Pullout Capacity of a Vertical Plate Anchor Embedded in Cohesion-less Soil

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Abstract

In this paper, the ultimate pullout capacity of a shallow laid vertical plate strip anchor in cohesion-less soil is analyzed with the consideration of active and passive states of limit equilibrium in the soil. Kötter's equation is used to compute the active and passive thrusts, which are subsequently used in the analysis in which, all the equation of equilibrium are properly interpreted. The unique failure surfaces under active and passive states of limit equilibrium are identified on the basis of force equilibrium conditions. One distinguishing feature of the proposed method is its ability to compute the point of application of active/passive thrust using moment equilibrium. Another distinguishing feature is the prediction of distribution of soil reactions on the failure surface. Comparison of the results of the proposed method with the available experimental results vis-a-vis other theoretical methods shows that, up-to embedment ratio of 3.0, the proposed method is capable of making reasonably good predictions.

Keywords: Vertical plate anchors, Cohesion-less soil, Pullout capacity, Kötter's (1903) equation

1. Introduction

Generally, earth anchors are used to transmit tensile forces from a structure to the soil and to generate passive support to bulkheads, sheet piles and retaining walls (Figures 1 and 2). Their pullout capacity is obtained through the shear strength and dead weight of the surrounding soil. Plate anchors may be made of a steel plate and precast or cast in situ concrete slabs. These anchors can be installed by excavating the ground to the required depth followed by back filling and compacting with a good quality soil.

In the analysis of estimation of ultimate pullout capacity, the vertical plate anchors can be divided in shallow and deep categories. In case of shallow anchors, the embedment ratio is such that, soil above the anchor top can be replaced as a surcharge without shear strength; whereas in case of deep anchors, the embedment ratio is such that, failure surface does not reach the ground surface at limit equilibrium (Das, 1990).

The proposed analysis is confined to shallow laid plate anchors in cohesion-less soil.

2. Previous Experimental Investigations

A number of investigations are reported by several researches to evaluate the ultimate pullout capacity of shallow laid vertical plate anchors.

Ovesen and Stromann (1964, 1972) used the failure mechanism proposed by Hansen (1953) to estimate the earth pressures for the case of a continuous shallow plate anchor flushing with the cohesion-less ground surface, termed as the basic case (H/h = 1), where h is the height of the plate anchor with embedment depth, H (Figure 3). The failure mechanism consists of Rankine (1857) and logarithmic spiral zones (Prandtl-zone) as shown in Figure 3. Based on the above failure mechanism, the ultimate pullout capacity, $T_{u(B)}$ per unit length of a strip anchor was estimated by Ovesen and Stromann (1964, 1972) by the following expression using horizontal force equilibrium.

$$T_{\rm u(B)} = P_{\rm pH} - P_{\rm aH} \tag{1}$$

In the above expression, P_{pH} and P_{aH} are the horizontal components of the passive and active thrusts, which can be estimated using the earth pressure coefficients reported by Caquot and Kerisel (1948).

The expression given in Equation 1 was further modified to estimate the ultimate pullout capacity, T_u per unit width of a strip anchor of width B in cohesion-less soil as,

$$T_{u} = R_{0v} T_{u(B)} \tag{2}$$

The parameter, R_{0v} in the above equation is given by Dickin and Leung (1985) based on the experimental evidence.

$$R_{0v} = \frac{C_{0v} + 1}{C_{0v} + H/h} \tag{3}$$

Where, $C_{0v} = 19$ for dense sand and 14 for loose sand.

Neely *et al.* (1973) performed laboratory tests on plate anchors in dry sand and ultimate resistances of these plates were examined using both limit analysis and the method of stress characteristics. Results of tests on rigid anchor plates in terms of M $_{q}$, a dimensionless force coefficient, were expressed as $M_{\gamma q} = T_{\rm u} / \gamma B {\rm h}^2$, where γ is unit weight of soil and B is width of plate anchor.

Das and Seeley (1975) conducted several laboratory model tests to determine the ultimate pullout resistance of shallow vertical anchors and suggested a simple semi-empirical relation for the pullout resistance in a non-dimensional form as the ratio of $T_u/\gamma Bh^2$ for square and rectangular anchors. Ultimate pull out capacity for a single anchor of width B was expressed by the following semi-empirical relation.

$$T_{\nu} = (4.59 \times 10^{-5}) \text{S}\phi^{3.22} (H/\text{h})^{n} \gamma B \text{h}^{2}$$
 (4)

Where, S is the shape factor which is a function of H/h and ϕ is angle of soil friction in degrees. The value of n varies linearly from 1.8, for B/h = 1 to about 1.68 for B/h = 5.

The capacity of deeper vertical anchors in medium dense sand was investigated by Akinmusuru (1978) for square, circular and rectangular anchors. On the basis of experimental findings, the variation of $T_u/\gamma h^3$, a non-dimensional anchor load at ultimate failure with λ , a non-dimensional embedment coefficient ($\lambda = H/h$) was presented for an anchor length of 10h in the form of a chart. Akinmusuru (1978) clearly defined the critical embedment depth as the one corresponding to $\lambda = 6.5$.

Dickin and Leung (1983) conducted both centrifuge and conventional chamber tests and reported very thorough investigations on the behaviour of vertical square and rectangular anchors in dense sand. The variations of breakout factor $N_{\gamma q}$, and the force coefficient $M_{\gamma q}$ with embedment ratio were separately reported in the form of a chart with $N_{\gamma q} = T_u/\gamma BhH$ and $M_{\gamma q} = T_u/\gamma Bh^2$. The results obtained by them suggested potentially serious overpredictions of pullout resistance and underestimations of the failure displacements. Such errors arose due to the characteristic stress- dependent behaviour of dense soils.

Hoshiya & Mandal (1984) investigated the capacity of square and rectangular anchors in loose sand. The size of box (40 cm x 30 cm x 40 cm deep) used for testing was very small, which facilitated the testing of 2.54 cm wide and 15.24 cm long plates. This was likely to introduce edge effects into the results. They concluded that, anchor break-out factor, $N_{\gamma q}$ increased with embedment depth up to a certain embedment ratio before reaching a constant value thereafter.

Naser (2006) carried out theoretical as well as experimental studies on the ultimate pullout capacity of an anchor block of concrete embedded in sand and observed that, anchor thickness contributed to the pullout capacity through base friction forces. This effect was not significant as compared to the passive resistance. Uplifting and tilting of the block at failure was also observed.

3. Previous Theoretical Investigations

Terzaghi (1943) evaluated the resistance of vertical strip anchor plates assuming Rankine (1857) states of passive and active pressures. This approach was adopted in the British civil engineering code of practice. The net resistance T_{u} , per unit length of a vertical strip anchor was given as $(P_p - P_a)$, where P_p and P_a are the passive and active thrusts (kN/m) acting on the anchor plate.

Teng (1962) estimated holding capacity of a vertical (strip) plate anchor embedded in granular soil at a relatively shallow depth (h/H \leq 1/3 to 1/2), based on Rankine's (1857) theory of lateral earth pressures. He obtained the expression for ultimate holding capacity as,

$$T_u = P_p - P_a \tag{5}$$

Where, P_p and P_a are the passive and active pressure thrusts (kN/m) acting on the anchor plate.

In case of shallow strip anchors, Meyerhof (1968, 1973) used the passive and active coefficients of earth pressure proposed by Caqout and Kerisel (1948) and Sokolovskii (1965) and proposed the following simple relationship for ultimate holding capacity per unit length of a vertical plate anchor in cohesion-less soil.

$$T_{u} = 1/2\gamma H^{2} K_{b} \tag{6}$$

Where, K_b is the pullout coefficient that can be obtained from a graph using soil friction angle.

Using limit analysis and plasticity solutions, Neely et al. (1973) determined the theoretical resistance of continuous (strip) vertical plate anchors in cohesion-less soils for two cases. In the first case, failure surface was assumed to be consisting of a logarithmic spirals and its tangent inclined at $(45^{\circ}-\phi/2)$ to the horizontal as shown in Figure 4. Soil above top of the anchor was considered to act as a simple surcharge, $q \{ \gamma(H-h) \}$ and therefore, the method was termed as the surcharge method.

Shearing resistance of the soil above the anchor top is ignored when H/h is small; therefore the method was subsequently modified by considering shear strength above the top of anchor plate when H/h is considerable and was defined as the Equivalent Free Surface method. The assumed failure surface in soil (Figure 5) is an arc of logarithmic spiral with pole at top of the wall. OB is a straight line which is an equivalent free surface. The shearing resistance of upper layers of soil was included in the calculation by making use of the equivalent free surface concept proposed by Meyerhof (1951) in connection with the bearing capacity of shallow foundations. The normal and shear stresses along OB (p₀ and s₀, respectively) were calculated using Rankine (1857) active stresses on the vertical surface, OA above the top of the anchor plate as shown in Figure 5.

The above analysis is based on the method of stress characteristics and represents a more refined analytical and numerical attempt to predict the ultimate capacity of the vertical plate anchors but it ignores the active earth pressure distribution behind the anchor plate and the kinematic behaviour of the material.

Rowe and Davis (1982b) reported a two-dimensional finite element analysis incorporating an elasto-plastic soil model. For a continuous vertical plate anchor assumed to be thin and perfectly rigid, the resistance is as given by the following expression.

$$M_{\gamma q} = F_{\gamma} R_{\psi} R_{R} R_{K} \tag{7}$$

Where, F_{ν} is the capacity factor of a smooth anchor resting on soil which deforms plastically at a constant volume ($\psi = 0^{\circ}$), with coefficient of earth pressure at rest, $K_0 = 1$ and R_{ψ} , R_R and R_K are correction factors for the effects of sand dilatancy, anchor plate roughness and initial stress state respectively. The theoretical data was presented in the form of design charts.

A comparative study of the force coefficient, Myg as obtained from experimental investigations and theoretical methods proposed by Ovesen and Stromann (1972), Neely et al., (1973) was carried out by Dickin and Leung (1983). Significant disparity was observed in the results because they were based on two-dimensional analysis and their application to single anchors required a suitable shape factor. Dickin and Leung (1985) observed that, effect of anchor shape on dimensionless coefficients was due to side shear resistance. They observed failure planes radiating outward involving a soil mass wider than a single anchor itself in the failed body. A dimensionless factor, Rov to account for the influence of anchor geometry on the ultimate resistance was introduced by them as stated previously.

Finite element method is also used by various researchers such as Vemeer and Sutjiadi (1985), Tagaya et al. (1983, 1988), Dickin and King (1997) and Sakai and Tanaka (1998). Unfortunately, only limited results are available from these studies.

Upper and lower bound limit analyses are also reported by Murray and Geddes (1987, 1989), Basudhar and Singh (1994) and Smith (1998) to estimate the capacity of vertical strip anchor plates. Basudhar and Singh (1994) obtained estimates with a generalized lower bound procedure based on finite element method and non-linear programming similar to that of Sloan (1988a). The solutions proposed by Murray and Geddes (1987, 1989) are based on kinematically admissible failure mechanisms (upper bound).

Merifield *et al.* (2006) presented the results of a rigorous numerical work (linear finite elements coupled with upper and lower bound limit analyses, nonlinear finite elements coupled with lower bound limit analyses and displacement finite elements using Solid Nonlinear Analysis Code (SNAC) - an algorithm developed by Abbo and Sloan, 2000) to estimate the ultimate pullout capacity T_u, for a vertical strip anchor plate in the cohesion-less material. For comparison purposes, numerical and theoretical results of the break-out factor were presented in the form analogous to Terzaghi's (1943) equation of the bearing capacity of shallow foundations.

$$T_{u} = \gamma Hh N_{\gamma} \tag{8}$$

Where, N_{ν} is the anchor break-out factor that can be obtained from a graph using soil friction angle

The failure mode (Figure 6) reported by Merifield *et al.* (2006) for vertical plate anchors indicates that, the soil retained behind the anchor can significantly affect the estimated capacity of shallow anchors. This is particularly the case for loose sands, where the development of a significant active zone behind the anchor is observed. Changing the interface roughness from perfectly rough ($\delta = \phi$) to perfectly smooth ($\delta = 0$) led to a reduction in the anchor capacity by as much as 65%.

Naser (2006) analyzed pullout capacity of an anchor block (Figure 7) using limit equilibrium approach. The ultimate pullout capacity (P_u) of a block anchor was obtained from the equilibrium of forces acting on the block by summing them along the horizontal direction and multiplying the lateral earth pressures (passive and active) by the 3-D corrections factor M, to yield the following equation.

$$P_{\rm u} = M(P_{\rm ph} - P_{\rm ah}) + F_{\rm t} + F_{\rm s} + F_{\rm b} \tag{9}$$

Where, F_t , F_b and F_s are the effective friction forces at the top, bottom and at two sides of the block, N is the normal force, P_{ph} is the effective horizontal passive thrust and P_{ah} is the effective horizontal active thrust (Figure 7). For Coulomb (1776) and log spiral theories, $F_b = 0$ (as N=0). Pullout capacity of block anchor with Rankine's theory (1857), corrected for the 3-D effect with the contribution of friction, showed a close agreement with experimental results.

More recently Kumar and Sahoo (2011) used an upper bound theorem of the limit analysis in combination with finite elements for estimation of horizontal pullout capacity of vertical plate anchors embedded in sand. The results were plotted for various combinations of embedment ratio, internal friction angle, ϕ of sand, and the anchor-soil interface friction angle, δ . It was observed that, the pullout resistance increased with increasing embedment ratio, friction angle of sand and anchor-soil interface friction angle.

4. Proposed Method

In the proposed analysis of the estimation of pullout capacity of a strip anchor in cohesion-less soil, all the three equation of equilibrium are utilized to obtain the required solution. Both passive and active states of equilibrium on the two sides of anchors are considered in the analysis. The active/passive thrusts along with their points of application are evaluated using Kötter's (1903) equation. This equation has been used by other researchers such as Dewaikar and Mohapatro (2003) for the computation of bearing capacity factor, N_{γ} , Deshmukh *et al.* (2010) for the estimation of breakout capacity of horizontal rectangular/square anchors in cohesion-less soils, Rangari *et al.* (2010) for the computation of seismic vertical uplift capacity factor for horizontal strip anchors and Kame, Dewaikar and Choudhury (2010a) for the estimation of active thrust and its point of application on a vertical retaining wall with horizontal cohesion-less backfill.

4.1 Geometry of the problem

In Figure 8 is shown a shallow laid continuous (strip) plate anchor buried vertically. The bottom of plate is at a depth, H below the ground surface and h is the height of plate anchor. In case of shallow laid anchors, the ultimate pullout capacity (T_u) is mainly derived from the passive and active resistances of cohesion-less soil in the front and on the back of the anchor plate respectively. The solution to the problem is proposed using Kötter's (1903) equation coupled with limit equilibrium analysis.

In Figure 9, the failure mechanism adopted in the analysis is shown. In the passive state of equilibrium, the failure surface consists of a log spiral followed by its tangent that meets the ground surface. In the active state of

equilibrium the failure surface is plane as per the Coulomb (1773) mechanism. The anchor plate is shallow laid with embedment ratio, H/h up to 5.

In Figure 10, free body diagram of the strip anchor is shown from which, the following information is generated.

 P_{Poy} = resultant passive thrust per unit length of the plate anchor

 $P_{\text{aq}\gamma}$ = resultant active thrust per unit length of the plate anchor

 δ = interfacial friction angle

 ϕ = angle of soil friction

 h_{pqy} = distance of point of application of passive thrust, P_{pqy} from the anchor base

 $h_{\text{aq}\gamma}$ = distance of point of application of active thrust, $P_{\text{aq}\gamma}$ from the anchor base

 W_p = weight of the anchor plate per unit length

t =thickness of the anchor plate

N = upward soil reaction

The parameters $P_{pq\gamma}$, $P_{aq\gamma}$, $h_{pq\gamma}$ and $h_{aq\gamma}$ are computed using Kötter's (1903) equation for embedment ratio, H/h up to 5.

4.2 Kötter's (1903) equation

In a cohesion-less soil medium with passive and active states of equilibrium under plane strain condition, Kötter's (1903) equation is given as,

$$\frac{\mathrm{d}p}{\mathrm{d}s} + 2p\tan\phi \frac{\mathrm{d}\alpha}{\mathrm{d}s} = \gamma\sin(\alpha + \phi) \text{ for the passive state (Figure 11a)}$$
 (10a)

And

$$\frac{\mathrm{d}p}{\mathrm{d}s} - 2p\tan\phi \frac{\mathrm{d}\alpha}{\mathrm{d}s} = \gamma\sin(\alpha - \phi) \quad \text{for the active state (Figure 11 b)}$$
 (10b)

In the above equations,

dp = differential reactive pressure on the failure surface

ds = differential length of arc of failure surface

 ϕ = angle of soil internal friction

 $d\alpha$ = differential angle and,

 α = inclination of the tangent at the point of interest with the horizontal

For the determination of ultimate pullout capacity using limit equilibrium, the failure mechanism adopted consists of combination of logarithmic spiral and straight lines inclined at 45°-\(\phi/2 \) to the horizontal in case of passive state of equilibrium and a plane failure surface (Coulomb mechanism, 1773) in case of active state of equilibrium. The soil above the level of the top of the anchor plate is assumed to act as simple surcharge, q kN/m. Contributions to the active/passive thrusts due to surcharge and self-weight are estimated separately using Kötter's (1903) equation.

4.3 Failure mechanism under the surcharge effect-passive state of equilibrium

In Figure 12 is shown a vertical plate anchor DE, with a horizontal cohesion-less backfill under surcharge loading. Soil unit weight is not considered in the analysis. The failure surface consists of log spiral EA, that originates from the anchor base with tangent AB meeting the ground surface at an angle, $(45^{\circ} - \phi/2)$. At point A, there is a conjugate failure plane AD, passing through the anchor top. Thus, as seen from the figure, ABD is a passive Rankine zone and pole of the log spiral lies on the line AD or its extension.

From Figure 12, the following information is generated.

 α = inclination of the tangent to the log spiral at point G with the horizontal

 r_0 = starting radius of the log spiral at the anchor base (at θ = 0)

 θ = spiral angle measured from the starting radius

 $r = \text{radius of log spiral at point G corresponding to the spiral angle } \theta$

 $\theta_{\rm m}$ = maximum spiral angle

 r_1 = radius of the maximum spiral angle at $\theta = \theta_{\rm m}$

 $\theta_{\rm v}$ = angle between vertical face of the plate anchor and the starting radius r_0

From Figure 13, which shows the free body diagrams of failure wedge, EACD, the following information is generated.

 P_{pqH} , P_{pqV} = horizontal and vertical components of resultant passive thrust, P_{pq} due to surcharge effect

 R_{pqH} , R_{pqV} = horizontal and vertical components of resultant soil reaction, R_{pq} acting on the curved part of the failure surface

 P_q = pasive thrust exerted by the backfill on the Rankine wall, AC

Q = resultant force due to surcharge

In Figure 13, line AC represents the Rankine wall and force, P_q as described above, is the force exerted on this wall by the backfill it retains. With this consideration and also considering that, pole of the log spiral lies above the anchor top on line AD, the dispositions of various forces are shown in the same figure.

4.3.1 Geometry of the failure surface

Referring to Figure 13 and considering triangle, ODE,

$$\frac{OD}{\sin\theta_{v}} = \frac{OE}{\sin(135 - \phi/2)} = \frac{DE}{\sin\theta_{m}} = \frac{h}{\sin\theta_{m}}$$
 (11)

Where, angles, $\theta_{\rm m}$ and $\theta_{\rm v}$ are as shown in the same figure.

From the above expression.

$$OD = \frac{h \sin \theta_v}{\sin \theta_m}$$

The initial radius, OE = r_0 of the log spiral is given as,

OE =
$$r_0 = \frac{h \sin(135 - \phi/2)}{\sin \theta}$$
...

Also, from the equation of the log spiral,

$$OA = r_0 \cdot e^{\theta_m \tan \phi} \tag{12}$$

And

$$AD = OA - OD$$

4.3.2 Computation of vertical and horizontal components of reaction on curved failure surface EA under the effect of surcharge

For the curved failure surface, EGA (Figure 13), Kötter's (1903) equation (Eq. 10a) takes the following form.

$$\frac{\mathrm{d}p}{\mathrm{d}s} + 2p\tan\phi \frac{\mathrm{d}\alpha}{\mathrm{d}s} = 0 \tag{13}$$

From quadrilateral, OEJG (Figure 12)

$$(90 + \theta_v) + \theta + 180 - \alpha + 90 - \phi = 360$$

With simplification,

$$\theta_v + \theta - \alpha - \phi = 0$$

Or,

$$\alpha = \theta - \phi + \theta$$

Differentiation with respect to θ gives,

$$d\alpha = d\theta \tag{14}$$

Combining Eq. 14 with Eq. 13, and multiplying throughout by ds/da, the following equation is obtained.

$$\frac{\mathrm{d}p}{p} = -2\tan\phi \cdot d\theta \tag{15}$$

For integration over the curved failure surface, EGA, the above equation is written as,

$$\int_{p}^{p_{A}} \frac{dp}{p} = -\int_{\theta}^{\theta_{m}} 2 \tan \phi d\theta$$

Where, p_A is the pressure intensity at point A (Figure 13).

Integration yields

$$p = p_A e^{2(\theta_m - \theta)\tan\phi} \tag{16}$$

From Eq. 16, the resultant soil reaction, R_{pq} on curved surface, EGA is given as,

$$R_{pq} = \int pds \tag{17}$$

Or

$$R_{pq} = \int p_A e^{2(\theta_m - \theta)\tan\phi} ds$$

From the geometry of log spiral,

$$ds = r \sec \phi d\theta \tag{18}$$

Using above equation, R_{pq} is obtained as,

$$R_{pq} = \int p_A e^{2(\theta_m - \theta)\tan\phi} r \sec\phi d\theta \tag{19}$$

With $r = r_0 e^{\theta \tan \phi}$ the above equation is transformed to,

$$R_{pq} = \int p_A e^{2(\theta_m - \theta)\tan\phi} r_0 e^{\theta\tan\phi} \sec\phi d\theta$$
 (20)

From Figure 13, considering Δ DEO

$$\theta_m = 180 - \theta_v - (90 + 45 - \phi/2)$$

Or,

$$\theta_m = 45 + \phi/2 - \theta_v$$

The angle (\angle FOG) made by the resultant, R_{pq} (Figure 13) with the horizontal can be obtained from the following expression.

$$\angle FOG = (45 - \phi / 2) + [45 + \phi / 2 - \theta_v] - \theta$$
$$\angle FOG = 90 - \theta_v - \theta$$

Or,

$$\angle FOG = \theta_L - \theta$$

Where,

$$\theta_{\rm L} = (90 - \theta_{\rm V})$$

The vertical component, R_{pqV} (Figure 13) of resultant soil reaction is then obtained as,

$$R_{pqV} = \int_{0}^{\theta_{m}} R_{pq} \sin(\theta_{L} - \theta) d\theta$$
 (21)

Similarly, the horizontal component, R_{pqH} (Figure 4) of soil reaction is obtained as,

$$R_{pqH} = \int_{0}^{\theta_{m}} R_{pq} \cos(\theta_{L} - \theta) d\theta$$
 (22)

4.3.3 Computation of reactive pressure distribution on the plane failure surface AB and reactive pressure at point A under the effect of surcharge

From the geometry of the problem, $\frac{d\alpha}{ds} = 0$ and Kötter's (1903) equation (Eq. 10a) takes the following form for a weightless medium.

$$\frac{\mathrm{d}p}{\mathrm{d}s} = 0\tag{23}$$

Integration yields,

$$p = \text{constant}$$
 (24)

Thus, the reactive pressure, p is uniformly distributed on the failure surface, AB and the resultant reaction, R' acts at the mid-point of AB.

To find the reactive pressure, p, equilibrium of failure wedge ABC is considered (Figure 16)

According to Rankine's theory, the passive thrust, P_q on the wall, AC is given as,

$$P_q = q \cdot AC \cdot K_p \tag{25}$$

Where, K_p is the coefficient of passive earth pressure for a horizontal cohesion-less backfill and it is as given by the following expression.

$$K_p = \frac{1 + \sin \phi}{1 - \sin \phi}$$

Horizontal equilibrium of the failure wedge ABC gives

$$P_q = R'\cos(45 - \phi/2) \tag{26}$$

From Eqs. 26 and 27 R' is obtained as

$$R' = q \cdot AB \cdot \tan(45 - \phi/2) K_n \tag{27}$$

The uniformly distributed soil pressure, p is then obtained as,

$$p = R' / AB$$

Or,

$$p = q \tan(45 - \phi/2) K_{p} \tag{28}$$

The intensity of reactive pressure, p_A at point A (Figures 12 and 14) is as given by the above expression.

From Figure 14, it is further seen that, the three-force equilibrium of the failure wedge, ABC gives the point of application of P_q at mid-point of the wall, AC.

4.4 Failure mechanism under the effect of soil self weight - passive state of equilibrium

Figure 15 shows the failure mechanism similar to that adopted for the analysis of the plate anchor with a horizontal cohesion-less backfill under surcharge effect. Using the above failure mechanism, the authors (2010 b)

have reported a method based on the application of Kötter's (1903) equation for the estimation of passive thrust on a vertical wall retaining horizontal cohesion-less backfill. The unique failure surface consisting of a log spiral and its tangent is identified on the basis of force equilibrium conditions and point of application of the passive thrust is computed using moment equilibrium. In the proposed analysis, this procedure is adopted to compute the values of passive thrust, $P_{\rm DV}$ under the effect of soil self weight and its point of application. The final expression for the reactive passive pressure distribution at any point on the curved failure surface, EA using Kötter's (1903) equation is obtained with the following expression.

$$p = \begin{bmatrix} \gamma r_0 \operatorname{Ksin} \left(\frac{\pi}{4} + \frac{\phi}{2} \right) e^{\tan \phi (3\theta_{\rm m} - 2\theta)} \\ + \frac{\gamma r_0 \sec \phi e^{\theta \tan \phi}}{\left(1 + 9 \tan^2 \phi \right)} \begin{cases} 3 \tan \phi \sin(\theta - \theta_{\rm L} + \phi) \\ -\cos(\theta - \theta_{\rm L} + \phi) \end{cases} \\ - \frac{\gamma r_0 \sec \phi e^{\tan \phi (3\theta_{\rm m} - 2\theta)}}{\left(1 + 9 \tan^2 \phi \right)} \begin{cases} 3 \tan \phi \sin(\theta_{\rm m} - \theta_{\rm L} + \phi) \\ -\cos(\theta_{\rm m} - \theta_{\rm L} + \phi) \end{cases} \end{cases}$$

$$(29)$$

Where, K is the parameter indicating location of the pole of the log spiral along line AO in terms of starting radius of log spiral r_0 as measured from point D (Figure 13) and $\theta_L = (90 - \theta_V)$

The distribution of reactive passive pressure on the failure surface is as shown in Figure 16. The magnitude of passive thrust on the vertical anchor plate and its point of application are thus obtained using Kötter's (1903) equation.

From Figure 17, the following information is generated.

 P_{pyH} , P_{pyV} = horizontal and vertical components of resultant passive thrust, P_{py}

 R_{pyH} , R_{pyV} = horizontal and vertical components of resultant soil reaction, R_{py} acting on the curved part of the failure surface

 H_1 = passive thrust exerted by the backfill on the Rankine wall AC

W_{ACD} = weight of soil in the failure wedge, forming a part of the Rankine zone

 W_{ADE} = weight of soil in the zone, EAD of the failure wedge, EABCD

 $Y_{pp\gamma}$ = the distance of point of application of $P_{p\gamma}$ from the anchor top

 \overline{X} = the distance from pole O to the centroid of sector, OEA formed by the log spiral

 h_{py} = distance of point of application of passive thrust, P_{py} from the anchor base

 η = varying angle of inclination of reactive pressure with the vertical

The resultant soil reaction, R_{py} (Figure 17) on the failure surface is obtained as,

$$R_{mi} = \int p.\mathrm{d}s \tag{30}$$

The vertical and horizontal components, $R_{p\gamma V}$ and $R_{p\gamma H}$ of resultant reaction are obtained as,

$$R_{\rm pyV} = \int_{0}^{\theta_{\rm m}} p \cos \eta \, \mathrm{d}s \tag{31}$$

$$R_{p\gamma H} = \int_{0}^{\theta_{m}} p \sin \eta . ds$$
 (32)

Where, ds is the length of failure surface and η is the varying angle of inclination of reactive pressure with vertical (Figure 17). The detailed calculations for estimation of the passive thrust are reported in the paper "Passive thrust on a vertical retaining wall with horizontal cohesion-less backfill" accepted for publication in Soils and Rocks, An International Journal of Geotechnical and Geo-environmental Engineering, Brazil. (Kame, Dewaikar and Choudhury, 2010-b)

4.5 Failure mechanism under combined effect of uniform surcharge loading and soil self weight -passive state of equilibrium

The distribution of reactive pressure on the failure surface is computed using Kötter's (1903) equation under the effect of uniform surcharge and soil self weight.

In Figure 18 is shown the free body diagram of failure wedge EACD for combined effect. The following information is generated from the figure.

 $P_{pq\gamma H}$, $P_{pq\gamma V}$ = horizontal and vertical components of resultant passive thrust, $P_{pq\gamma}$ under the combined effect.

 $R_{pq\gamma}$ = resultant reactive pressure on curved failure surface

4.5.1 Computation of reaction due to combined effect on the curved failure surface EA

The magnitude of vertical component of soil reaction, $R_{pq\gamma V}$ for the combined effect is obtained by adding up Eqs. 21 and 31 as,

$$R_{pq\gamma V} = R_{pqV+} R_{p\gamma V}$$

Or

$$R_{pq\gamma V} = \int_{0}^{\theta_{m}} R_{pq} \sin(\theta_{L} - \theta) d\theta + \int_{0}^{\theta_{m}} p \cos \eta . ds$$
 (33)

Similarly the horizontal component soil reaction, R_{pqyH} is obtained by adding Eqs. 22 and 32 as,

$$R_{pq\gamma H} = \int_{0}^{\theta_{m}} R_{pq} \cos(\theta_{L} - \theta) d\theta + \int_{0}^{\theta_{m}} p \sin \eta . ds$$
 (34)

4.5.2 Magnitude of passive thrust under the combined effect

In Figure 18, the passive Rankine thrust, H_1 under the effect of soil self weight and passive thrust, P_q on the wall, AC under the effect of surcharge loading (Eq. 25) act at a distance 1/2AC and 2/3AC respectively from point, C. Equilibrium of wedge, EACD is then considered.

Vertical force equilibrium condition gives

$$P_{\text{payV}} = P_{\text{pay}} \sin \delta = R_{\text{payV}} - W_{\text{ACD}} - W_{\text{ADE}} - Q \tag{35}$$

From which, $P_{pq\gamma}$ is obtained as,

$$P_{pq\gamma} = \frac{R_{pq\gamma V} - W_{ACD} - W_{ADE} - Q}{\sin \delta}$$
 (36)

In the above equation, Q is the equivalent force due to surcharge (Q = q.DC). It acts at the mid-point of DC.

Horizontal force equilibrium condition gives

$$P_{pq\gamma H} = P_{pq\gamma} \cos \delta = R_{pq\gamma H} + P_q + H_1 \tag{37}$$

From which, $P_{pq\gamma}$ is obtained as,

$$P_{\text{pq}\gamma} = \frac{R_{\text{pq}\gamma H} + P_q + H_1}{\cos \delta} \tag{38}$$

It may be noted that, both Eqs. 36 and 38 give the magnitude of unknown thrust, $P_{pq\gamma}$. These two equations will yield the same and unique value of $P_{pq\gamma}$ only when the equilibrium conditions correspond to those at failure, which are uniquely defined by a characteristic value of θ_V and this value can be determined by trial and error procedure.

4.5.3 Trial and error procedure for combined analysis - passive state of equilibrium

In this procedure, first a trial value of θ_V (Figure 18) is assumed and corresponding weight of trial failure wedge, EACD and resultant force due to surcharge (Figure 18) are computed. Using Eqs. 33 and 34, magnitudes of

vertical and horizontal components of soil reaction ($R_{pq\gamma V}$ and $R_{pq\gamma H}$) are computed and from Eqs. 36 and 38, values of $P_{pq\gamma}$ are determined. If the trial value of θ_V is equal to its characteristic value corresponding to the failure condition, the two computed values of $P_{pq\gamma}$ will be the same; otherwise, they will be different. For various trial values of θ_V , computations are carried out till the convergence is reached to a specified (third) decimal accuracy. Thus, in this method of analysis, the unique failure surface (Figure 19) is identified by locating the pole of log spiral in such a manner that, force equilibrium condition of failure wedge, EACD is satisfied.

4.5.4 Point of application of passive thrust under the combined effect

Moment equilibrium condition is now used to compute the point of application of passive thrust by considering moments of forces and reactions about the pole of the log spiral.

Referring to Figure 18, for pole above anchor top, the following moment equilibrium equation is obtained by considering moment of the various forces about the pole of the log spiral.

$$P_{\text{pq}\gamma\text{H}}(Y_{\text{pq}\gamma} + \text{FD}) = \begin{bmatrix} \left(W_{\text{ACD}} \cdot (\text{OF} + \frac{2}{3} \cdot \text{DC}) + W_{\text{ADE}} \cdot \overline{X} \right) \\ + H_{1} \left(\frac{2}{3} \cdot \text{AC} + \text{FD} \right) + Q \cdot (OF + 0.5DC) \\ + P_{q} \cdot (FD + 0.5AC) + P_{\text{pq}\gamma_{\text{V}}} \cdot \text{OF} \end{bmatrix}$$
(39)

In the above equation, terms on the right hand side represent moment of weight of soil in the failure wedge, EACD, moment of the force Q, moment of the forces H_1 and P_q and moment due to vertical component of the resultant passive thrust, $P_{pq\gamma V}$ about the pole, O. The term on the left hand side of the above expression is the moment due to horizontal component of the resultant passive thrust, $P_{pq\gamma H}$ about the pole, O. From the above equation, $Y_{pq\gamma}$ (which is the distance of point of application of $P_{pq\gamma}$ from the anchor top), is obtained as,

$$Y_{pq\gamma} = \frac{1}{P_{pq\gamma H}} \begin{bmatrix} \left(W_{ACD} \cdot (OF + \frac{2}{3} \cdot DC) + W_{ADE} \cdot \overline{X} \right) \\ + H_1 \left(\frac{2}{3} \cdot AC + FD \right) + Q \cdot (OF + 0.5DC) \\ + P_q \cdot (FD + 0.5AC) + P_{pq\gamma V} \cdot OF - P_{pq\gamma H} \cdot FD \end{bmatrix}$$

$$(40)$$

The height, $h_{pq\gamma}$ of the passive thrust, $P_{p\gamma}$ from the anchor base is then obtained as,

$$h_{pay} = h - Y_{pay}$$

The basic purpose of this analysis was to compute passive pressure thrust, $P_{pq\gamma}$ along with its location and study their variation with respect to the parameters involved in the analysis. The height, $h_{pq\gamma}$ of point of application of passive thrust from the anchor base is expressed in terms of its ratio with respect to the height, h of the plate anchor in a non-dimensional form $(h_{rq\gamma} = h_{pq\gamma}/h)$.

4.6 Failure mechanism under the surcharge effect - active state of equilibrium

In Figure 20 is shown a vertical anchor plate DE, with horizontal cohesion-less backfill under surcharge loading. Soil unit weight is not considered in the analysis. The failure surface, EL is assumed to be plane (Das, 1990). The reaction, R_{aq} on the failure surface is inclined with normal at an angle, ϕ (Coulomb, 1776).

4.6.1 Computation of active thrust

The inclination, θ_{cr} of the failure plane EL, with the horizontal gives maximum value of P_{aq} as per the procedure available in any text book.

4.6.2 Point of application of P_{aq}

This computation is facilitated using Kötter's (1903) equation (Figure 11 b) for a cohesion-less soil medium under active condition as given below.

For the present analysis $\gamma = 0$ and with this modification Eq. 10b is written as,

$$\frac{dp}{d\alpha} = 2p \tan \phi \tag{41}$$

Or

$$dp = 2p \tan \phi d\theta \tag{42}$$

For a plane failure surface, $d\theta$ is zero and the above equation finally becomes,

$$dp = 0 (43)$$

The corresponding solution is obtained as,

$$p = constant$$
 (44)

The above solution indicates that, soil reactive pressure; p is uniformly distributed along the failure plane, EL. Therefore, the resultant soil reaction, R_{aq} acts at the mid-point of the failure plane. Free body diagram of the failure wedge is shown in Figure 21.

In Figure 21 the distance, TU is 0.5DL or 0.5h/tan θ_{cr} . The force, Q of surcharge acts at the mid-point of DL and therefore, meets the force, R_{aq} at U. The three force equilibrium requires that, line of the active thrust, P_{aq} should also pass through point U and this facilitates computation of its point of application.

The distance h_{aq} of point of application of P_{aq} as measured from the wall base is then given as,

$$h_{aq} = 0.5h \left[1 - \frac{\tan \delta}{\tan \theta_{\rm cr}} \right] \tag{45}$$

4.6.3 Active thrust under the effect of soil self weight

For this analysis, the method proposed by Dewaikar *et al.* (2003) is used. The angle, θ_{cr} of the failure plane EL is obtained using trial and error procedure, coupled with Kötter's (1903) equation.

For a plane failure surface, $d\theta$ is zero and Kötter's (1903) equation as given above takes the following form.

$$dp = \gamma \sin(\theta - \phi) . ds \tag{46}$$

Integration yields,

$$p = \gamma \sin(\theta - \phi) \cdot s + C_1 \tag{47}$$

At point L, both p and s are zero and with this condition the constant C_1 works out to be zero. Therefore, the reactive pressure, p on the failure surface is finally expressed as,

$$p = \gamma \sin(\theta - \phi).s \tag{48}$$

To compute reaction, $R_{a\gamma}$, the above expression is integrated within the limits s=0 (at point L) to s= length EL (at point E).

$$R_{a\gamma} = \gamma \int_{0}^{AC} \sin(\theta - \phi) . s ds \tag{49}$$

$$R_{a\gamma} = 0.5\gamma \sin(\theta - \phi)AC^2 \tag{50}$$

From Figure 23, length EL can be written as,

$$EL = h/\sin\theta \tag{51}$$

Substitution of the above value of EL in the expression for $R_{a\gamma}$ gives

$$R_{av} = 0.5 \gamma \sin \left(\theta - \phi\right) h^2 / \sin^2 \theta \tag{52}$$

Now referring to Figure 23, the vertical force equilibrium gives

$$W - P_{a\gamma} \sin \delta - R_{a\gamma} \sin(90 - \theta + \phi) = 0$$

$$\tag{53}$$

In the above equation, W is the weight of the wedge, DLE.

Or

$$W - P_{a\gamma} \sin \delta - \left\{ \frac{0.5 \gamma \sin (\theta - \phi) h^2}{\sin^2 \theta} \right\} \sin(90 - \theta + \phi) = 0$$
 (54)

From which, P_{ay} is obtained as,

$$P_{a\gamma} = \frac{\left\{ W - \left[\frac{0.5 \gamma \sin (\theta - \phi) h^2}{\sin^2 \theta} \right] \sin(90 - \theta + \phi) \right\}}{\sin \delta}$$
 (55)

Again refering to Figure 23, horizontal force equilibrium gives,

$$P_{a\gamma}\cos\delta - \frac{\left[0.5\gamma\sin(\theta - \phi)h^2\right]}{\sin^2\theta}\cos(90 - \theta + \phi) \tag{56}$$

Eqs. (55) and (56) will yield the same value of $P_{a\gamma}$ for the critical value of θ , denoted as θ_{cr} .

Therefore in the analysis, various trial values of θ are chosen and when the two values of $P_{a\gamma}$ (Eqs. 55 and 56) match each other (up-to three decimal places), trials are terminated.

The reaction $R_{a\gamma}$ corresponding to θ_{cr} is then computed as,

$$R_{a\gamma} = \frac{0.5\gamma \sin(\theta_{cr} - \phi)h^2}{\left(\sin \theta_{cr}\right)^2} \tag{57}$$

4.6.4 Point of application of Pay

For this purpose, first point of application of $R_{a\gamma}$ is computed. Referring to Figure 23, in which the angle, θ is now θ_{cr} , moments of elemental reactive forces about the anchor base are considered.

The elemental reaction, $dR_{a\gamma}$ at any point on the failure plane EL is computed as

$$dR_{a\gamma} = \gamma \sin(\theta_{cr} - \phi)s \cdot ds \tag{58}$$

The moment, dM₁ of normal component of elemental reaction about the wall base is given as,

$$dM_1 = \gamma \sin(\theta_{cr} - \phi) \cdot s \left(\frac{h}{\sin \theta_{cr}} - s\right) \sin \phi \cdot ds$$
 (59)

Integration yields the total moment M₁.

$$M_1 = \gamma \int_0^{H/\sin\theta_{cr}} \sin(\theta_{cr} - \phi) \cdot \left(\frac{h}{\sin\theta_{cr}} - s\right) s \sin\phi \cdot ds$$
 (60)

$$= \gamma \sin(\theta_{cr} - \phi) \sin \phi \left(\frac{h}{\sin \theta_{cr}}\right)^3 / 6 \tag{61}$$

The moment, M_2 of normal component of total reaction, R_{ay} about the anchor base is expressed as,

$$M_2 = R_{a\gamma} \sin \phi \cdot x = \frac{0.5\gamma \sin(\theta_{cr} - \phi)h^2 \sin \phi \cdot x}{\sin^2 \theta_{cr}}$$
 (62)

Where, x is the distance of R_{ay} from the anchor base, along the failure surface, EL.

Equating the expressions as given by Eqs. 61 and 62, x is finally computed as,

$$x = \frac{[h/\sin\theta_{cr}]}{3} = \frac{EL}{3} \tag{63}$$

Thus, the reactive force, $R_{a\gamma}$ acts at a distance of 1/3 EL as measured from the anchor base. From Figure 23, it is further seen that, distance ET is equal to h/3, since forces $P_{a\gamma}$, W and $R_{a\gamma}$ meet at point U which is located such that EU = EL/3.

The point of application of P_{ay} is finally computed by considering the following geometry from Figure 23.

$$h_{a\gamma} = ET - UT \cdot \tan \delta$$
 and UT = 1/3DL = h/(3\tan\theta) (64)

Where h_{av} is the height of P_{av} above the anchor base.

4.7 Active thrust under combined effect

The values of $P_{aq\gamma}$ and $R_{aq\gamma}$ (Figure 24) can be obtained by varying the inclination of failure plane EL so as to identify critical value θ_{cr} giving maximum value of $P_{aq\gamma}$ and corresponding value of $R_{aq\gamma}$.

From the results obtained for P_{aq} , $P_{a\gamma}$ it is seen that, the angle θ_{cr} that maximizes the active thrust, remains the same in all the cases (surcharge effect, soil self weight effect and combined effect) and therefore the summation of active thrust values $(P_{aq}, P_{a\gamma})$ exactly matches with the values $P_{aq\gamma}$ that is computed for the combined effect.

4.7.1 Point of application of P_{aqy}

The principle of superposition leads to the computation of point of application of active thrust, $P_{aq\gamma}$ using moment equilibrium about the anchor base. The following expression is obtained.

$$h_{aq\gamma} = \frac{P_{aq}.h_{aq} + P_{a\gamma}.h_{a\gamma}}{P_{aa\gamma}} \tag{65}$$

Where, $h_{aq\gamma}$ is the distance of point of application of $P_{aq\gamma}$ as measured from anchor base.

4.8 Analysis of the plate anchor

Referring to Figure 10, all the three equilibrium conditions are examined.

4.8.1 Vertical equilibrium

The forces involved are $P_{pq\gamma}\sin\delta$ and N in the vertically upward direction and $P_{aq\gamma}\sin\delta$ and W_p in the vertically downward direction. Since $P_{pq\gamma}\sin\delta > P_{aq\gamma}\sin\delta$ and weight, W_p of the plate is small enough, there is no equilibrium of the forces in the vertical direction. The reaction, N is zero and the plate accelerates in the vertically upward direction. This agrees well with the experimental observation (Naser, 2006).

4.8.2 Moment equilibrium

The forces N and Ntan δ now can be considered to be zero and the moment equilibrium is considered about the point, A as shown in Figure 10. The only forces that contribute to the moment equilibrium are $P_{aq\gamma}$ and $P_{pq\gamma}$ and since $P_{pq\gamma} > P_{aq\gamma}$, clearly moment equilibrium is also not satisfied. The plate rotates at limit equilibrium and this agrees well with the experimental observation (Naser, 2006).

4.8.3 Horizontal equilibrium

Summing up the forces in horizontal direction the following expression is obtained.

$$T_u = P_{pq\gamma}\cos\delta - P_{aq\gamma}\cos\delta \tag{66}$$

As stated earlier, $P_{aq\gamma}$ and $P_{pq\gamma}$ are evaluated using Kötter's (1903) equation and thus T_u is determined from the horizontal equilibrium condition.

The values of T_u are computed using the available experimental data and comparisons with the available theoretical solutions are made.

5. Results and Discussions

For the purpose of comparison, detailed information on the available theoretical solutions and the proposed method is reported in Table 1.

The non-dimensional pullout force coefficient, Myq is defined using following expression.

$$M\gamma q = \frac{T_u}{\gamma B h^2} \tag{67}$$

In the present analysis, for a vertical strip plate anchor (H/h = 1 to 5) a total of eight experimental studies (Neely et al., 1973; Das and Seeley, 1975; Akinmusuru, 1978; Ovesen and Stroman, 1964; Dickin and Leung, 1985; Hoshiya and Mandal, 1984; Murray and Geddes, 1987; Rowe and Davis, 1982 and Basudhar and Singh, 1994) and a total of eight theoretical methods (Ovesen and Stroman, 1964; Meyerhof, 1973; Neely et al., 1973, Surcharge method; Neely et al., 1973, Equivalent Free Surface Method (m = 0); Neely et al., 1973, Equivalent Free Surface Method (m = 1); Das and Seeley, 1975; Rowe and Davis, 1982 and Merifield and Sloan, 2005, SNAC) are referred for comparison with the proposed solution and the results are reported in Table 3. In addition to this, computations are performed for (i) different values of H/h ranging from 0 to 5, (ii) different values of ϕ varying from 20° to 45° with an interval of 5°, and (iii) three values of δ , namely 0, 0.5 ϕ and ϕ . The numerical results obtained from the analysis are summarized below

In Table 2, the results reported by Kumar and Sahoo (2011), Soubra (2000), and Chen (1975) using the upper bound limit analysis are compared with those obtained by the proposed method. The results obtained by Kumar (2002) using upper bound analysis based on bilinear and composite logarithmic spiral failure are also reported in the table.

The comparison shows that, proposed values are higher than all the earlier reported values. However with increasing δ and ϕ , the difference becomes less.

The values of force coefficient (Myq) as computed by the proposed method are reported in Table 3 along with corresponding experimental results and the prediction based on the available theoretical methods. A wide variation is seen in the results. However it is seen that, up-to the embedment ratio of H/h = 3, the proposed method shows a reasonable agreement with the available experimental data.

In Figure 25, the results obtained by the proposed method are compared with the experimental results reported by Ovesen and Stroman (1964) vis-a-vis other theoretical predictions. It is seen that, there is a large difference between the theoretical predictions and the experimental results in respect to value of Myq. As compared to the proposed method, the experimental results of Ovesen and Stroman (1964) are on the lower side.

As seen from Table 3, results of the proposed method compare well with the theoretical results reported by Neely et al. (1973, surcharge method, equivalent free surface method with m = 0) up to the embedment ratio of 3. From Table 2 it is further seen that, there is a good agreement between results of the proposed method and the Meyerhof's (1973) method up-to embedment ratio of 5 with the maximum difference of 14%.

In Figure 26, the experimental results of Neely et al. (1973) are compared with the results predicted by various available theoretical methods.

It is seen that, the proposed method and methods proposed by Ovesen and Stroman (1964), Meyerhof (1973), Neely et al. (1973) show a good agreement with the experimental results up to the embedment ratio of 3.

The data reported in Table 3 further shows that, results of the proposed method and the other theoretical methods when compared with the experimental data of Akinmusuru (1978) and Hoshiya and Mandal (1984) show large differences. However, the values of Myq as obtained by the proposed method and those of Ovesen and Stroman (1964) and Meyerhof (1973), show a reasonably good agreement up-to the embedment ratio of 3.

In Figure 27, a comparison is shown between the experimental results reported by Das and Seeley (1975) and the results predicted by various theoretical methods. It is seen that, the methods proposed by Rowe and Davis (1982) and Merifield and Sloan (2005) show a better agreement with experimental results for all embedment depths. The methods proposed by Neely et al. (1973, m = 0 and 1). Das and Seeley (1975) and the proposed method show a fair agreement with experimental results up-to embedment ratio of 3.0.

The experimental data reported by Dickin and Leung (1985) is compared with the available theoretical solutions as shown Figure 28. The proposed method and the method by Neely et al. (1973, surcharge method) perform better than the other methods whereas, the method of Ovesen and Stroman (1964) and Neely et al. (1973, equivalent free surface method, m = 0) show a reasonably good agreement with the experimental results. The equivalent free surface method Neely et al. (1973, m = 1), method of Das and Seeley (1975), Rowe and Davis (1982) and Merifield and Sloan (2005) overestimate the results.

From the above discussion it is clearly seen that, there is no unique theoretical solution for the analysis of a vertical plate anchor in cohesion-less soil. The proposed method is intended for shallow laid anchors only and with this limitation, it shows a reasonably good agreement with some of the experimental/theoretical results up-to the embedment ratio of 3.0.

6. Conclusions

A numerical method based on the application of Kötter's (1903) equation is proposed for the estimation of pullout capacity of shallow laid vertical plate anchors in cohesion-less soil. The unique failure surfaces under active and passive state of limit equilibrium are identified on the basis of force equilibrium conditions. Kötter's (1903) equation facilitates the computation of point of application of active and passive thrusts.

Comparison of the results of the proposed method with the available experimental results vis-a-vis other theoretical methods shows that, up-to embedment ratio of 3.0, the proposed method is capable of making reasonably good predictions.

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Table 1. Comparison of the proposed method with the available theoretical solutions

| Name | Authors | Method adopted | Failure mechanism/ model adopted | Comments |
|-----------------|----------------------------------|---------------------------------------------------------------------------------------|---------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------|
| Method 1 | Ovesen and Stromann (1964) | Limit equilibrium (1948) | Failure mechanism proposed by Hansen (1953) | Use of earth pressure coefficients reported by Caquot and Kerisel (1948) |
| Method 2 | Meyerhof (1973) | Semi-empirical (1965) | Logarithmic spiral | Use of earth pressure coefficients reported by Caquot and Kerisel (1948) and Sokolovskii (1965) |
| Method 3 | Neely <i>et al.</i> (1973) | Surcharge method (limit analysis and plasticity solutions) | Logarithmic spiral and its tangent | Pole of the logarithmic spiral is assumed to be located at anchor top and resistance due to active earth pressures is neglected |
| Methods 4 and 5 | Neely <i>et al.</i> (1973) | Equivalent free surface method (m = 0, 1) m=degree of mobilization of shear strength | Logarithmic spiral | Pole of the logarithmic spiral is assumed to be located at anchor top and resistance due to active earth pressures is neglected |
| Method 6 | Das and Seeley (1975) | Semi-empirical | Based on laboratory model tests | Use of chart/graph |
| Method 7 | Rowe and Davis (1982) | Two-dimensional finite element analysis | Elasto-plastic soil model | Use of design charts |
| Method 8 | Merifield and Sloan (2005) | Finite element analysis | Solid Nonlinear Analysis Code (SNAC) | Use of chart/graph |
| Method 9 | Kumar and Sahoo (2011) | Upper bound theorem of the limit analysis in combination with finite elements | Elasto-plastic soil model | Use of chart/graph |
| Proposed method | Kame <i>et al.</i> (2011) | Kötter's (1903) equation coupled with limit equilibrium analysis | Log spiral and its tangent | All equilibrium equations are used. |

Table 2. Comparison of force coefficient (M γ q) for H/h = 1

| | | Proposed | roposed Kumar and Sahoo Kumar (2002) Chen (1975) | | 75) | Soubra | | |
|-----|-----------------------------|----------|--------------------------------------------------|----------|------------|----------|------------|--------|
| ф | ϕ δ/ϕ method | | (2011) Method 9 | Bilinear | Log-spiral | Bilinear | Log-spiral | (2000) |
| | 0 | 1.71 | 1.37 | 1.50 | 1.50 | 1.50 | 1.50 | 1.50 |
| 30° | 0.5 | 2.42 | 2.15 | 2.28 | 2.28 | 2.28 | 2.28 | 2.27 |
| | 1 | 3.16 | 2.80 | 3.14 | 3.07 | 3.14 | 3.07 | 2.97 |
| | 0 | 2.73 | 2.24 | 2.30 | 2.30 | 2.30 | 2.30 | 2.30 |
| 40° | 0.5 | 4.96 | 4.64 | 4.76 | 4.74 | 4.75 | 4.75 | 4.70 |
| | 1 | 8.14 | 7.42 | 8.71 | 8.01 | 8.70 | 8.01 | 7.51 |

Table 3. Comparison of force coefficient $(M\gamma q)$ – Experimental results and theoretical methods

| | I | | | | | | | | | | | | | |
|-----------------------------|-----------|-----------|--------|-----|-----------------|-----------------|-------------|----------|----------|-------------|-------------|-------------|-------------|-------------|
| Exp. Method | Anchor pa | nrameters | | | Exp. results | Proposed method | Method 1 | Method 2 | Method 3 | Method 4 | Method 5 | Method 6 | Method 7 | Method 8 |
| | γ kN/m³ | ф | δ | H/h | Мγq | Mγq | Мүq | Mγq | Мүq | Mγq | Mγq | Мүq | Муq | Мγq |
| | | | | 1 | 2.83 | 9.43 | 2.96 | 2.56 | 9.26 | 9.90 | 9.90 | 7.59 | 8.77 | 10.08 |
| Ovesen and | | | | 2 | 7.6 | 21.73 | 12.16 | 10.24 | 21.72 | 22.60 | 27.00 | 24.31 | 29.56 | 29.52 |
| Stroman | 16.77 | 42° | 38.66° | 3 | 15 | 34.22 | 27.65 | 23.04 | 36.85 | 41.60 | 53.00 | 48.04 | 60.43 | 55.20 |
| (1964) | | | | 4 | 23.6 | 46.75 | 49.50 | 40.96 | 54.20 | 64.00 | 80.80 | 77.90 | 92.15 | 84.64 |
| | | | | 5 | 32.87 | 59.29 | 77.81 | 64 | 75.13 | 89.20 | 109.20 | 113.33 | 129.17 | 119.70 |
| | | | | 1 | 3.5 | 4.61 | 2.44 | 2.18 | 5.05 | 5.70 | 5.70 | 5.73 | 6.15 | 8.19 |
| | | | | 2 | 13.5 | 11.55 | 10.03 | 8.72 | 12.17 | 16.30 | 20.00 | 18.37 | 20.77 | 24.06 |
| Neely <i>et al</i> . (1973) | 15.9 | 38.5° | 21° | 3 | 27 | 18.70 | 22.63 | 19.62 | 20.55 | 28.30 | 39.00 | 36.30 | 42.49 | 45.23 |
| (111) | | | | 4 | 45 | 25.90 | 40.22 | 34.88 | 30.05 | 43.00 | 58.40 | 58.86 | 64.01 | 69.52 |
| | | | | 5 | 75 | 33.11 | 62.77 | 54.5 | 41.41 | 59.10 | 79.10 | 85.64 | 88.93 | 98.35 |
| | | | | 1 | 5.1 | 4.47 | 1.96 | 1.82 | 4.48 | 4.62 | 4.70 | 3.84 | 3.93 | 5.76 |
| Das and | | | | 2 | 16 | 10.91 | 8.19 | 7.28 | 11.16 | 11.80 | 14.00 | 12.31 | 12.84 | 17.04 |
| Seeley | 15.92 | 34° | 34° | 3 | 31 | 16.37 | 18.55 | 16.38 | 18.70 | 20.80 | 26.00 | 24.33 | 25.99 | 32.40 |
| (1975) | | | | 4 | 50 | 21.03 | 33.00 | 29.12 | 28.00 | 31.60 | 39.00 | 39.45 | 40.21 | 50.08 |
| | | | | 5 | 74 | 25.17 | 51.53 | 45.5 | 37.60 | 45.60 | 53.60 | 57.39 | 56.94 | 70.90 |
| | | | | 1 | 8 | 4.37 | 1.95 | 1.9 | 4.42 | 5.10 | 5.10 | 4.22 | 4.23 | 6.30 |
| 41. | | | | 2 | 21 | 10.73 | 7.94 | 7.6 | 10.97 | 13.00 | 15.00 | 13.52 | 13.83 | 18.60 |
| Akinmusuru (1978) | 15.55 | 35° | 29° | 3 | 38 | 17.23 | 17.59 | 17.1 | 18.29 | 23.00 | 28.00 | 26.71 | 28.01 | 35.25 |
| , , | | | | 4 | 60 | 23.77 | 30.71 | 30.4 | 27.26 | 35.00 | 42.00 | 43.31 | 43.12 | 54.40 |
| | | | | 5 | 88 | 30.31 | 47.10 | 47.5 | 36.57 | 50.00 | 58.00 | 63.01 | 60.84 | 77.00 |
| | | | | 1 | 3.4 | 3.03 | 1.54 | 1.465 | 5.50 | 2.90 | 2.90 | 2.43 | 2.74 | 3.50 |
| Hoshiya and | | | | 2 | 14.5 | 7.49 | 6.58 | 5.86 | 13.53 | 8.05 | 9.50 | 7.79 | 8.93 | 10.52 |
| Mandal | 14.12 | 29.5° | 29.5° | 3 | 34 | 11.24 | 14.87 | 13.185 | 22.18 | 14.20 | 17.00 | 15.40 | 18.06 | 20.46 |
| (1984) | | | | 4 | 62 | 14.43 | 26.34 | 23.44 | 33.13 | 20.70 | 25.50 | 24.97 | 28.67 | 31.96 |
| | | 35° | | 5 | 99 | 17.27 | 40.93 | 36.625 | 44.37 | 28.00 | 33.80 | 36.33 | 41.31 | 45.30 |

| Method 1 | Method 2 | Method 3 | Method 4 | Method 5 | Method 6 | Method 7 | Method 8 |
|------------------------------------|-----------------|-----------------------------------------------|--------------------------------------------------------------------------|--------------------------------------------------------------------------|-----------------------------|-----------------------------|--------------------------------------------|
| Ovesen and Stroman (1964) | Meyerhof (1973) | Neely et al. (1973) Surcharge method | Neely et al. (1973) - Equivalent free surface method (m = 0) | Neely et al. (1973) - Equivalent free surface method (m = 1) | Das and Seeley (1975) | Rowe and Davis (1982) | Merifield and Sloan (2005) – SNAC |

m = degree of mobilization

Table 3. Comparison of force coefficient $(M\gamma q)$ – Experimental results and theoretical methods (Continued)

| Exp. Method | Anchor pa | nrameters | | | Exp. results | Proposed method | Method 1 | Method 2 | Method 3 | Method 4 | Method 5 | Method 6 | Method 7 | Method 8 | | | | | | | | | | | |
|-----------------------|------------------|-----------|-------|-----|-----------------|-----------------|----------|----------|----------|----------|-------------|----------|-------------|-------------|---|------|-------|-------|------|-------|-------|-------|-------|-------|-------|
| | $\gamma kN/m^3$ | ф | δ | H/h | Мүq | Mγq | Mγq | Mγq | Мүq | Мүq | Мүq | Mγq | Мүq | Мүq | | | | | | | | | | | |
| | | | | 1 | 3.8 | 6.77 | 2.75 | 2.43 | 7.05 | 8.70 | 8.70 | 7.02 | 8.15 | 9.54 | | | | | | | | | | | |
| Dickin | | | | 2 | 14.6 | 16.43 | 11.23 | 9.72 | 16.69 | 20.80 | 25.00 | 22.50 | 27.40 | 27.96 | | | | | | | | | | | |
| and Leung | 16 | 41° | 29° | 3 | 28.2 | 26.31 | 25.31 | 21.87 | 28.43 | 37.80 | 49.00 | 44.46 | 56.00 | 52.35 | | | | | | | | | | | |
| (1985) | (1985) | | | 4 | 44 | 36.23 | 44.97 | 38.88 | 41.99 | 58.00 | 74.40 | 72.08 | 84.87 | 80.32 | | | | | | | | | | | |
| | | | | 5 | 62.5 | 46.18 | 70.16 | 60.75 | 58.65 | 80.60 | 100.60 | 104.87 | 118.43 | 113.60 | | | | | | | | | | | |
| | | | | 1 | 3.5 | 4.69 | 2.97 | 2.77 | 5.05 | 11.82 | 11.82 | 8.56 | 9.83 | 10.94 | | | | | | | | | | | |
| Murry and | | | | 2 | 7.8 | 11.94 | 11.80 | 11.08 | 12.23 | 25.48 | 30.20 | 27.42 | 33.18 | 32.02 | | | | | | | | | | | |
| Geddes | 16.5 | 43.6° | 10.6° | 3 | 12 | 19.52 | 26.04 | 24.93 | 21.74 | 47.68 | 59.40 | 54.19 | 67.87 | 59.76 | | | | | | | | | | | |
| (1989) | | | | 4 | 16.5 | 27.15 | 45.37 | 44.32 | 33.84 | 73.60 | 91.04 | 87.87 | 104.40 | 91.55 | | | | | | | | | | | |
| | | | | 5 | 21.5 | 34.80 | 69.54 | 69.25 | 48.60 | 102.96 | 122.96 | 127.83 | 147.25 | 129.46 | | | | | | | | | | | |
| | | | | 1 | 3 | 4.61 | 2.21 | 2.18 | 5.05 | 5.70 | 5.70 | 5.73 | 6.15 | 8.19 | | | | | | | | | | | |
| Basudhar and Singh | | | | 2 | 15 | 11.55 | 8.68 | 8.72 | 12.17 | 16.30 | 20.00 | 18.37 | 20.77 | 24.06 | | | | | | | | | | | |
| | 16 | 38.5° | 21° | 3 | 27.6 | 18.70 | 18.74 | 19.62 | 20.55 | 28.30 | 39.00 | 36.30 | 42.49 | 45.23 | | | | | | | | | | | |
| (1994) | | | | 4 | 46 | 25.91 | 31.92 | 34.88 | 30.05 | 43.00 | 58.40 | 58.86 | 64.01 | 69.52 | | | | | | | | | | | |
| | | | | | | | | ļ | | Ī | | | | | 5 | 78.5 | 33.12 | 47.84 | 54.5 | 41.41 | 59.10 | 79.10 | 85.64 | 88.93 | 98.35 |

| Method 1 | Method 2 | Method 3 | Method 4 | Method 5 | Method 6 | Method 7 | Method 8 |
|------------------------------------|-----------------|-----------------------------------------------|--------------------------------------------------------------------------|-----------------------------------------------------------------------|-----------------------------|-----------------------------|--------------------------------------------|
| Ovesen and Stroman (1964) | Meyerhof (1973) | Neely et al. (1973) Surcharge method | Neely et al. (1973) - Equivalent free surface method (m = 0) | Neely et al. (1973) - Equivalent free surface method (m = 1) | Das and Seeley (1975) | Rowe and Davis (1982) | Merifield and Sloan (2005) – SNAC |

m = degree of mobilization

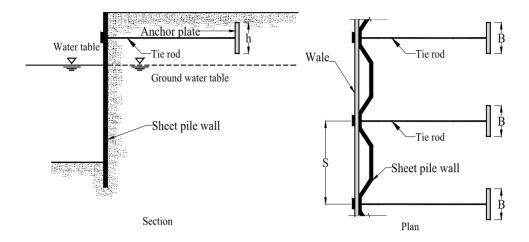


Figure 1. Sheet pile wall

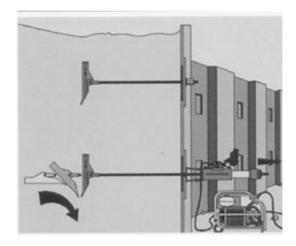


Figure 2. Retaining wall (www.anchorsystems.co.uk)

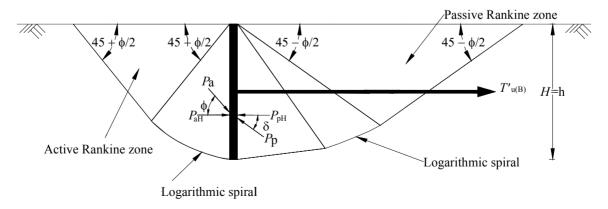


Figure 3. Basic case-failure surface of a vertical plate anchor in cohesion-less soil (Ovesen and Stromann, 1972)

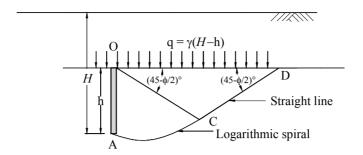


Figure 4. Surcharge method (Neely et al., 1973)

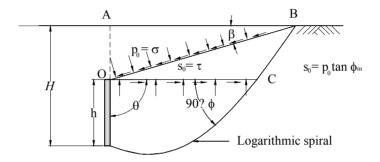


Figure 5. Equivalent free surface analysis (Neely et al., 1973)

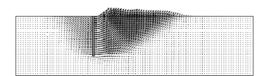


Figure 6. Failure modes and zones of plastic yielding for rough vertical anchors in cohesion-less soils (ϕ =20°), Merifield *et al.* (2006)

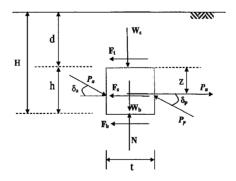


Figure 7. Free body diagram of a block anchor (Naser, 2006)

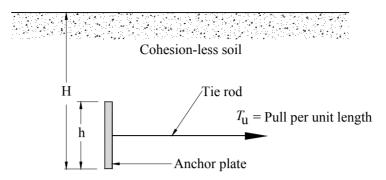


Figure 8. Anchor plate – Definition of basic parameters

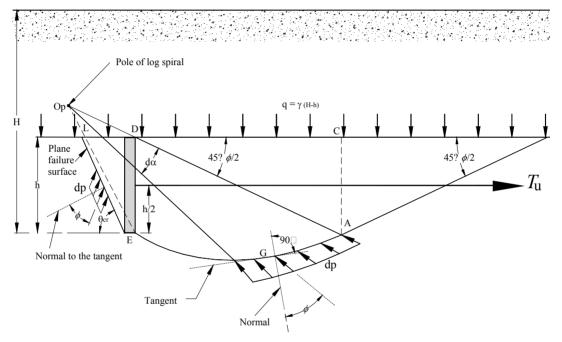


Figure 9. Failure mechanism at ultimate load for a continuous (strip) vertical plate anchor in cohesion-less soil

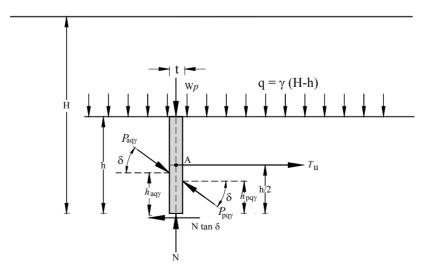


Figure 10. Free body diagram of the anchor plate

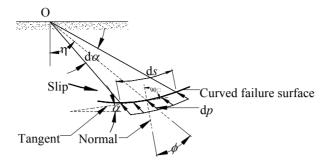


Figure 11. (a) Reactive pressure distribution on the failure surface for passive case (Kame, Dewaikar and Choudhury, 2010-b)

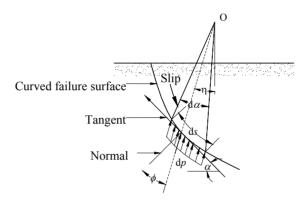


Figure 11. (b) Reactive pressure distribution on the failure surface for active case (Kame, Dewaikar and Choudhury, 2010-a)

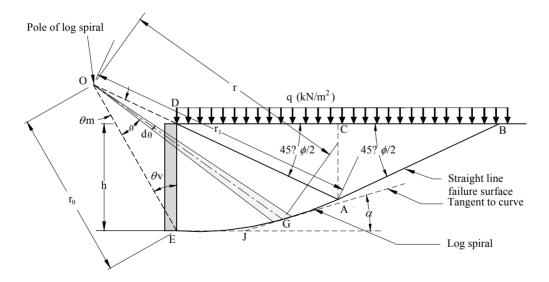


Figure 12. Surcharge effect – failure mechanism

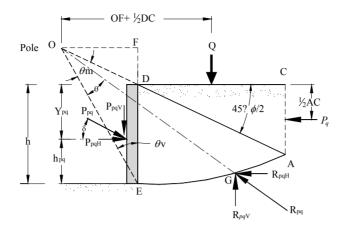


Figure 13. Free body diagram of failure wedge EACD - surcharge effect

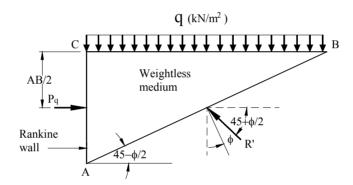


Figure 14. Free body diagram of failure wedge ABC

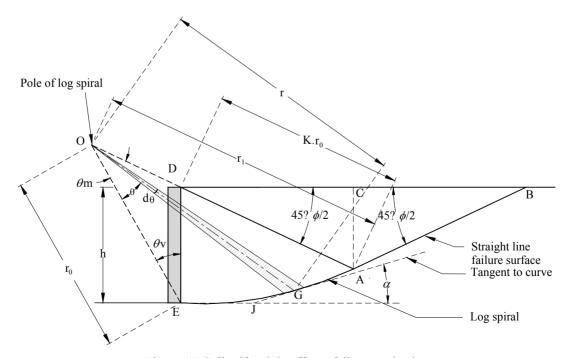


Figure 15. Soil self weight effect - failure mechanism

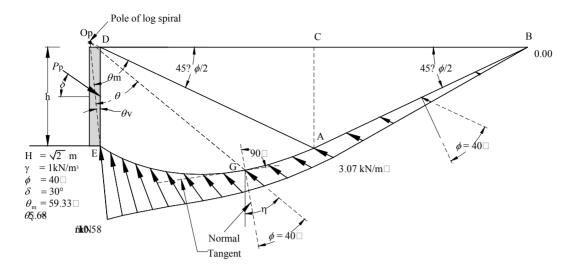


Figure 16. Reactive passive pressure distribution on the failure under the effect of soil self weight using Kötter's (1903) equation (Kame, Dewaikar and Choudhury, 2010-b)

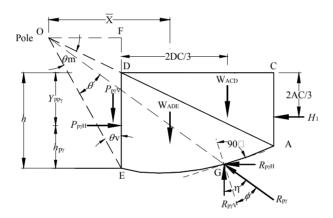


Figure 17. Free body diagram of failure wedge EACD - soil self weight effect

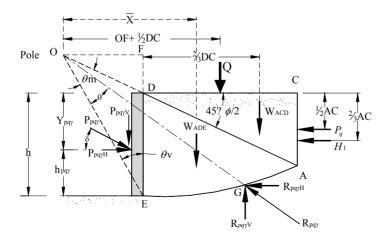


Figure 18. Free body diagram of failure wedge EACD - combined effect

Final failure surface

Log spiral

Е

Figure 19. Trial procedure for locating pole of the log spiral - passive state of equilibrium

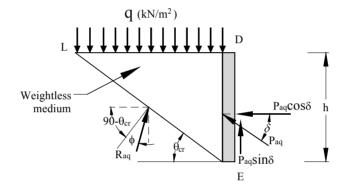


Figure 20. Surcharge effect – failure mechanism

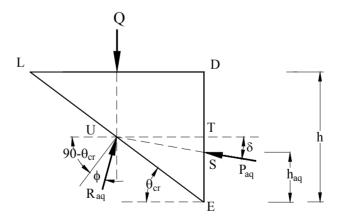
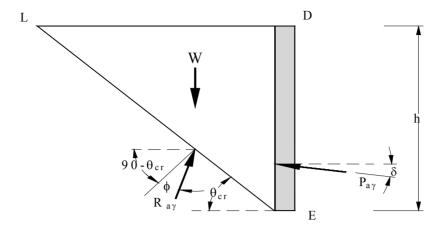


Figure 21. Free body diagram of the failure wedge, ABC



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Figure 22. Soil self weight effect – failure mechanism

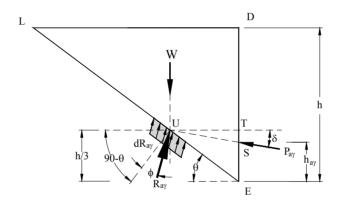


Figure 23. Free body diagram of failure wedge DEL

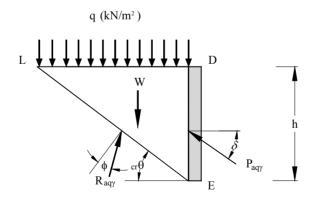


Figure 24. Combined effect – failure mechanism

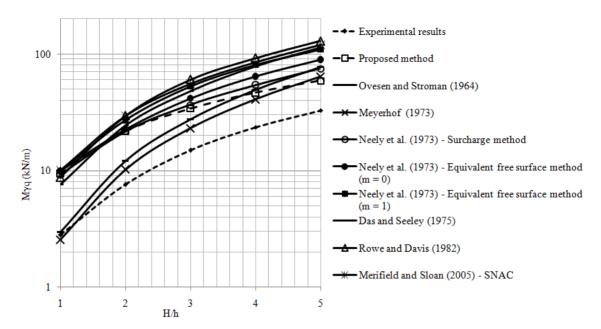


Figure 25. Comparison of theoretical methods with experimental results of Ovesen and Stroman (1964)

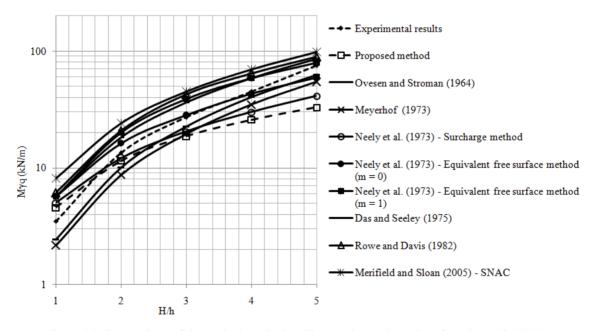


Figure 26. Comparison of theoretical methods with experimental results of Neely et al. (1973)

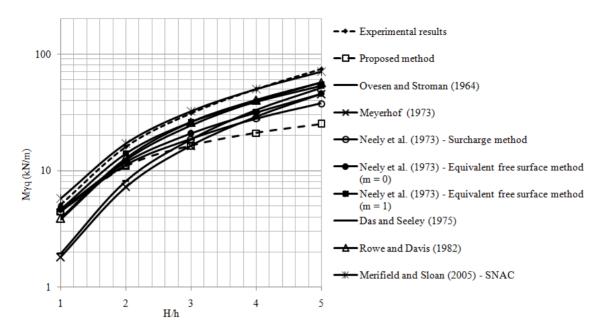


Figure 27. Comparison of theoretical methods with experimental results of Das and Seeley (1975)

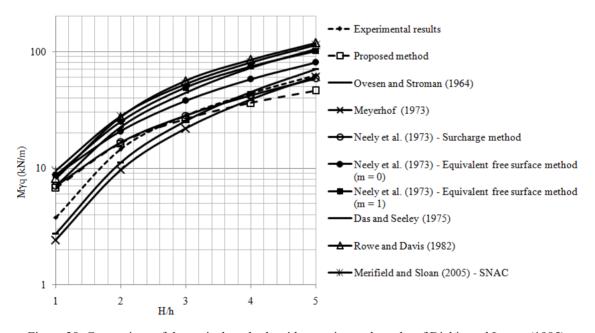


Figure 28. Comparison of theoretical methods with experimental results of Dickin and Leung (1985)