Using Mean Oxidation Number of Organic Carbons to Quantify Buswell's Equation

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Abstract

Buswell's equation can represent anaerobic digestion. The overall stoichiometric chemical equation is important for the counting of biomethane and theoretical biochemical methane potential. Although the concept of oxidation number of organic carbons has been applied in organic chemistry and biochemistry, the relationship between mean oxidation number of organic carbons and quantity of biomethane has not been studied. This article uses the H-atom method as a balancing tool to build a Buswell's model which can help understand the redox nature of organic compounds and establish the mathematical relationships among the stoichiometric coefficients of Buswell's equation, elemental composition of organic carbons as a metric, the mathematical equations for the counting of biomethane and theoretical biochemical methane potential are attained. The parameters of Buswell's equation can also be quantified by any given structural formula of an organic compound.

Keywords: anaerobic digestion, Buswell's equation, H-atom method, mean oxidation number of organic carbons, elemental composition, biomethane, theoretical biochemical methane potential, Buswell's ratio, biogas ratio, methane content percentage

1. Introduction

Anaerobic digestion (AD) is a sequence of bacteria-mediated biochemical processes and technologies (Batstone et al., 2002; Angelidaki & Sanders, 2004; Bidlingmaier, 2016; Banks, 2020). It is widely used for waste management, bioenergy production, and sustainable development (Horan et al., 2019; Holden et al., 2021; Torales, 2013). It is a cost-effective alternative to aerobic digestion, and has advantages in energy saving, reduction of sludge yield, and production of biofuel (Fang, 2010).

Buswell (Buswell & Boruff, 1932; Buswell & Hatfield, 1936; Buswell & Mueller, 1952) established the overall molecular chemical equation to represent organic matter in terms of their elemental composition regarding AD. An example of an unbalanced Buswell's equation (Symons & Buswell, 1933; Boyle, 1977) is shown below:

$$C_xH_yO_zN_vS_u+H_2O \rightarrow CH_4+CO_2+NH_3+H_2S$$

The Buswell's equation is a model to quantify biomethane and the biochemical methane potential is a critical measuring parameter in AD (Holliger et al., 2016; Rodrigues et al., 2019; Yasim & Buyong, 2023; Koch et al., 2019).

AD has been given less attention than aerobic digestion in biochemistry textbooks (Shen & Chen, 2021) and BEq is rarely mentioned in physical sciences and life sciences. Many students are unable to understand and manipulate the stoichiometric BEq. Although the concept of mean oxidation number of organic carbons has been applied in organic chemistry (Hanson, 1990; Halkides, 2000; Bentley et al., 2002; Yuen & Lau, 2022a), environmental chemistry (Kroll et al., 2011), biogeochemistry (Masiello et al., 2008; LaRowe & Van Cappellen, 2011; Dick et al., 2019), water treatment (Vogel et al., 2000), and organic combustion reaction (Yuen & Lau, 2023a), the relationship between ON_C and nCH_4 has not been studied.

The purpose of this article is to explore the BEq model which can help unpack the redox nature of organic compounds and establish the mathematical relationship between mean oxidation number of organic carbons (ON_C) and theoretical quantity of biomethane (nCH_4). The H-atom method is used for balancing and deducting BEqs (Yuen & Lau, 2023b). The mathematical equation between ON_C and nCH_4 is then derived. Lastly, the Buswell's ratio, biogas ratio, biomethane content percentage, and theoretical biochemical methane potential (TBMP) can be calculated by using ON_C as a metric for any given organic compound.

2. Procedures for Counting ON_N, ON_C, and Balancing BEq

Organonitrogen compounds are rich in nature and nitrogen is an essential element in life (Bada, 1998). The general formula of organonitrogen compound, $C_xH_yO_zN_v$, is chosen to be the model molecule for balancing and deducting BEqs. The chemical formula of $C_2H_5O_2N$ has different isomers. Three of them are selected and shown as follows:



The unbalanced BEq is shown as: $C_2H_5O_2N+H_2O\rightarrow CH_4+CO_2+NH_3$

- Step 3. Balance the BEq by using the H-atom method (Yuen & Lau, 2021; 2022b)
- Step 3.1 Divide an overall equation into two half reactions

 $C_2H_5O_2N \rightarrow CH_4+NH_3$ $C_2H_5O_2N \rightarrow CO_2+NH_3$

- Step 3.2 Balance two half reactions (from $C \rightarrow N \rightarrow O \rightarrow H$)
 - $\begin{array}{l} C_{2}H_{5}O_{2}N \rightarrow CH_{4} + NH_{3} \\ C_{2}H_{5}O_{2}N \rightarrow 2CH_{4} + NH_{3} \\ C_{2}H_{5}O_{2}N \rightarrow 2CH_{4} + NH_{3} + 2O \\ C_{2}H_{5}O_{2}N + 6H \rightarrow 2CH_{4} + NH_{3} + 2O \\ C_{2}H_{5}O_{2}N + 6H + 4H \rightarrow 2CH_{4} + NH_{3} + 2O + 4H \\ C_{2}H_{5}O_{2}N + 10H \rightarrow 2CH_{4} + NH_{3} + 2H_{2}O \\ C_{2}H_{5}O_{2}N \rightarrow CO_{2} + NH_{3} \\ C_{2}H_{5}O_{2}N \rightarrow 2CO_{2} + NH_{3} \\ C_{2}H_{5}O_{2}N + 2O \rightarrow 2CO_{2} + NH_{3} \\ C_{2}H_{5}O_{2}N + 2O \rightarrow 2CO_{2} + NH_{3} \\ C_{2}H_{5}O_{2}N + 2O \rightarrow 2CO_{2} + NH_{3} + 2H \\ C_{2}H_{5}O_{2}N + 2O + 4H \rightarrow 2CO_{2} + NH_{3} + 2H + 4H \\ C_{2}H_{5}O_{2}N + 2H_{2}O \rightarrow 2CO_{2} + NH_{3} + 6H \end{array}$

Step 3.3 Combine two half reactions with equivalence of H-atom (LCM = 30)

$$(C_{2}H_{5}O_{2}N+10H\rightarrow 2CH_{4}+NH_{3}+2H_{2}O) \times 3$$
$$(C_{2}H_{5}O_{2}N+2H_{2}O\rightarrow 2CO_{2}+NH_{3}+6H) \times 5$$
$$8C_{2}H_{5}O_{2}N+4H_{2}O\rightarrow 6CH_{4}+10CO_{2}+8NH_{3}$$
$$C_{2}H_{5}O_{2}N+\frac{1}{2}H_{2}O\rightarrow \frac{3}{4}CH_{4}+\frac{5}{4}CO_{2}+NH_{3}$$

Step 4. Identify the stoichiometric coefficients of nH₂O, nCH₄, and nCO₂

The stochiometric coefficients of $nH_2O = \frac{1}{2}$, $nCH_4 = \frac{3}{4}$, and $nCO_2 = \frac{5}{4}$ can be identified by the balanced BEq.



Step 5. Count the ON_C of

The ON_C

By using the molecular formula method (IUPAC, 2019): $\Sigma ON_i = 0$

$$2ON_{C} + 5ON_{H} + 2ON_{O} + 1ON_{N} = 0$$

$$2ON_{C} = -5ON_{H} - 2ON_{O} - 1ON_{N}$$

$$\therefore ON_{H} = +1; ON_{O} = -2; ON_{N} = -3$$

$$\therefore 2ON_{C} = -5(+1) - 2(-2) - 1(-3)$$

$$ON_{C} = \frac{-5+4+3}{2} = +1$$

$$H_{2}N \longrightarrow OH (C_{2}H_{5}O_{2}N) \text{ equals } +1.$$

3. Relationships among ON_N, ON_C, and Stoichiometric Coefficients of C₂H₅O₂N Molecules in BEq

By using the same procedure shown in Example 1 ($ON_N = -3$), different N-products are assigned by different ON_N . Nitrogen atoms have nine individual oxidation numbers (ON_N) and their values lie between the integer range of -3 to +5. The chemical formulas of N-products are combined with H-atom, O-atom, or both O-atom and H-atom. The resulting oxidation numbers of ON_N and ON_C , stoichiometric coefficients of nH_2O , nCH_4 , and nCO_2 are summarized in Table 1. When the value of nH_2O is positive, it is on the reactant's side. When the value is negative, it is on the product's side.

Equation #	Balanced Buswell's equation	ON _N	nH ₂ O	nCH ₄	nCO ₂	ON _C
1	$C_2H_5O_2N + \frac{1}{2}H_2O \rightarrow \frac{3}{4}CH_4 + \frac{5}{4}CO_2 + NH_3$	-3	$\frac{1}{2}$	$\frac{3}{4}$	<u>5</u> 4	+1
2	$C_2H_5O_2N + \frac{1}{4}H_2O \rightarrow \frac{7}{8}CH_4 + \frac{9}{8}CO_2 + \frac{1}{2}N_2H_4$	-2	$\frac{1}{4}$	<u>7</u> 8	<u>9</u> 8	$+\frac{1}{2}$
3	$C_2H_5O_2N \rightarrow CH_4 + CO_2 + \frac{1}{2}N_2H_2$	-1	0	1	1	0
4	$C_2H_5O_2N+H_2O \rightarrow CH_4+CO_2+NH_2OH$	-1	1	1	1	0
5	$C_{2}H_{5}O_{2}N \rightarrow \frac{9}{8}CH_{4} + \frac{7}{8}CO_{2} + \frac{1}{2}N_{2} + \frac{1}{4}H_{2}O$	0	$-\frac{1}{4}$	<u>9</u> 8	<u>7</u> 8	$-\frac{1}{2}$
6	$C_{2}H_{5}O_{2}N \rightarrow \frac{5}{4}CH_{4} + \frac{3}{4}CO_{2} + \frac{1}{2}N_{2}O + \frac{1}{2}H_{2}O$	+1	$-\frac{1}{2}$	<u>5</u> 4	$\frac{3}{4}$	-1
7	$C_2H_5O_2N \rightarrow \frac{11}{8}CH_4 + \frac{5}{8}CO_2 + NO + \frac{3}{4}H_2O$	+2	$-\frac{3}{4}$	$\frac{11}{8}$	<u>5</u> 8	$-\frac{3}{2}$
8	$C_2H_5O_2N+H_2O\rightarrow \frac{3}{2}CH_4+\frac{1}{2}CO_2+HNO_2$	+3	1	$\frac{3}{2}$	$\frac{1}{2}$	-2
9	$C_{2}H_{5}O_{2}N + \frac{1}{2}H_{2}O \rightarrow \frac{3}{2}CH_{4} + \frac{1}{2}CO_{2} + \frac{1}{2}N_{2}O_{3}$	+3	$\frac{1}{2}$	<u>3</u> 2	$\frac{1}{2}$	-2
10	$C_{2}H_{5}O_{2}N \rightarrow \frac{13}{8}CH_{4} + \frac{3}{8}CO_{2} + \frac{1}{2}NO_{2} + \frac{5}{4}H_{2}O_{3}$	+4	$-\frac{5}{4}$	<u>13</u> 8	<u>3</u> 8	$-\frac{5}{2}$
11	$C_2H_5O_2N \rightarrow \frac{7}{4}CH_4 + \frac{1}{4}CO_2 + HNO_3 + \frac{3}{2}H_2O$	+5	$-\frac{3}{2}$	$\frac{7}{4}$	$\frac{1}{4}$	-3
12	$C_2H_5O_2N+H_2O \rightarrow \frac{7}{4}CH_4 + \frac{1}{4}CO_2 + \frac{1}{2}N_2O_5$	+5	1	$\frac{7}{4}$	$\frac{1}{4}$	-3

Table 1. Parameters of C₂H₅O₂N molecules in the balanced BEqs

With reference to Table 1, when Equation 1 and Equation 3 are compared, NH_3 ($ON_N = -3$) and N_2H_2 ($ON_N = -1$) have different ON_N , and their ON_C are +1 and 0 respectively. Consequently, they produce different stoichiometric coefficients of nCH_4 and nCO_2 .

$$H_2N \xrightarrow{O} OH$$
, $ON_N = -3$) $C_2H_5O_2N + \frac{1}{2}H_2O \rightarrow \frac{3}{4}CH_4 + \frac{5}{4}CO_2 + NH_3(ON_N = -3)$

, $ON_N = -1$) $C_2H_5O_2N \rightarrow CH_4 + CO_2 + \frac{1}{2}N_2H_2$ ($ON_N = -1$)

Equation 3:

HO (H

When Equation 8 and Equation 9 are compared, N-products of HNO_2 and N_2O_3 have identical ON_N but different chemical formulas. Their ON_N produce the same ON_C of -2. Their stoichiometric coefficients of nCH_4 and nCO_2 remain the same in Equations 8 and 9.

Equation 8:
$$\begin{pmatrix} H & H & O \\ H & -C & -C & -N^+ \\ H & H & O^- \end{pmatrix}$$
, $ON_N = +3) C_2H_5O_2N + H_2O \rightarrow \frac{3}{2}CH_4 + \frac{1}{2}CO_2 + HNO_2 (ON_N = +3)$

Equation 9:

$$C = C = N + H + O^{-1}$$
, $ON_N = +3$) $C_2H_5O_2N + \frac{1}{2}H_2O \rightarrow \frac{3}{2}CH_4 + \frac{1}{2}CO_2 + \frac{1}{2}N_2O_3$ ($ON_N = +3$)

BEq is a biochemical redox reaction, in which the carbon atoms of an organic molecule disproportionate to CH_4 and CO_2 . An ideal BEq model indicates that electron transfer occurs in sole organic carbons of organic compound, and other non-carbon atoms are not involved in the redox process.

4. Deducting the General BEq of C_xH_yO_zN_v Molecules

 NH_3 ($ON_N = -3$) is chosen as a N-product to balance BEq of $C_xH_yO_zN_v$ in Example 2.

Example 2. Deducting the BEq reaction of C_xH_yO_zN_v

Step 1. Set up the BEq reaction by choosing [N-product] ($ON_N = -3$)

$$C_xH_yO_zN_v+H_2O\rightarrow CH_4+CO_2+NH_3$$

Step 2. Deduct the BEq by using the H-atom method

Step 2.1 Divide an overall equation into two half reactions

$$C_xH_yO_zN_v \rightarrow CH_4 + NH_3$$

$$C_xH_yO_zN_v \rightarrow CO_2 + NH_3$$

Step 2.2 Balance two half reactions

$$\begin{split} &C_xH_yO_zN_v{\rightarrow}xCH_4{+}vNH_3\\ &C_xH_yO_zN_v{+}(4x{-}y{+}3v{+}2z)H{\rightarrow}vCH_4{+}vNH_3{+}zH_2O\\ &C_xH_yO_zN_v{\rightarrow}xCO_2{+}vNH_3\\ &C_xH_yO_zN_v{+}(2x{-}z)H_2O{\rightarrow}xCO_2{+}vNH_3{+}(4x{+}y{-}2z{-}3v)H \end{split}$$

Step 2.3 Combine two half reactions with equivalence of H-atom $\{LCM=(4x-y+3y+2z)(4x+y-2z-3y)\}$

 $(C_xH_yO_zN_v+(4x-y+3v+2z)H\rightarrow vCH_4+vNH_3+zH_2O)\times(4x+y-2z-3v)$

$$(C_xH_yO_zN_v+(2x-z)H_2O \rightarrow xCO_2+vNH_3+(4x+y-2z-3v)H) \times (4x-y+3v+2z)$$

$$8xC_{x}H_{y}O_{z}N_{v}+2x(4x-y-2z+3v)H_{2}O \rightarrow x(4x+y-2z-3v)CH_{4}+x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y-2z+3v)H_{2}O \rightarrow x(4x+y-2z-3v)CH_{4}+x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+vNH_{3}+2x(4x-y+2z+3v)CO_{2}+2x(4x-y+2v)CO_{2}+2x(4x-y+2v)CO$$

$$C_xH_yO_zN_v + \frac{4x - y - 2z + 3v}{4}H_2O \longrightarrow \frac{4x + y - 2z - 3v}{8}CH_4 + \frac{4x - y + 2z + 3v}{8}CO_2 + vNH_3$$

Step 3. Identify the stoichiometric coefficients of nH₂O, nCH₄, and nCO₂

By using the atomic coefficients (AC) of the chemical formula, the stochiometric coefficients (SC) can be represented as follows: For [N-product] = $NH_3(ON_N = -3)$

$$nCH_4 = \frac{4x+y-2z-3v}{8}$$
$$nCO_2 = \frac{4x-y+2z+3v}{8}$$
$$nH_2O = \frac{4x-y-2z+3v}{4}$$

Step 4. Count the ON_C

Count ON of non-carbon atoms:

all hydrogen atoms: $ON_H = +1$

all oxygen atoms: $ON_O = -2$

one nitrogen atom: $ON_N = -3$

By using the molecular formula method: $\Sigma ON_i = 0$

$$xON_C + y - 2z - 3v = 0$$

$$xON_{C} = -y + 2z + 3v$$
$$ON_{C} = \frac{-y + 2z + 3v}{x}$$

The ON_C of $C_xH_yO_zN_v$ is equal to $\frac{-y+2z+3v}{x}$.

4.1 Assigning Oxidation Numbers of ON_N and ON_C, and Balancing BEq for nH₂O, nCH₄, and nCO₂

By using the same procedure shown in Example 2, different N-products are assigned by different ON_N . The unbalanced BEq is shown as: $C_xH_yO_zN_v+nH_2O$ H₂O \rightarrow nCH₄ CH₄+nCO₂ CO₂+v[N-product]. Their ON_N, nH₂O, nCH₄, nCO₂, and ON_C are given in Table 2.

Table 2. Stoichiometric coefficients of nH ₂ O, nCH ₄ and nCO ₂ , and oxidation numbers of ON _N , and ON _C in the balanced
BEq of $C_x H_y O_z N_v$

$ON_N of C_x H_y O_z N_v$	nH ₂ O	nCH ₄	nCO ₂	ON _C	[N-product]
-3	$\frac{4x-y-2z+3v}{4}$	$\frac{4x+y-2z-3v}{8}$	$\frac{4x - y + 2z + 3v}{8}$	$\frac{-y+2z+3v}{x}$	NH ₃
-2	$\frac{4x - y - 2z + 2v}{4}$	$\frac{4x+y-2z-2v}{8}$	$\frac{4x - y + 2z + 2v}{8}$	$\frac{-y + 2z + 2v}{x}$	N_2H_4
-1	$\frac{4x - y - 2z + v}{4}$	$\frac{4x+y-2z-v}{8}$	$\frac{4x - y + 2z + v}{8}$	$\frac{-y+2z+v}{x}$	N_2H_2
-1	$\frac{4x-y-2z+5v}{4}$	$\frac{4x+y-2z-v}{8}$	$\frac{4x - y + 2z + v}{8}$	$\frac{-y+2z+v}{x}$	NH ₂ OH
0	$\frac{4x-y-2z}{4}$	$\frac{4x+y-2z}{8}$	$\frac{4x - y + 2z}{8}$	$\frac{-y+2z}{x}$	N_2
+1	$\frac{4x - y - 2z + v}{4}$	$\frac{4x + y - 2z + v}{8}$	$\frac{4x-y+2z-v}{8}$	$\frac{-y+2z-v}{x}$	N_2O
+2	$\frac{4x-y-2z+2v}{4}$	$\frac{4x+y-2z+2v}{8}$	$\frac{4x-y+2z-2v}{8}$	$\frac{-y+2z-2v}{x}$	NO
+3	$\frac{4x-y-2z+3v}{4}$	$\frac{4x+y-2z+3v}{8}$	$\frac{4x-y+2z-3v}{8}$	$\frac{-y+2z-3v}{x}$	HNO ₂
+3	$\frac{4x - y - 2z + v}{4}$	$\frac{4x + y - 2z + 3v}{8}$	$\frac{4x-y+2z-3v}{8}$	$\frac{-y+2z-3v}{x}$	N_2O_3
+4	$\frac{4x-y-2z}{4}$	$\frac{4x+y-2z+4v}{8}$	$\frac{4x-y+2z-4v}{8}$	$\frac{-y+2z-4v}{x}$	NO_2
+5	$\frac{4x - y - 2z + 5v}{4}$	$\frac{4x + y - 2z + 5v}{8}$	$\frac{4x - y + 2z - 5v}{8}$	$\frac{-y + 2z - 5v}{x}$	HNO ₃
+5	$\frac{4x - y - 2z + 7v}{4}$	$\frac{4x + y - 2z + 5v}{8}$	$\frac{4x - y + 2z - 5v}{8}$	$\frac{-y + 2z - 5v}{x}$	N ₂ O ₅

By using the AC, the assigned ON of $ON_H = +1$, $ON_O = -2$, and ON_N , the SC of nCH₄, nCO₂, and ON_C can be represented as follows:

 $C_xH_yO_zN_v+nH_2O \ H_2O {\longrightarrow} nCH_4 \ CH_4+nCO_2 \ CO_2+v[N-product]$

 $nCH_4 = \frac{4x + y - 2z + ON_N v}{8}$

$$nCO_2 = \frac{4x - y + 2z - ON_N v}{8}$$
$$ON_C = \frac{-y + 2z - ON_N v}{x}$$

4.2 Mathematical Relationships among SC, AC, and ON of C_xH_yO_zN_y Molecules

Any ON of non-carbon atoms (ON_H , ON_O , ON_N) and AC of $C_xH_yO_zN_v$ can be determined by its structural formula (Yuen & Lau, 2022a; 2023a).

ON of non-carbon atoms: ON_H, ON_O, ON_N

AC: x for carbon, y for hydrogen, z for oxygen, v for nitrogen

Atom	С	Н	0	N
ON	-	ON _H	ONo	ON_N
AC	х	У	Z	v

The values of nCH₄, nCO₂, and ON_C can be calculated by using ON of ON_H, ON_O, and ON_N, and AC of x, y, z, and v.

By balancing the BEq: $C_xH_yO_zN_v+H_2O\rightarrow CH_4+CO_2+[H-product]+[O-product]+[N-product],$ the general derived mathematical equations of $C_xH_yO_zN_v$ molecules are given as follows:

$$nCH_4 = \frac{4x + ON_H y + ON_O z + ON_N v}{8}$$
$$nCO_2 = \frac{4x - ON_H y - ONO z - ON_N v}{8}$$
$$ON_C = \frac{-ON_H y - ON_O z - ON_N v}{x}$$

The value of ON for hydrogen is either -1 or +1, for oxygen it is either -1 or -2, and for nitrogen it is between the integer range of -3 to +5. By using the above derived general mathematical equations, the balanced BEq of $C_xH_yO_zN_v$ molecule can be found, and is shown in the following example.



Example 3. Given an example of tyrosine,

(a) Identify AC and ON of non-carbon atoms

Atom	С	Н	0	Ν
ON	-	+1	-2	-3
AC	9	11	3	1

(b) Use mathematical equations for calculating nCH₄, nCO₂, and ON_C

nCH ₄	$= \frac{4x + 0N_{\rm H} y + 0N_{\rm O} z + 0N_{\rm N} v}{8}$	$= \frac{4(9)+(1)(11)-(2)(3)+(-3)(1)}{8} = \frac{19}{4}$
nCO ₂	$= \frac{4x - ON_{\rm H} y - ON_{\rm O} z - ON_{\rm N} v}{8}$	$= \frac{4(9)-(1)(11)+(2)(3)-(-3)(1)}{8} = \frac{17}{4}$
ON _C	$= \frac{-ON_{\rm H} y - ON_{\rm O} z - ON_{\rm N} v}{x}$	$= \frac{-(1)(11)+2(3)-(-3)(1)}{9} = -\frac{2}{9}$

(c) Balance BEq by counting nH₂O

C₉H₁₁O₃N+nH₂O H₂O→nCH₄ CH₄+nCO₂ CO₂+NH₃

 $C_9H_{11}O_3N+nH_2OH_2O \rightarrow \frac{19}{4}CH_4 + \frac{17}{4}CO_2+NH_3$

Balance O atom:
$$3 + nH_2O = \frac{17}{2}$$

$$nH_2O = \frac{11}{2}$$

Balanced BEq: $C_9H_{11}O_3N + \frac{11}{2}H_2O \rightarrow \frac{19}{4}CH_4 + \frac{17}{4}CO_2 + NH_3$

5. Mathematical Relationships among nCH4, nCO2, and ONC in CxHyOzXwNvSuPt Molecule

The strategy, which is used for balancing and deducting $C_xH_yO_zN_v$, can be extended to work on organic molecules containing the molecular formula $C_xH_yO_zX_wN_vS_uP_t$ (C, H, O, X, N, S, P stand for carbon, hydrogen, oxygen, halogen, nitrogen, sulfur, and phosphorus element respectively, and x, y, z, w, v, u, t stand for their corresponding atomic coefficients). For $C_xH_yO_zX_wN_vS_uP_t$, all possible ON of non-carbon atoms are shown as: $ON_H = +1$ or -1, $ON_O = -1$ or -2, $ON_X =$ integer between -1 and +7, $ON_N =$ integer between -3 and +5, $ON_S =$ integer between -2 and +6, and $ON_P =$ integer between -3 and +5.

The general unbalanced BEq is shown as:

 $C_xH_yO_zX_wN_vS_uP_t+H_2O \rightarrow CH_4+CO_2+[H-product]+[O-product]+[X-product]+[N-product]+[S-product]+[P-product].$ The ON of non-carbon atoms and AC for calculating nCH₄, nCO₂, and ON_C are shown as follows:

	Atom	С	Н	0	Х	Ν	S	Р
-	ON	-	$ON_{\rm H}$	ONo	ON _X	ON_N	ONs	ON _P
_	AC	Х	У	Z	W	V	u	t

The derived general mathematical equations for CxHyOzXwNvSuPt are shown as follows:

$$nCH_4 = \frac{4x + 0N_H y + 0N_O z + 0N_X w + 0N_N v + 0N_S u + 0N_P t}{8}$$
$$nCO_2 = \frac{4x - 0N_H y - 0N_O z - 0N_X w - 0N_N v - 0N_S u - 0N_P t}{8}$$

$$ON_{C} = \frac{-ON_{H} y - ON_{O} z - ON_{X} w - ON_{N} v - ON_{S} u - ON_{P} t}{x}$$

By using these derived general mathematical equations, the balanced BEqs can be found by given structural formulas in Examples 4 to 7.



Example 4. Given an example of taurine,

(a) Identify	AC and	ON o	of non-	carbon	atoms

Atom	С	Н	0	N	S
ON	-	+1	-2	-3	+4
AC	2	7	3	1	1

(b) Use mathematical equations to calculate nCH_4 , nCO_2 , and ON_C

Unbalanced BEq:	C ₂ H ₇ O ₃ NS+H ₂ O-	\rightarrow CH ₄ +CO ₂ +NH ₃ +SO ₂
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nCH ₄	$= \frac{4x + 0N_{\rm H} y + 0N_{\rm O} z + 0N_{\rm N} v + 0N_{\rm S} u}{8}$	$=\frac{4(2)+(1)(7)+(-2)(3)+(-3)(1)+(+4)(1)}{8}=\frac{5}{4}$
nCO ₂	$= \frac{4x - 0N_{\rm H} y - 0N_{\rm O} z - 0N_{\rm N} v - 0N_{\rm S} u}{8}$	$= \frac{4(2)-(1)(7)-(-2)(3)-(-3)(1)-(+4)(1)}{8} = \frac{3}{4}$
ON _C	$= \frac{-ON_{\rm H} y - ON_{\rm O} z - ON_{\rm N} v - ON_{\rm S} u}{x}$	$= \frac{-(1)(7) - (-2)(3) - (-3)(1) - (+4)(1)}{2} = -1$

(c) Balance BEq by counting nH₂O

C₂H₇O₃NS+nH₂O H₂O $\rightarrow \frac{5}{4}$ CH₄+ $\frac{3}{4}$ CO₂+NH₃+SO₂ Balance O atom: 3 + nH₂O = $\frac{3}{2}$ + 2 nH₂O = $\frac{1}{2}$

Attained balanced BEq: $C_2H_7O_3NS + \frac{1}{2}H_2O \rightarrow \frac{5}{4}CH_4 + \frac{3}{4}CO_2 + NH_3 + SO_2$



Example 5. Balancing the Buswell's equation for ATP, (a) Identify AC and ON of non-carbon atoms

Atom	С	Н	0	Ν	Р
ON	-	+1	-2	-3	+5
AC	10	16	13	5	3

(b) Use mathematical equations to calculate nCH_4 , nCO_2 , and ON_C

Unbalanced BEq: $C_{10}H_{16}O_{13}N_5P_3+H_2O \rightarrow CH_4+CO_2+NH_3+H_3PO_4$

nCH ₄	$= \frac{4x+0N_{\rm H}y+0N_{\rm O}z+0N_{\rm N}v+0N_{\rm P}t}{8}$	$= \frac{4(10)+(1)(16)+(-2)(13)+(-3)(5)+(+5)(3)}{8} = \frac{15}{4}$
nCO ₂	$= \frac{4x - 0N_{\rm H} y - 0N_{\rm O} z - 0N_{\rm N} v - 0N_{\rm P} t}{8}$	$= \frac{4(10) - (1)(16) - (-2)(13) - (-3)(5) - (+5)(3)}{8} = \frac{25}{4}$
ON _C	$= \frac{-ON_{\rm H} y - ON_{\rm O} z - ON_{\rm N} v - ON_{\rm P} t}{x}$	$= \frac{-(1)(16) - (-2)(13) - (-3)(5) - (+5)(3)}{10} = +1$

(c) Balance BEq by counting nH₂O

$$C_{10}H_{16}O_{13}N_5P_3 + nH_2O H_2O \rightarrow \frac{15}{4}CH_4 + \frac{25}{4}CO_2 + 5NH_3 + 3H_3PO_4$$

Balance O atom: $13 + nH_2O = \frac{25}{2} + 12$
 $nH_2O = \frac{23}{2}$

Attained balanced BEq: $C_{10}H_{16}O_{13}N_5P_3 + \frac{23}{2}H_2O \rightarrow \frac{15}{4}CH_4 + \frac{25}{4}CO_2 + 5NH_3 + 3H_3PO_4$



Example 6. Given chlorpyrifos,

, C9H11O3Cl3NSP

(a) Identify AC and ON of non-carbon atoms

Atom	С	Н	0	Cl	Ν	S	Р
ON	-	+1	-2	-1	-3	-2	+5
AC	9	11	3	3	1	1	1

(b) Use mathematical equations to calculate nCH_4 , nCO_2 , and ON_C

Unbalanced BEq: $C_9H_{11}O_3Cl_3NSP+H_2O \rightarrow CH_4+CO_2+HCl+NH_3+H_2S+H_3PO_4$

nCH ₄	$= \frac{4x + 0N_{\rm H} y + 0N_{\rm O} z + 0N_{\rm X} w + 0N_{\rm N} v + 0N_{\rm S} u + 0N_{\rm P} t}{8}$	$= \frac{4(9)+(1)(11)+(-2)(3)+(-1)(3)+(-3)(1)+(-2)(1)+(+5)(1)}{8} = \frac{19}{4}$
nCO ₂	$= \frac{4x - ON_{\rm H} y - ON_{\rm O} z - ON_{\rm X} w - ON_{\rm N} v - ON_{\rm S} u - ON_{\rm P} t}{8}$	$= \frac{4(9)-(1)(11)-(-2)(3)-(-1)(3)-(-3)(1)-(-2)(1)-(+5)(1)}{8} = \frac{17}{4}$
ON _C	$= \frac{-ON_{H} y - ON_{O} z - ON_{X} w - ON_{N} v - ON_{S} u - ON_{P} t}{x}$	$= \frac{-(1)(11)-(-2)(3)-(-1)(3)-(-3)(1)-(-2)(1)-(+5)(1)}{9} = -\frac{2}{9}$

(c) Balance BEq by counting nH₂O

$$C_9H_{11}O_3Cl_3NSP + nH_2O \xrightarrow{19}{4}CH_4 + \frac{17}{4}CO_2 + 3HCl + NH_3 + H_2S + H_3PO_4$$

Balance O atom: $3 + nH_2O = \frac{17}{2} + 4$

$$nH_2O = \frac{19}{2}$$

Attained balanced BEq: $C_9H_{11}O_3Cl_3NSP + \frac{19}{2}H_2O \rightarrow \frac{19}{4}CH_4 + \frac{17}{4}CO_2 + 3HCl + NH_3 + H_2S + H_3PO_4$

Example 7. Given chlorthion,

(a) Identify AC and ON of non-carbon atoms

Atom	С	Н	0	Cl	N	S	Р
ON	-	+1	-2	-1	+3	-2	+5
AC	8	9	5	1	1	1	1

, C₈H₉O₅ClNPS

(b) Use mathematical equations to calculate nCH_4 , nCO_2 , and ON_C

Unbalanced BEq: C₈H₉O₅ClNPS+H₂O→CH₄+CO₂+HCl+HNO₂+H₂S+H₃PO₄

nCH ₄	$= \frac{4x+0N_{H}y+0N_{O}z+0N_{X}w+0N_{N}v+0N_{S}u+0N_{P}t}{8}$	$= \frac{4(8)+(1)(9)+(-2)(5)+(-1)(1)+(+3)(1)+(-2)(1)+(+5)(1)}{8} = \frac{9}{2}$
nCO ₂	$= \frac{4x - 0N_{\rm H} y - 0N_{\rm O} z - 0N_{\rm X} w - 0N_{\rm N} v - 0N_{\rm S} u - 0N_{\rm P} t}{8}$	$=\frac{4(8)-(1)(9)-(-2)(5)-(-1)(1)-(+3)(1)-(-2)(1)-(+5)(1)}{8}=\frac{7}{2}$
ON _C	$=\frac{-0N_{H}y-0N_{O}z-0N_{X}w-0N_{N}v-0N_{S}u-0N_{P}t}{x}$	$= \frac{-(1)(9)-(-2)(5)-(-1)(1)-(+3)(1)-(-2)(1)-(+5)(1)}{8} = -\frac{1}{2}$

(c) Balance BEq by counting nH₂O

C₈H₉O₅ClNPS+nH₂O H₂O
$$\rightarrow \frac{9}{2}$$
CH₄+ $\frac{7}{2}$ CO₂+HCl+HNO₂+H₂S+H₃PO₄
Balance O atom: 5 + nH₂O = 7 + 2 + 4
nH₂O = 8

Attained balanced BEq: $C_8H_9O_5CINPS+8H_2O \rightarrow \frac{9}{2}CH_4+\frac{7}{2}CO_2+HCl+HNO_2+H_2S+H_3PO_4$

6. Mathematical Relationship between ONc and nCH4

Based on the following mathematical equations,

$$x = n_{C} = nCH_{4} + nCO_{2}$$

$$ON_{C} = \frac{-ON_{H} y - ON_{O} z - ON_{X} w - ON_{N} v - ON_{S} u - ON_{P} t}{x}$$

$$nCH_{4} = \frac{4x + ON_{H} y + ON_{O} z + ON_{X} w + ON_{N} v + ON_{S} u + ON_{P} t}{8}$$

$$nCO_{2} = \frac{4x - ON_{H} y - ON_{O} z - ON_{X} w - ON_{N} v - ON_{S} u - ON_{P} t}{8}$$

new mathematical equations can be derived as follows:

$$\therefore \text{ x ON}_{C} = -\text{ ON}_{H} \text{ y} - \text{ ON}_{O} \text{ z} - \text{ ON}_{X} \text{ w} - \text{ ON}_{N} \text{ v} - \text{ ON}_{S} \text{ u} - \text{ ON}_{P} \text{ t}$$
$$\therefore \text{ nCH}_{4} = \frac{x(4-0N_{C})}{8} \text{ and } \text{ nCO}_{2} = \frac{x(4+0N_{C})}{8}$$

Consequently, the important parameters of BEq, which include Buswell's ratio $\left(\frac{nCH_4}{nCO_2}\right)$, biogas ratio $\left(\frac{nCH_4}{nCH_4+nCO_2}\right)$, methane

content percentage $\left(\frac{nCH_4}{nCH_4+nCO_2} \times 100\%\right)$, and TBMP $\left(\frac{x(4-ON_c)(22400)}{8\mu}\right)$ can be determined by using the sole ON_C, or ON_C to complement use of d/a w. These means the use the use the sole of the s

to complement x and/or μ . These parameters and their mathematical equations are summarized in Table 3.

Table 3. Mathemati	al equations	for parameters	of BEq and ON _C
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Parameter of BEq	Mathematical equation	Mathematical equation				
nCH ₄	$= \frac{4x+0N_{\rm H} y+0N_{\rm O} z+0N_{\rm X} w+0N_{\rm N} v+0N_{\rm S} u+0N_{\rm P} t}{8}$	$=\frac{\mathrm{x}(4-\mathrm{ON}_{\mathrm{c}})}{8}$				
nCO ₂	$= \frac{4x - 0N_{\rm H} y - 0N_{\rm O} z - 0N_{\rm X} w - 0N_{\rm N} v - 0N_{\rm S} u - 0N_{\rm P} t}{8}$	$=\frac{\mathrm{x}(4+\mathrm{ON}_{\mathrm{c}})}{8}$				
Buswell's ratio	$=\frac{nCH_4}{nCO_2}$	$=\frac{(4-ON_c)}{(4+ON_c)}$				
Biogas* ratio	$= \frac{nCH_4}{nCH_4 + nCO_2}$	$=\frac{(4-ON_c)}{8}$				
Methane content percentage $(nCH_4\%)$	$= \frac{nCH_4}{nCH_4 + nCO_2} \times 100\%$	$=\frac{(4-\mathrm{ON}_{\mathrm{c}})}{8}\times100\%$				
TBMP (at STP, mL/g)	$=\frac{22400(nCH_4)}{\mu}$	$=\frac{x(4-ON_{c})(22400)}{8\mu}$				

*Biogas is defined as the sum of quantitative amounts of biomethane and carbon dioxide (nbiogas = $nCH_4 + nCO_2$).

When ON_C for any given molecule is determined, the parameters of BEq can be counted. According to the molecules in Examples 3 – 7, all the resulting values of parameters of BEq are exhibited in Table 4.

Molecule	ON _C	х	nCH ₄	nCO ₂	Buswell's ratio	Biogas ratio	nCH ₄ %
			$=\frac{\mathrm{x}(4-\mathrm{ON}_{\mathrm{c}})}{8}$	$=\frac{\mathrm{x}(4+\mathrm{ON}_{\mathrm{c}})}{8}$	$=\frac{(4-\mathrm{ON}_{\mathrm{c}})}{(4+\mathrm{ON}_{\mathrm{c}})}$	$=\frac{(4-ON_c)}{8}$	$=\frac{(4-0N_c)}{8} \times 100\%$
HO HO HO HO HO HO HO HO H	$-\frac{2}{9}$	9	<u>19</u> 4	$\frac{17}{4}$	$\frac{19}{17} = 1.12$	$\frac{19}{36} = 0.53$	52.78%
О, ОН H ₂ N (), ОН	-1	2	<u>5</u> 4	$\frac{3}{4}$	$\frac{5}{3} = 1.67$	$\frac{5}{8} = 0.63$	62.50%
$C_2H_7O_3NS$							
HO-P-O-P-O-P-O-N-N-N-N-N-N-N-N-N-N-N-N-N-	+1	10	$\frac{15}{4}$	25 4	$\frac{3}{5} = 0.60$	$\frac{3}{8} = 0.38$	37.50%
$C_{10}H_{16}O_{13}N_5P_3$							
$CI + CI + CI + O - CH_3$ $CI + N + O + O - CH_3$ CH_3	- 2 9	9	$\frac{19}{4}$	$\frac{17}{4}$	$\frac{19}{17} = 1.12$	$\frac{19}{36} = 0.53$	52.78%
C ₉ H ₁₁ O ₃ Cl ₃ NSP							
$\begin{array}{c} S \\ H_3 CO - P \\ O CH_3 \end{array}, \\ NO_2 \\ CI \\ O CH_3 \end{array},$	$-\frac{1}{2}$	8	<u>9</u> 2	<u>7</u> 2	$\frac{9}{7} = 1.29$	$\frac{9}{16} = 0.56$	56.25%
C ₈ H ₉ O ₅ CINPS							

Table 4. ON_C for determination of $nCH_4, nCO_2,$ and parameters of BEq

With reference to the results in Table 4, Buswell's ratio, biogas ratio, and methane content percentage are determined by the assigned ON_C of a given molecule. The nCH₄ and nCO₂ can be counted by ON_C and its number of organic carbons (x).

According to the given molecules in Examples 3 - 7, all resulting values are summarized in Table 5. The TBMP can be calculated by ON_C, x, and molecular mass (μ) for any given organic molecule.

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Molecule	ON _C	х	Molecular mass (µ) (g/mol)	$TBMP = \frac{x(4-0N_c)(22400)}{8\mu} \ (mL/g)$
HO NH ₂ OH, C ₉ H ₁₁ O ₃ N	$-\frac{2}{9}$	9	181.19	587.23
H_2N O $C_2H_7O_3NS$ O $C_2H_7O_3NS$	-1	2	125.15	223.73
$\overset{\circ}{\underset{OH}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}}{\overset{\circ}}{\overset{\circ}}{\overset$	+1	10	240.97	348.59
CI CI CI CI CI CH_3 CH_3 $CH_1 O_3 CI_3 NSP$	$-\frac{2}{9}$	9	350.59	303.49
$H_{3}CO-\overset{NO_{2}}{\overset{NO_{2}}{\overset{OCH_{3}}{\overset{O}}{\overset{OCH_{3}}{\overset{OCH_{3}}{\overset{OCH_{3}}{\overset{O}}{\overset{OCH_{3}}{\overset{OCH_{3}}{\overset{OCH_{3}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{O}}{\overset{{O}}}{\overset{{O}}}{\overset{{O}}}{\overset{{O}}}{{\overset{O}}}{\overset{{O}}}{\overset{{O}}}{\overset{O}}{\overset{{O}}}{\overset{O}}{{\overset{O}}}{{{\overset{O}}}}{{{\overset{O}}}}{{\overset{O}}}{{{\overset{O}}}}{{{\overset{O}}}}{{$	$-\frac{1}{2}$	8	297.65	338.65
With reference to Table 1, three structura	al formulas	of C ₂ H4	H ₂ N HON	$ \begin{array}{c} 0 \\ H \\ H \\ -C \\ -C \\ -N \\ -N \\ -N \\ -N \\ -N \\ -N$

Table 5. Counting TBMP by ON_C , x, and μ

όн , With reference to Table 1, three structural formulas of C₂H₅O₂N are

Their ON_C values are +1, 0, and -2 respectively. All parameters of BEq are calculated and summarized in Table 6. Among these isomers of C₂H₅O₂N, the isomer carrying the highest reduced ON_C can produce the most TBMP.

Table 6. ONc for determination of nCH ₄ , nCO ₂ ,	, and BEq's parameters for C ₂ H ₅ O ₂ N molecules
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$C_2H_5O_2N$	ON_N	ON _C	$nCH_4 =$	$nCO_2 =$	Buswell's	Biogas	$nCH_4 \% =$	TBMP =
Molecule			x(4-0N _c)	x(4+0N _c)	ratio =	ratio =	$\frac{(4-0N_c)}{100\%}$	x(4-ON _c)(22400)
x =2			8	8	$\frac{(4-0N_c)}{(4+0N_c)}$	(4-0N _C)	8	8μ
$\mu=75.07~g/mol$					(4+0N _c)	8		(mL/g)
H ₂ N 0	-3	+1	$\frac{3}{4}$	<u>5</u> 4	<u>3</u> 5	<u>3</u> 8	37.50%	223.79
ОН								
но, Ц	-1	0	1	1	1	$\frac{1}{2}$	50.00%	298.39
H H								
	+3	-2	3	$\frac{1}{2}$	3	3	75.00%	447.58
H-C-C-N+ \ H H O-			2	Z		4		

7. Conclusion

The ON_C is an important redox concept in organic chemistry and biochemistry. In this article, the BEq model is developed by using the H-atom method for understanding the redox nature of organic compounds. ON_C acts as a metric for

quantifying parameters of BEq. The mathematical relationship between ON_c and nCH₄ is established as nCH₄ = $\frac{x(4-ON_c)}{c}$.

Consequently, for any given structural formula of an organic molecule, the parameters of BEq, such as quantity of biomethane, Buswell's ratio, biogas ratio, biomethane content percentage and theoretical biochemical methane potential can be determined.

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Authors contributions

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No additional data is available.

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