An Investigation of the Predictive Speed of the UK VIX for the Downside Risk in European Equity Markets

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Abstract

Using the time-series data of UK volatility index (VIX) and other four European equity indices of France, Italy, Spain, and Portugal, and applying quantile regressions, this study investigates the predictive power and predictive speed of the UK VIX for the future sharp price drops in other four European equity markets. As a result, our empirical examinations derive the following findings. (1) First, we clarify that the increases of the UK VIX have statistically significant predictive power for the downside risk in other four European equity markets. (2) Second, our empirical results reveal that the two to four days before, the changes in the UK VIX can forecast the downside risk in other four European equity markets.

Keywords: European equity markets, downside risk, quantile regression, VIX

1. Introduction

In the fields of business, economics, and finance, downside risk in financial markets is a highly crucial research topic and in fact, recently, many interesting studies regarding this issue have been conducted (e.g., Galsband, 2012; Reboredo and Rivera-Castro, 2014; Min and Kim, 2016; Tsuji, 2017a; Farago and Tédongap, 2018; Bernstein et al., 2018). In a globalizing and tightening international financial markets, how does downside risk in international equity markets spill over? Further, how is the speed of downside risk spillovers in international equity markets? To answer these research questions, by using the time-series data of the UK VIX and other four European equity price indices of France, Italy, Spain, and Portugal, and applying quantile regressions, this study investigates the predictive power and predictive speed of the UK volatility index (VIX) for the future sharp price drops in other European equity markets.

In European equity markets, the UK equity market is particularly important, and the UK VIX used in this study is the volatility index as to the most representative and popular UK equity market index, the FTSE100. Thus, the use of this UK VIX is highly meaningful for conducting beneficial empirical examinations for European equity markets. In addition, the equity markets of France, Italy, Spain, and Portugal are also important in Europe; and all the five countries are included in the Southern and Western Europe. That is, this study focuses on these major important five European equity markets in the Southern and Western Europe.

Furthermore, we stress that this study is highly significant because our study can be expected to reveal the following matters: (1) How does the turmoil of the UK equity market spill over to other European equity markets? (2) Does the increasing fear in the UK equity market predict the downside risk in other European equity markets? The clarifications regarding these matters shall lead to new contributions to existing and future research in the fields of business, economics, and finance; and this is the reason why we conduct this research in this paper. In addition, it is noted that the left-tail downside risk of the price changes in equity markets can be effectively tested by using quantile regressions. More specifically, by applying quantile regressions, we can test the one-to-one linkages between the UK VIX increases and the sharp price drops in other European equity markets more directly. For these reasons, we apply quantile regressions in this study.

As a result, the main findings derived from our investigations are as follows. First, the second and third lags of the changes in the UK VIX predict the downside risk for the French equity market. Next, the second, third, and fourth lags of the changes in the UK VIX predict the downside risk for the Italian equity market. Third, the third and/or fourth lags of the changes in the UK VIX predict the downside risk for the Spanish equity market. Fourth,

the third and/or fourth lags of the changes in the UK VIX predict the downside risk for the Portuguese equity market. The above results derived from our examinations are interesting and quite new; hence this work makes important and new contributions to the existing and future research in business, economics, and finance.

The rest of this paper is as follows. Section 2 reviews recent literature; Section 3 describes our data and variables; Section 4 introduces our quantitative methodology; Section 5 provides our empirical results; and Section 6 provides our conclusions.

2. Recent Literature Review

In this section, we briefly review existing recent literature that studied downside risk of asset prices. We focus on only recent studies in this literature review. First, Hilal et al. (2011) attempted to model the tail dependence between S&P 500 and US VIX futures, and presented some hedging effectiveness using their model. Further, using the data of emerging economies of Brazil, Chile, Colombia, India, Mexico, Russia, South Africa, and Turkey, and applying copulas, Reboredo et al. (2016) investigated the downside and upside risk spillovers between exchange rates and equity prices. Tsuji (2016) empirically exhibited that, in predicting the US equity market downside risk, US VIX did not outperform the volatility forecasts of S&P 500, which were derived from EGARCH and TGARCH models. Min and Kim (2016) investigated whether the time-variations of momentum strategies' profitability have a relationship with the variations in macroeconomic conditions, and they found that momentum strategies exposed investors to greater downside risk in financial markets.

Sukcharoen and Leatham (2017) empirically examined the effectiveness of hedging downside risk of oil refineries by applying vine copulas. The empirical results of this study suggested that the D-vine copula model was a safe and good choice in managing the downside risk as to oil refineries. Tsuji (2017b) investigated the forecast power of the previous day's US VIX for large price drops in the Tokyo Stock Price Index (TOPIX) in Japan, and this study exhibited that the previous day's US VIX had statistically significant forecast power for large price declines in the TOPIX in Japan. Further, Xiaoye (2018) investigated the downside risk spillovers from China to Asian equity markets by applying a CoVaR-copula approach.

Moreover, Farago and T ádongap (2018) researched by focusing on downside risk in asset pricing framework, and they found three priced disappointment-related factors in the US; namely, (*i*) a downstate factor, (*ii*) a market downside factor, and (*iii*) a volatility downside factor. Tsuji (2018a) analyzed return transmission and volatility spillovers between oil futures and international oil equities, and interpreted the clarified asymmetric spillovers between them were related to downside risk in the international oil and equity markets. Finally, using the data of 20 global currencies against the US dollar, Chuli áet al. (2018) investigated the currency downside risk, liquidity, and financial stability by estimating volatility- and quantile-based spillovers across the 20 currencies against the US dollar.

As the above recent literature review shows, we understand that downside risk is one of the most significant and appealing research topics in the fields of business, economics, and finance. Hence in this study, focusing on downside risk in the Southern and Western European equity markets, we quantitatively examine whether and how UK VIX predict downside risk in other European equity markets of France, Italy, Spain, and Portugal.

3. Data and Variables

This section explains our data and variables. In this study, DUKVIX denotes the first difference series of the VIX as to FTSE100 in the UK; DFRA denotes the first difference series of the French equity price index, CAC40; DITA denotes the first difference series of the Italian equity price index, FTSE MIB; DSPN denotes the first difference series of the Spanish equity price index, IBEX35; and DPORT denotes the first difference series of the Portuguese equity price index, PSI ALL-SHARE.

All price data are from Thomson Reuters, and the sample period is from May 14, 2004 to August 2, 2018 for price series, and the period from May 17, 2004 to August 2, 2018 is for all the first price difference (i.e., price change) series. Figure 1 displays the daily time-series evolution of all the above four equity prices with the UK VIX, and Figure 2 shows all the above first difference series of the four equity price indices with the first difference series of the UK VIX.

In this study, as above, we use not return series but price change series because price changes are more important than return series in the context of risk management of asset prices as they are used in the Value-at-Risk (VaR) computations. As in VaR calculations, we focus on the left-tail quantiles of asset price changes in this study. Thus, our use of the quantile regressions applied to price change data in this paper is suitable from the viewpoint of the downside risk evaluation, which is the focus of this study.

Table 1 shows the descriptive statistics for the first difference series of the four European equity price indices

and the first difference series of the UK VIX. This table suggests that the skewness value of DUKVIX is positive, while the skewness values of DFRA, DITA, DSPN, and DPORT are all negative. Further, Table 1 also shows that the kurtosis of DUKVIX is especially high, and the kurtosis values of DFRA, DITA, DSPN, and DPORT are also higher than that of normal distributions. In addition, Figure 1 indicates that when the UK VIX largely increases, the equity prices of France, Italy, Spain, and Portugal sharply drop. Further, Figure 2 shows that when the volatility of the UK VIX changes largely increases, the volatilities of the changes in equity prices of France, Italy, Spain, and Portugal also sharply increases.

4. Methodology

This section documents our investigating methodology. In this study, we employ the following quantile regression model (1):

$$Q_t = \xi_0 + \xi_1 DUKVIX_{t-k} + v_t. \tag{1}$$

In the above model (1), Q_t denotes the specified quantile of the distribution of DFRA, DITA, DSPN, or DPORT. In our analyses, we use 0.01 quantile, 0.015 quantile, and 0.02 quantile in order to capture the large downside risk of the four European equity indices. Further, DUKVIX_{*t*-*k*} denotes the *k*th lag variable of the daily first difference series of the VIX as to FTSE100, and we use *k*=1,...,5.

Hence, using model (1), we can test the predictive power and predictive speed of the UK VIX changes as to the 1% left-tail, 1.5% left-tail, and 2% left-tail downside risk of the distributions for price changes in other European equity indices of France, Italy, Spain, and Portugal. As we noted, the quantile regressions are suitable for examining the left-tail downside risk of equity price changes more directly and effectively.

5. Empirical Results

This section documents our main results. As noted, we derive our results by using price change series because price changes are more important than return series in the context of asset price downside risk evaluations. In fact, in VaR calculations, asset price changes are often used. Hence, we focus on the left-tail quantiles of equity price changes in this study. Table 2 exhibits the estimation results of our quantile regression model (1), and this table shows the predictive power and predictive speed of the UK VIX for the large price declines in other European equity markets. First, Panel A of Table 2 indicates that the second and third lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the French equity market. This means that the turmoil of the UK equity market predicts the 1%, 1.5%, and 2% left-tail downside risk for the French equity market in two or three days.

Table 1. Descriptive statistics of price changes in European equity indices and UK VIX changes

	DUKVIX	DFRA	DITA	
Mean	-0.0014	0.5009 -1.5837		
Median	-0.0200	0.8100 6.2800		
Maximum	23.3000	367.0100 2333.5900		
Minimum	-14.1400	-368.7700 -2242.3600		
Standard deviation	1.5843	53.3033 322.7287		
Skewness	1.1548	-0.1966 -0.2711		
Kurtosis	28.2022	8.0400 7.8981		
	D	SPN	DPORT	
Mean	0.	5173	-0.0138	
Median	3.8000		0.3300	
Maximum	1305.8000		133.2500	
Minimum	-109	97.6000	-161.5100	
Standard deviation	139	9.8906	17.2408	
Skewness	-0	.1674	-0.5287	
Kurtosis	10.5293		12.2198	

Note. DUKVIX denotes the first difference series of the VIX as to FTSE100; DFRA denotes the first price difference series of CAC40; DITA denotes those of FTSE MIB; DSPN denotes those of IBEX35; and DPORT denotes those of PSI ALL-SHARE. All observations for the five time-series are 3,709.

Panel A. France







Panel D. Portugal



Figure 1. Dynamic time-series price evolution of European countries' equity indices with the VIX in the UK: From May 14, 2004 to August 2, 2018







Figure 2. Dynamic time-series evolution of price changes in European countries' equity indices with UK VIX changes: From May 17, 2004 to August 2, 2018



Panel A. France								
	0.01 quantile		0.015 quantile		0.02 quantile			
	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value		
Constant	-146.5005***	0.0000	-131.1324***	0.0000	-120.7339***	0.0000		
DUKVIX(-1)	3.3113	0.3804	0.2997	0.8528	1.3997	0.1880		
DUKVIX(-2)	-3.3968	0.1440	-2.7142**	0.0107	-2.1391***	0.0037		
DUKVIX(-3)	-3.7722**	0.0398	-5.3453***	0.0016	-5.5420***	0.0000		
DUKVIX(-4)	-1.4074	0.7506	-2.1114	0.3552	-1.6458	0.2180		
DUKVIX(-5)	2.3319	0.4604	2.8743	0.1176	1.5837	0.1441		
Panel B. Italy								
	0.01 qua	intile	0.015 quantile		0.02 quantile			
	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value		
Constant	-916.9733***	0.0000	-791.8599***	0.0000	-747.5550***	0.0000		
DUKVIX(-1)	29.6605***	0.0029	9.2034	0.3299	2.3928	0.6868		
DUKVIX(-2)	-33.8504***	0.0011	-11.8987	0.5985	-19.6509	0.1271		
DUKVIX(-3)	-13.4432	0.1668	-27.8245***	0.0000	-29.4966***	0.0100		
DUKVIX(-4)	-17.1099 * * *	0.0059	-27.1027***	0.0010	-32.2428***	0.0000		
DUKVIX(-5)	31.6342***	0.0000	16.2099*	0.0594	12.8975	0.1079		
Panel C. Spain								
	0.01 qua	0.01 quantile		0.015 quantile		0.02 quantile		
	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value		
Constant	-384.0946***	0.0000	-339.6576***	0.0000	-315.0487***	0.0000		
DUKVIX(-1)	4.9010**	0.0304	0.8935	0.7561	-0.2470	0.9110		
DUKVIX(-2)	-3.9899	0.5365	1.0542	0.8192	-4.7069	0.1889		
DUKVIX(-3)	-6.1510***	0.0031	-7.9787***	0.0000	-10.4921***	0.0000		
DUKVIX(-4)	-2.4303	0.5536	-2.3766	0.3492	-5.0431***	0.0085		
DUKVIX(-5)	2.7151	0.2348	0.2751	0.9227	1.2125	0.6315		
Panel D. Portugal								
	0.01 quantile		0.015 quantile		0.02 quantile			
	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value	Coefficient	<i>p</i> -value		
Constant	-50.7222***	0.0000	-45.4806***	0.0000	-40.6466***	0.0000		
DUKVIX(-1)	0.6325	0.1418	0.0985	0.8830	-0.1826	0.8051		
DUKVIX(-2)	0.3387	0.7326	-0.4838	0.4559	-0.9485	0.2670		
DUKVIX(-3)	-0.2936	0.7271	-1.2586*	0.0991	-1.8222	0.1122		
DUKVIX(-4)	-0.7613***	0.0067	-0.9961*	0.0939	-0.4897	0.5126		
DUKVIX(-5)	0.1938	0.8733	0.3082	0.8513	0.8762	0.5076		

Table 2. Predictive speed of the UK VIX for the large price declines in equity indices of other European countries: Results of quantile regressions

Note. In Panel A, the dependent variable is DFRA; in Panel B, the dependent variable is DITA; in Panel C, that is DSPN; and in Panel D, that is DPORT. In this table, DUKVIX(-k) denotes the *k*th lag variable of the daily first difference series of the VIX as to FTSE100. ***, **, and * means the statistical significance at the 1%, 5%, and 10% levels, respectively.

Second, Panel B of Table 2 suggests that the second, third, and fourth lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the Italian equity market. This indicates that the turmoil of the UK equity market predicts the 1%, 1.5%, and 2% left-tail downside risk for the Italian equity market, and the increasing fear in the UK equity market spills over to the Italian equity market in two to four days. Third, Panel C of Table 2 indicates that the third and/or fourth lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the Spanish equity market. This means that the turmoil of the UK equity market predicts the 1%, 1.5%, and 2% left-tail downside risk for the Spanish equity market, and the increasing fear in the UK equity market spills over to the Spanish equity market in three or four days. Fourth, Panel D of Table 2 suggests that the third and/or fourth lags of the changes in the UK VIX predict the 0.01 and 0.015 quantile downside risk for the Portuguese equity market. This suggests that the turmoil of the UK equity market predicts the 1% and 1.5% left-tail downside risk for the Portuguese equity market, and the increasing fear in the UK equity market spills over to the Portuguese equity market, and the increasing fear in the UK equity market predicts the 1% and 1.5% left-tail downside risk for the Portuguese equity market in three or four days.

In addition, Panels A to D of Table 2 indicate that in general, the first lags of the changes in the UK VIX do not predict the 0.01, 0.015, or 0.02 quantile downside risk for other four European equity markets, and the coefficients of the first lags of the UK VIX changes take positive signs weirdly in general. We interpret that this is because the UK VIX includes the information as to downside risk in other European equity markets very quickly, and as a result, the first lags of the UK VIX changes show little linkages with the downside risk for other four European equity markets.

However, as above, interestingly, all our empirical results from effective quantile regressions show that the two to four days before, the changes in the UK VIX can forecast the downside risk for other European equity markets investigated in this study. We note that looking at the statistically significant lags of the UK VIX changes in Panels A to D in Table 2, it is also understood that after the increases of the UK VIX, the equity prices in France firstly drop, and then those in Italy decline. After that, the equity prices in Spain decline, and then those in Portugal drop. Therefore, our quantile regression analyses also reveal that the predictive and spillover speed of the UK VIX changes as to the downside risk in other four European equity markets slightly differ with countries. Overall, as we demonstrated above, the UK VIX have statistically significant forecast power for sharp price drops in other European equity markets of France, Italy, Spain, and Portugal.

6. Summary and Conclusions

In the fields of business, economics, and finance, downside risk in financial markets is highly crucial, and recently, on the back of globalizing and tightening financial markets, the research of downside risk becomes more important. More concretely, how does the downside risk in international equity markets spill over? Further, how is the speed of downside risk spillovers in international equity markets? In order to answer these research questions, using the time-series data of the UK VIX and other four European equity indices, and applying quantile regressions, this study has investigated the predictive power and predictive speed of the UK VIX for the future sharp price drops in the equity markets of France, Italy, Spain, and Portugal. Our empirical examinations derived the following findings.

First, (1) the second and third lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the French equity market. Next, (2) the second, third, and fourth lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the Italian equity market. Third, (3) the third and/or fourth lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the Italian equity market. Third, (3) the third and/or fourth lags of the changes in the UK VIX predict the 0.01, 0.015, and 0.02 quantile downside risk for the Spanish equity market. Fourth, (4) the third and/or fourth lags of the changes in the UK VIX predict the 0.01 and 0.015 quantile downside risk for the Portuguese equity market. Finally, (5) as to the predictive and spillover speed of downside risk, after the increases of the UK VIX, the equity prices in France firstly drop, and then those in Italy decline. After that, the equity prices in Spain decline, and then those in Portugal drop. Therefore, our quantile regression analyses also revealed that the predictive and spillover speed of the UK VIX as to downside risk in other four European equity markets slightly differ with countries.

In addition, our empirical results can be interpreted as follows. First, (1) the downside risk in European equity markets comoves. This interpretation is quite interesting and important, and we also consider that such downside risk comovements may relate to the psychology of equity markets because VIX is known as a fear gauge. Second, (2) we understand that there are downside risk spillovers between the UK and other European equity markets, and this can be interpreted that the spillovers of asset price evolutions between international equity markets shall be asymmetric (This context of spillovers is analyzed by Tsuji (2018a, 2018b), for example.). These two viewpoints are highly important and useful for further considerations of the issues related to international financial market linkages and interactions. This kind of further work is one of our future tasks.

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