21}} \left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} l_{(\infty-1)h}^0 \end{array} \right\} \dots \lim_{\longrightarrow} F_{2n} \lambda_1^{1h} l_{1h}^0,$$

$$\left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^0 \end{array} \right\} \xrightarrow{F_{21}} \left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} l_{(\infty-1)h}^0 \end{array} \right\} \dots \lim_{\longrightarrow} F_{2n} \lambda_1^{1h} l_{1h}^0.$$

Case(3):

Here the chaotic on the vertices v^0, v^1, v^2, v^3 will be reduce, such that $F_{3m}(v_{jh}^i) = v_{(j-1)h}^i$, where $i = 0, 1, 2, 3, j = 0, 1, 2, \dots, \infty, m = 1, \dots, n$. The adjacent $A_h(G_h)$, incident $I_h(G_h)$, vertex area $M_h(G_h)$, and vertex volume $N_h(G_h)$ matrices will change, but the edge $E_h(G_h)$, area $R_h(G_h)$, volume $V_h(G_h)$, edge area $H_h(G_h)$, edge volume $J_h(G_h)$ matrices, and area volume $U_h(G_h)$ matrices will not change.

See Fig.(4).

$$\begin{aligned}
 A_h(F_{31}(G_h)) &= \begin{bmatrix} 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \end{bmatrix} \\
 \dots \lim_{F_{3n}} A_h(\lim F_{3n}(G_h)) &= \begin{bmatrix} 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \\ 1_{01h} & 0_{01h} & 1_{01h} & 1_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \end{bmatrix}, \\
 *I_h(G_h) &= \begin{bmatrix} 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{31}} \\
 I_h(F_{31}(G_h)) &= \begin{bmatrix} 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \end{bmatrix} \\
 \dots \lim_{F_{3n}} I_h(\lim F_{3n}(G_h)) &= \begin{bmatrix} 1_{01h} & 0_{01h} & 0_{01h} \\ 1_{01h} & 1_{01h} & 1_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} \\ 0_{01h} & 0_{01h} & 1_{01h} \end{bmatrix}, \\
 *M_h(G_h) &= \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{31}} M_h(F_{31}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \end{bmatrix} \\
 \dots \lim_{F_{3n}} M_h(\lim F_{3n}(G_h)) &= \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 0_{01h} \\ 1_{01h} \end{bmatrix}, \\
 *N_h(G_h) &= \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \\ 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{31}} N_h(F_{31}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \end{bmatrix} \\
 \dots \lim_{F_{3n}} N_h(\lim F_{3n}(G_h)) &= \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 1_{01h} \\ 0_{01h} \end{bmatrix},
 \end{aligned}$$

The 1- chaotic, 2- chaotic, 3- chaotic chains will not change. Only the 0- chaotic chain will change as follows

$$\left\{ \begin{array}{l} \lambda_1^{1h} v_{1h}^0 + \lambda_2^{1h} v_{1h}^1 + \lambda_3^{1h} v_{1h}^2 + \lambda_4^{1h} v_{1h}^3 \\ \lambda_1^{2h} v_{2h}^0 + \lambda_2^{2h} v_{2h}^1 + \lambda_3^{2h} v_{2h}^2 + \lambda_4^{2h} v_{2h}^3 \\ \vdots \\ \lambda_1^{\infty h} v_{\infty h}^0 + \lambda_2^{\infty h} v_{\infty h}^1 + \lambda_3^{\infty h} v_{\infty h}^2 + \lambda_4^{\infty h} v_{\infty h}^3 \end{array} \right\} \xrightarrow{F_{31}} \left\{ \begin{array}{l} \lambda_1^{1h} v_{1h}^0 + \lambda_2^{1h} v_{1h}^1 + \lambda_3^{1h} v_{1h}^2 + \lambda_4^{1h} v_{1h}^3 \\ \lambda_1^{2h} v_{2h}^0 + \lambda_2^{2h} v_{2h}^1 + \lambda_3^{2h} v_{2h}^2 + \lambda_4^{2h} v_{2h}^3 \\ \vdots \\ \lambda_1^{(\infty-1)h} v_{(\infty-1)h}^0 + \lambda_2^{(\infty-1)h} v_{(\infty-1)h}^1 \\ + \lambda_3^{(\infty-1)h} v_{(\infty-1)h}^2 + \lambda_4^{(\infty-1)h} v_{(\infty-1)h}^3 \end{array} \right\}$$

$$\xrightarrow{\dots \lim F_{3n}} \lambda_1 v^0 + \lambda_2 v^1 + \lambda_3 v^2 + \lambda_4 v^3,$$

Case(4) :

In this case, the folding acts on the chaotics of the edges e^0, e^1, e^2 , such that $F_{4m}(e_{jh}^i) = e_{(j-1)h}^i$, where $i = 0, 1, 2, j = 0, 1, 2, \dots, \infty, m = 1, \dots, n$. Then the chaotic adjacent $A_h(G_h)$, edge $E_h(G_h)$, incident $I_h(G_h)$, edge area $H_h(G_h)$, edge volume $U_h(G_h)$ matrices and the 1-chaotic chains only will change.

See Fig.(5).

The matrices will be in the form

$$\begin{aligned} *A_h(G_h) &= \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{41}} \\ A_h(F_{41}(G_h)) &= \begin{bmatrix} 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \end{bmatrix} \\ \dots \lim_{\xrightarrow{F_{4n}}} F_{4n} A_h(\lim F_{4n}(G_h)) &= \begin{bmatrix} 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \\ 1_{01h} & 0_{01h} & 1_{01h} & 1_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} & 0_{01h} \end{bmatrix}, \\ *E_h(G_h) &= \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} \\ 1_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{41}} \\ E_h(F_{41}(G_h)) &= \begin{bmatrix} 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \end{bmatrix} \\ \dots \lim_{\xrightarrow{F_{4n}}} F_{4n} E_h(\lim F_{4n}(G_h)) &= \begin{bmatrix} 0_{01h} & 1_{01h} & 1_{01h} \\ 1_{01h} & 0_{01h} & 1_{01h} \\ 1_{01h} & 1_{01h} & 0_{01h} \end{bmatrix}, \\ *I_h(G_h) &= \begin{bmatrix} 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{41}} \\ I_h(F_{41}(G_h)) &= \begin{bmatrix} 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} & 0_{012\dots(\infty-1)h} & 1_{012\dots(\infty-1)h} \end{bmatrix} \\ \dots \lim_{\xrightarrow{F_{4n}}} F_{4n} I_h(\lim F_{4n}(G_h)) &= \begin{bmatrix} 1_{01h} & 0_{01h} & 0_{01h} \\ 1_{01h} & 1_{01h} & 1_{01h} \\ 0_{01h} & 1_{01h} & 0_{01h} \\ 0_{01h} & 0_{01h} & 1_{01h} \end{bmatrix}, \\ *H_h(G_h) &= \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{41}} H_h(F_{41}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \end{bmatrix} \\ \dots \lim_{\xrightarrow{F_{4n}}} F_{4n} H_h(\lim F_{4n}(G_h)) &= \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 1_{01h} \end{bmatrix}, \\ *J_h(G_h) &= \begin{bmatrix} 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \\ 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{41}} J_h(F_{41}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \end{bmatrix} \end{aligned}$$

$$\xrightarrow{\dots \lim F_{4n}} J_h(\lim F_{4n}(G_h)) = \begin{bmatrix} 0_{01h} \\ 1_{01h} \\ 0_{01h} \end{bmatrix},$$

and it's 1-chaotic chains are

$$\left\{ \begin{array}{c} \lambda_1^{1h} e_{1h}^0 + \lambda_2^{1h} e_{1h}^1 + \lambda_3^{1h} e_{1h}^2 \\ \lambda_1^{2h} e_{2h}^0 + \lambda_2^{2h} e_{2h}^1 + \lambda_3^{2h} e_{2h}^2 \\ \vdots \\ \lambda_1^{\infty h} e_{\infty h}^0 + \lambda_2^{\infty h} e_{\infty h}^1 + \lambda_3^{\infty h} e_{\infty h}^2 \end{array} \right\} \xrightarrow{F_{41}} \left\{ \begin{array}{c} \lambda_1^{1h} e_{1h}^0 + \lambda_2^{1h} e_{1h}^1 + \lambda_3^{1h} e_{1h}^2 \\ \lambda_1^{2h} e_{2h}^0 + \lambda_2^{2h} e_{2h}^1 + \lambda_3^{2h} e_{2h}^2 \\ \vdots \\ \lambda_1^{(\infty-1)h} e_{(\infty-1)h}^0 + \lambda_2^{(\infty-1)h} e_{(\infty-1)h}^1 + \lambda_3^{(\infty-1)h} e_{(\infty-1)h}^2 \end{array} \right\}$$

$$\xrightarrow{\dots \lim F_{4n}} \{ \lambda_1 e^0 + \lambda_2 e^1 + \lambda_3 e^2 \}.$$

Corollary(1) :

The folding of the chaotic edges of a chaotic general tree leads to folding of it's chaotic vertices.

Case(5) :

In this case, we fold the chaotics of the area a^0 , such that $F_5(a_{jh}^0) = a_{(j-1)h}^0$, where $j = 0, 1, 2, \dots, \infty$. The matrices which will be changed are the adjacent $A_h(G_h)$, area $R_h(G_h)$, vertex area $M_h(G_h)$, edge area $H_h(G_h)$ and the area volume $U_h(G_h)$ matrices.

See Fig.(6).

$$*A_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{51}}$$

$$A_h(F_{51}(G_h)) = \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots(\infty-1)h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix}$$

$$\xrightarrow{\dots \lim F_{5n}} A_h(\lim F_{5n}(G_h)) = \begin{bmatrix} 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \\ 1_{012\dots\infty h} & 0_{012\dots\infty h} & 1_{012\dots\infty h} & 1_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{01h} & 0_{012\dots\infty h} \\ 0_{012\dots\infty h} & 1_{012\dots\infty h} & 0_{012\dots\infty h} & 0_{012\dots\infty h} \end{bmatrix},$$

$$*R_h(G_h) = [0_{012\dots\infty h}] \xrightarrow{F_{51}} R_h(F_{51}(G_h)) = [0_{012\dots(\infty-1)h}]$$

$$\xrightarrow{\dots \lim F_{5n}} R_h(\lim F_{5n}(G_h)) = [0_{01h}],$$

$$*M_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{51}} M_h(F_{51}(G_h)) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots\infty h} \end{bmatrix}$$

$$\xrightarrow{\dots \lim F_{5n}} M_h(\lim F_{5n}(G_h)) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 0_{01h} \\ 1_{012\dots\infty h} \end{bmatrix},$$

$$*H_h(G_h) = \begin{bmatrix} 0_{012\dots\infty h} \\ 0_{012\dots\infty h} \\ 1_{012\dots\infty h} \end{bmatrix} \xrightarrow{F_{51}} H_h(F_{51}(G_h)) = \begin{bmatrix} 0_{012\dots(\infty-1)h} \\ 0_{012\dots(\infty-1)h} \\ 1_{012\dots(\infty-1)h} \end{bmatrix}$$

$$\xrightarrow{\dots \lim F_{5n}} H_h(\lim F_{5n}(G_h)) = \begin{bmatrix} 0_{01h} \\ 0_{01h} \\ 1_{01h} \end{bmatrix}$$

and

$$\begin{aligned} *U_h(G_h) &= [0_{012... \infty h}] \xrightarrow{F_{51}} U_h(F_{51}(G_h)) = [0_{012...(\infty-1)h}] \\ &\xrightarrow{\dots \lim F_{5n}} U_h(\lim F_{5n}(G_h)) = [0_{01h}]. \end{aligned}$$

It's 2- chaotic chains are

$$\begin{aligned} \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^0 \end{array} \right\} &\xrightarrow{F_{51}} \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} a_{(\infty-1)h}^0 \end{array} \right\} \xrightarrow{\dots \lim F_{5n}} \{ \lambda_1 a^0 \}, \\ \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} a_{\infty h}^0 \end{array} \right\} &\xrightarrow{F_{5n}} \left\{ \begin{array}{c} \lambda_1^{1h} a_{1h}^0 \\ \lambda_1^{2h} a_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} a_{(\infty-1)h}^0 \end{array} \right\} \xrightarrow{\dots \lim F_{5n}} \{ \lambda_1 a^0 \}. \end{aligned}$$

Case(6) :

Here the folding acts on the chaotic of the volume. The edge $E_h(G_h)$, area $R_h(G_h)$, vertex area $M(G_h)$, and edge area $H(G_h)$ matrices will not change but the adjacent $A(G_h)$, incident $I(G_h)$, volume $V(G_h)$, vertex volume $N_h(G_h)$ and edge volume $J(G_h)$, area volume $U_h(G_h)$ matrices will change, where $F_{6m}(l_{jh}^0) = l_{(j-1)h}^0$, where $j = 0, 1, 2, \dots, \infty, m = 1, \dots, n$.

See Fig.(7).

such that

$$\begin{aligned} *A_h(G_h) &= \begin{bmatrix} 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 0_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \end{bmatrix} \xrightarrow{F_{61}} \\ A_h(F_{61}(G_h)) &= \begin{bmatrix} 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 0_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012...(\infty-1)h} \end{bmatrix} \\ \dots \lim F_{6n} A_h(\lim F_{6n}(G_h)) &= \begin{bmatrix} 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 0_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} & 0_{01h} \end{bmatrix}, \end{aligned}$$

$$\begin{aligned} *V_h(G_h) &= [0_{012... \infty h}] \xrightarrow{F_{61}} V_h(F_{61}(G_h)) = [0_{012...(\infty-1)h}] \\ &\xrightarrow{\dots \lim F_{6n}} V_h(\lim F_{6n}(G_h)) = [0_{01h}], \end{aligned}$$

$$\begin{aligned} *I_h(G_h) &= \begin{bmatrix} 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 0_{012... \infty h} & 1_{012... \infty h} \end{bmatrix} \xrightarrow{F_{61}} \\ I_h(F_{61}(G_h)) &= \begin{bmatrix} 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 0_{012... \infty h} & 1_{012...(\infty-1)h} \end{bmatrix} \end{aligned}$$

$$\begin{aligned}
\lim_{n \rightarrow \infty} F_{6n} I_h(\lim F_{6n}(G_h)) &= \begin{bmatrix} 1_{012... \infty h} & 0_{012... \infty h} & 0_{012... \infty h} \\ 1_{012... \infty h} & 1_{012... \infty h} & 1_{012... \infty h} \\ 0_{012... \infty h} & 1_{012... \infty h} & 0_{012... \infty h} \\ 0_{012... \infty h} & 0_{012... \infty h} & 1_{01h} \end{bmatrix}, \\
*N_h(G_h) &= \begin{bmatrix} 0_{012... \infty h} \\ 0_{012... \infty h} \\ 1_{012... \infty h} \\ 0_{012... \infty h} \end{bmatrix} \xrightarrow{F_{61}} N_h(F_{61}(G_h)) = \begin{bmatrix} 0_{012... \infty h} \\ 0_{012... \infty h} \\ 1_{012... \infty h} \\ 0_{012... \infty h} \end{bmatrix} \\
\lim_{n \rightarrow \infty} F_{6n} N_h(\lim F_{6n}(G_h)) &= \begin{bmatrix} 0_{012... \infty h} \\ 0_{012... \infty h} \\ 1_{012... \infty h} \\ 0_{012... \infty h} \end{bmatrix}, \\
*J_h(G_h) &= \begin{bmatrix} 0_{012... \infty h} \\ 1_{012... \infty h} \\ 0_{012... \infty h} \end{bmatrix} \xrightarrow{F_{61}} J_h(F_{61}(G_h)) = \begin{bmatrix} 0_{012...(\infty-1)h} \\ 1_{012...(\infty-1)h} \\ 0_{012...(\infty-1)h} \end{bmatrix} \\
\lim_{n \rightarrow \infty} F_{6n} J_h(\lim F_{6n}(G_h)) &= \begin{bmatrix} 0_{01h} \\ 1_{01h} \\ 0_{01h} \end{bmatrix}, \\
*U_h(G_h) &= [0_{012... \infty h}] \xrightarrow{F_{61}} U_h(F_{61}(G_h)) = [0_{012...(\infty-1)h}] \\
\lim_{n \rightarrow \infty} F_{6n} U_h(\lim F_{6n}(G_h)) &= [0_{01h}].
\end{aligned}$$

and the 3- chaotic chains are

$$\left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^0 \end{array} \right\} \xrightarrow{F_{61}} \left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} l_{(\infty-1)h}^0 \end{array} \right\} \xrightarrow{\lim_{n \rightarrow \infty} F_{6n}} \lambda_1 l^0,$$

and

$$\left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{\infty h} l_{\infty h}^0 \end{array} \right\} \xrightarrow{F_{61}} \left\{ \begin{array}{c} \lambda_1^{1h} l_{1h}^0 \\ \lambda_1^{2h} l_{2h}^0 \\ \vdots \\ \lambda_1^{(\infty-1)h} l_{(\infty-1)h}^0 \end{array} \right\} \xrightarrow{\lim_{n \rightarrow \infty} F_{6n}} \lambda_1 l^0.$$

From the above discussion, we will arrive to the following theorems:

Theorem (1):

The folding of the chaotics into itself which reduce the number of chaotics will induce a folding to the representing matrices and also for the chains.

Proof :

The prove comes directly from the above cases.

Theorem (2) :

The folding of the vertices not necessary induce a folding for edges and volumes.

Proof :

See Fig.(3).and Fig.(4).

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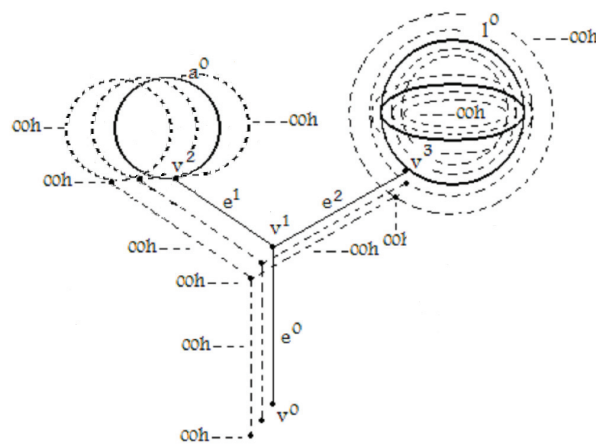


Figure 1.

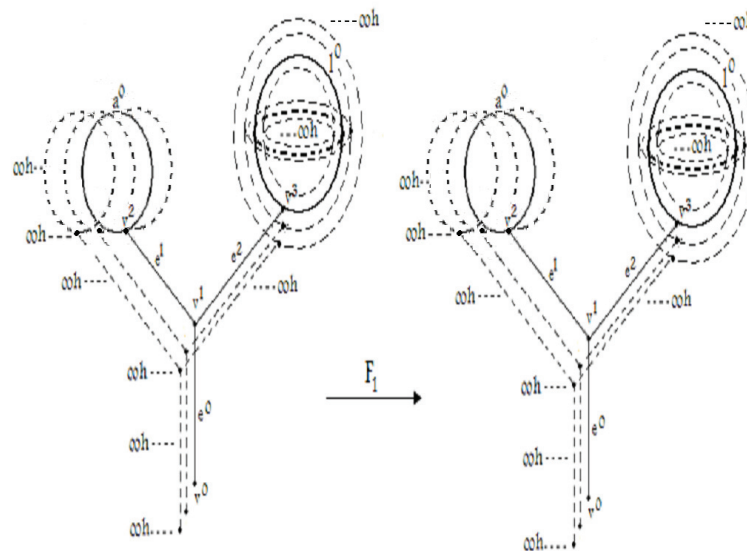


Figure 2.

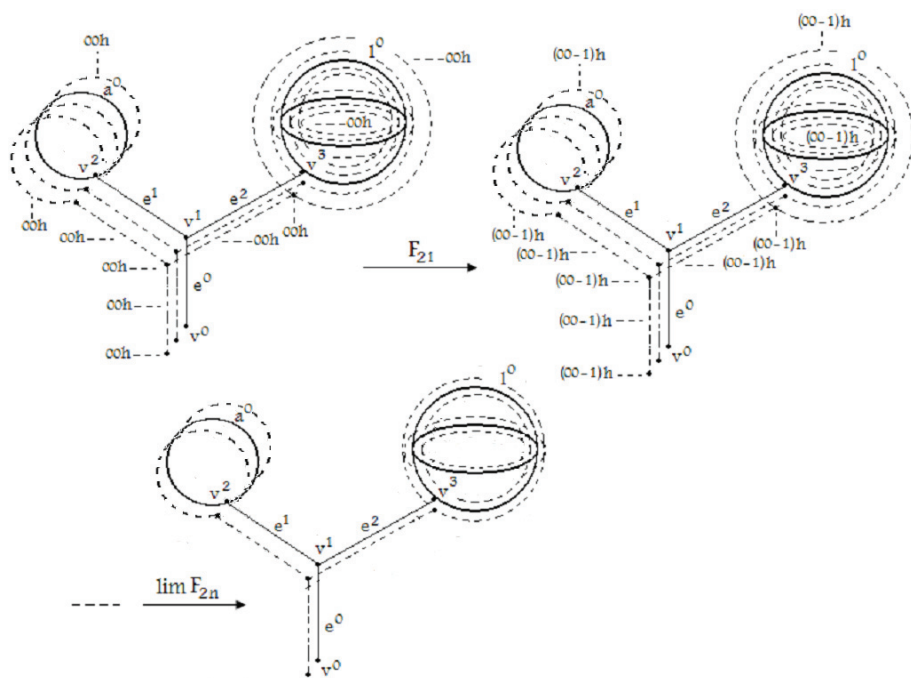


Figure 3.

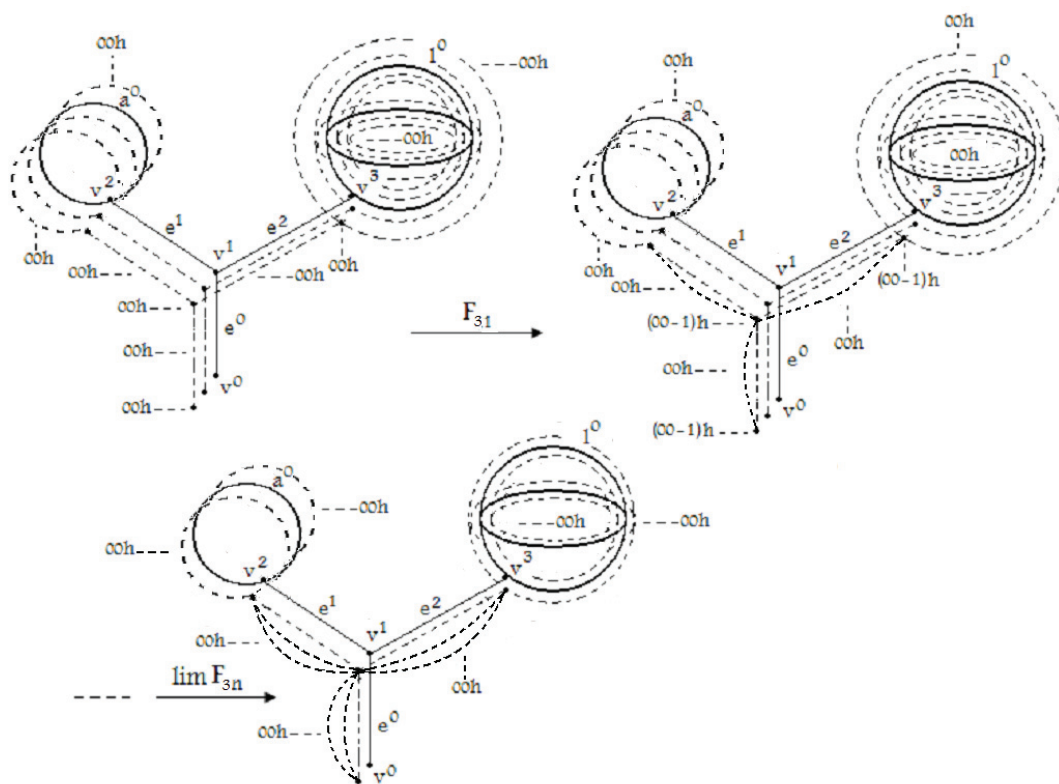


Figure 4.

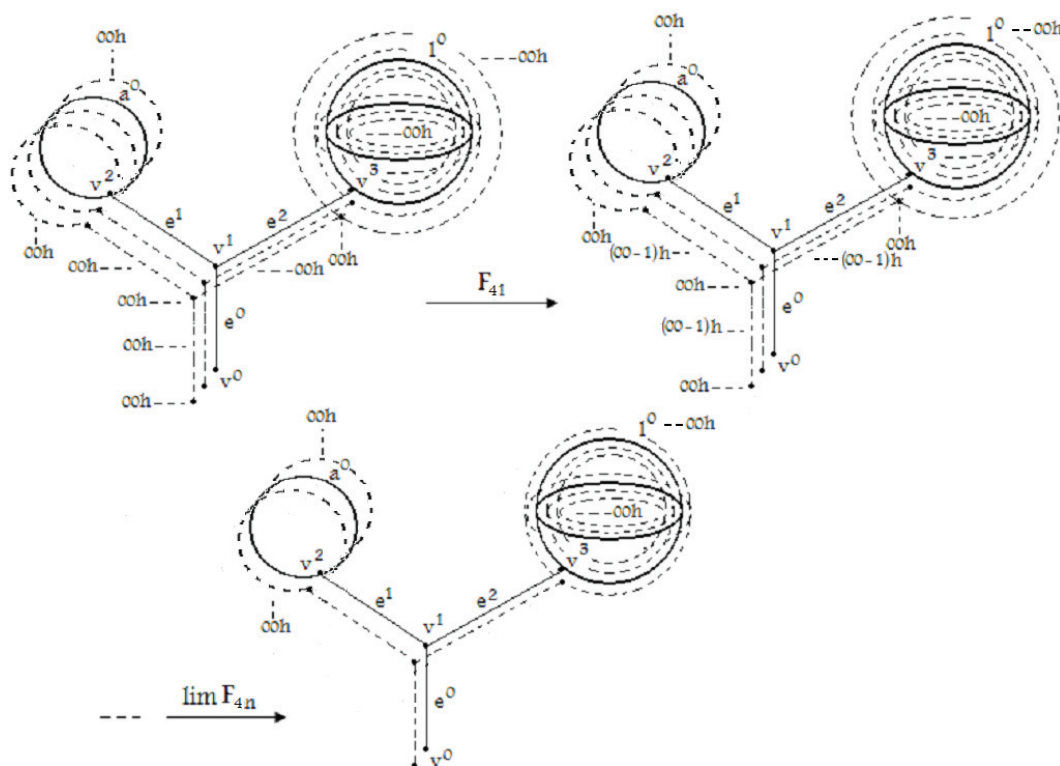


Figure 5.

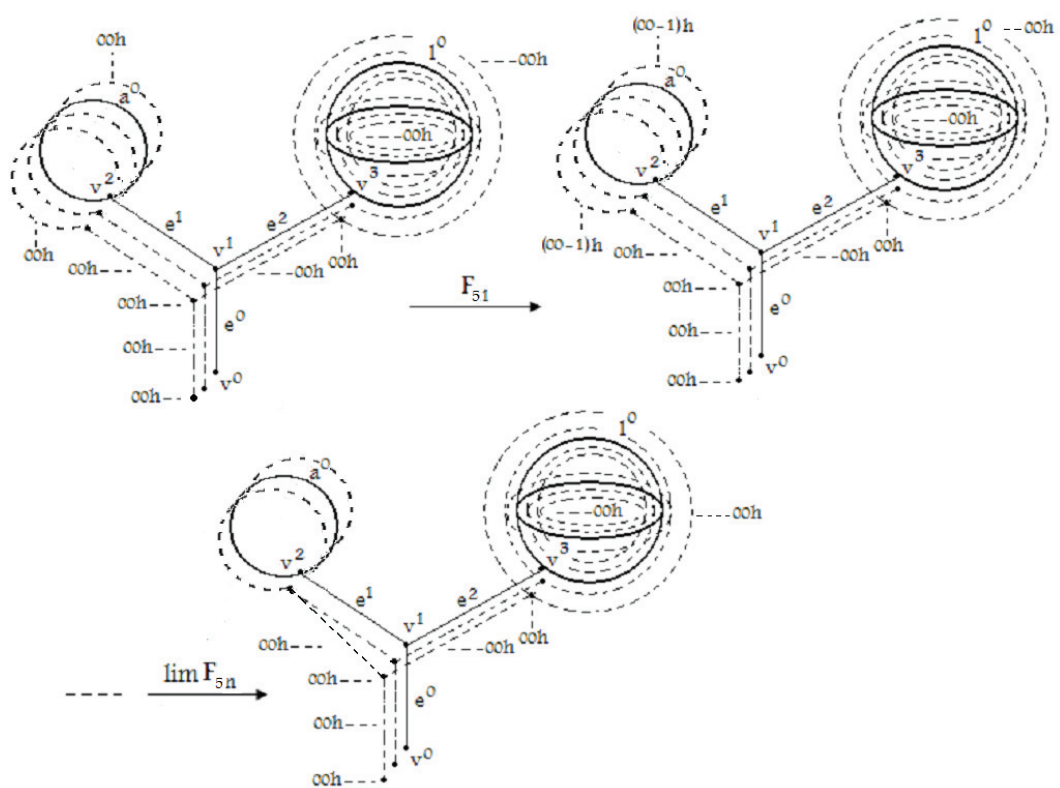


Figure 6.

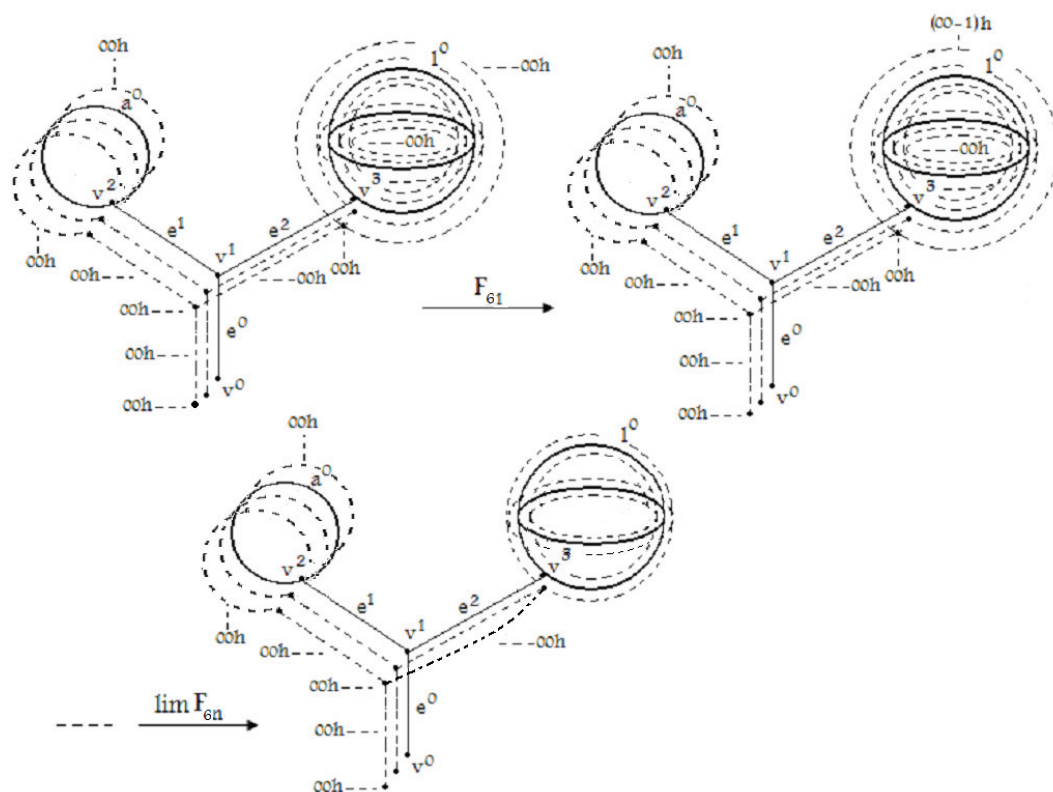


Figure 7.