

Pressure Dependency Grüneisen Parameter γ for bcc Mo

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Abstract

It has been reinforced by Kushwah et al. (Kushwah, 2013) that the Lindemann law doesn't work satisfactorily for the transition metals. We think this point is open to question. Combining the Lindemann law and the Vinet et al thermal equation of state with the melting curves of bcc Mo, we present an explicitly simple expression of the pressure dependency Grüneisen parameter γ for Molybdenum. The results yield good agreement with density functional theory and experiments.

Keywords: Molybdenum, Grüneisen parameter, melting temperature

1. Introduction

The transition metal Molybdenum (Mo) has wide engineering and technology application for its thermal and mechanical strength and chemical resistance (Errandonea, 2001; Santamaría-Pérez, 2009; Belonoshko, 2008; Moruzzi, 1988). At low temperatures, Mo is stable in the body-centered-cubic (bcc) phase up to a pressure (P) of about 700GPa, where it transforms to fcc phase (Belonoshko, 2008). Considerable experimental and theoretical methods had been developed for Mo to study its thermodynamic properties such as melting temperature T_m , thermal equation of state (EOS), Grüneisen parameter γ and Debye temperature Θ_D , et al (Hixson, 1992; Zhang, 2008; Errandonea, 2005; Burakovsky, 2004; Kushwah, 2013; Zeng, 2011; Litasov, 2013; Al'tshuler, 1987; Asimow, 2009; Cazorla, 2007; Vinet, 1989). It's found that there exist great discrepancies in the melting curves between laser-heated diamond anvil cell (DAC) (Santamaría-Pérez, 2009) and shock-wave (SW) measurements (Hixson, 1992; Zhang, 2008). Errandonea (Errandonea, 2005) considered the following expression for the volume dependence of γ similar to that proposed by Burakovsky and Preston (Burakovsky, 2004):

$$\gamma = \gamma_\infty + \gamma_1 \eta^{1/3} + \gamma_2 \eta^n \quad (1)$$

where $\eta = V/V_0$, the subscript "0" and "∞" represent the corresponding zero and infinite pressure, respectively, γ_1 , γ_2 and n are constants with $n > 1$. However, the values of γ_1 , γ_2 and n proposed by Errandonea were different from those proposed by Burakovsky and Preston in Equation (1). Then the following volume dependence of melting curve (Equation (4) in Ref. (Errandonea, 2005)) is different.

$$T_m = T_{m0} \eta^{-1/3} \exp[-6\gamma_1(\eta^{1/3} - 1) - (2\gamma_2/n)(\eta^n - 1)] \quad (2)$$

Using the Lindemann law, Kushwah et al (Kushwah, 2013) had discussed curves of γ vs η and T_m vs pressure P from Equations (1) and (2) for Mo. They found that the Burakovsky–Preston approach diverges the DAC experimental melting data while the Errandonea parameters reproduce it. But γ becomes much smaller than 1 for the Errandonea approach which doesn't agree with the density functional theory performed by Zeng et al (Zeng, 2011). They then concluded that the Lindemann law doesn't work satisfactorily for the transition metals.

Litasov et al (Litasov, 2013) had discussed two other forms of γ for Mo. One is from Mie–Grüneisen–Debye (MGD) EOS, γ has the following form

$$\gamma = \gamma_0 \eta^q \quad (3)$$

Fitting Equation (3) to the MGD relation yields $q = 0.24$, which is different from the values 1.2 and 1.0 discussed by Zeng et al (Zeng, 2011). While $q=1.2$ and $q=1.0$, Equation (3) agrees with the results calculated by Zeng et al (Zeng, 2011) at low and high pressure, respectively.

The other form of γ is from Kunc–Einstein (KE) EOS (Litasov, 2013), and γ has the following form by Al'tshuler et al (Al'tshuler, 1987):

$$\gamma = \gamma_{\infty} + (\gamma_0 - \gamma_{\infty})\eta^{\beta} \quad (4)$$

where $\gamma_0, \gamma_{\infty}$ and β have different values for different models Mo-1 and Mo-2. It's found that (Litasov, 2013) the values of γ derived from the model Mo-1 seem too high, whereas the model Mo-2 yielded consistent results with shock-wave (SW) data (Asimow, 2009) and theoretical calculations (Zeng, 2011).

In summary, while discussing the Grüneisen parameter for Mo, Equations (1) and (3) don't work satisfactorily. For Equation (4), parameters such as $\gamma_0, \gamma_{\infty}$ and β in it are calculated by simultaneously weighted least-squares fitting to KE EOS (Litasov, 2013) from the available high-pressure P-V and P-V-T data, experimental data on the heat capacity, thermal expansion and adiabatic bulk modulus at zero pressure and various temperature. There are too many constants to be decided and the calculation is complicated. Therefore, it's necessary to propose a new form of γ for bcc Mo.

Here, we combined bcc melting curve with thermal equation of state and Lindemann law, and presented a new simple expression for the pressure dependence of the Grüneisen parameter γ for bcc Mo. Method of analysis is shown in Section 2, results and discussions are presented in Section 3, and conclusions are made in section 4.

2. Method of Analysis

Recently, Carzorra et al (Cazorla, 2007) yielded the bcc Mo melting curve (P in GPa, T_m in K) as follows

$$T_m = T_{m0} \left(1 + \frac{P}{a}\right)^b \quad (5)$$

where $T_{m0}=2894\text{K}$, $a=37.2\text{ GPa}$ and $b=0.43$. We noticed that Kushwah et al had compared the melting curve for Mo from the Lindemann law using the Burakovsky-Preston approach with the experimental DAC melting curve (Santamaría-Pérez, 2009). However, Belonoshko et al (Belonoshko, 2008) pointed out that the DAC melting curve of Mo at high P is essentially a bcc-solid phase boundary, and that the original interpretation of the SW data on Mo is correct. We had plotted melting curves Equation (5) and experimental SW data (Hixson, 1992; Zhang, 2008) in Fig. 1. It's found that Equation (5) fits good agreement with the experimental SW data.

Vinet et al (Vinet, 1989) demonstrated that the following two-parameter expression fits the experimental compression data for 24 different materials, including Mo, to within a few percent, over the entire experimentally attainable pressure range.

$$\frac{\Delta V}{V_0} = \frac{\ln(1 + C_2 P)}{C_1} \quad (6)$$

where $\Delta V = V_0 - V$, $C_1 = K'_0 + 1$, $C_2 = \frac{C_1}{K_0}$, K_0, K'_0 denote the bulk modulus, pressure derivative of the bulk modulus at $P=0$, respectively. For Mo, $K_0 \approx 268.5\text{ GPa}$, $K'_0 = 4$ (Kennedy, 1972).

The Lindemann melting law (Lindemann, 1910) is the widely used thermodynamic expression relating the melting temperature to the Grüneisen parameter. Different from Kushwah et al (Kushwah, 2013), we think that the Lindemann law does work for the transition metals.

$$\frac{d \ln T_m}{d \ln V} = \frac{2}{3} - 2\gamma \quad (7)$$

Combining Equations (5),(6) with (7) we get

$$\gamma = \frac{1}{3} + \frac{bK_0(1 + C_2 P)}{2(a + P)} \left[1 - \frac{1}{C_1} \ln(1 + C_2 P)\right] \quad (8)$$

3. Results and Discussions

(1) We have plotted γ versus P in Fig.2 according to the present work Equation (8). It's found that Equation (8) is in good agreement with the density functional theory (Zeng, 2011) and experiments (Hixson, 1992; Asimow, 2009). At $P = 0$, our calculated zero-pressure value of γ is 1.894, which is consistent with the value $\gamma_0 = 1.8 - 2.0$ using MGD form (Litasov, 2013). At 390GPa, we obtained $\gamma = 0.978$, agrees with the value 0.95 estimated by Hixson et al (Hixson, 1992) and 0.92 calculated by Zeng et al (Zeng, 2011).

(2) Zeng et al (Zeng, 2011) had pointed out that the relative volume (V/V_0) of bcc Mo is weakly dependent on T from $0K$ to $3500K$, γ shows very weak dependency on temperature along the isobar, but its pressure dependence is strong, and it drops quickly as pressure increases. Equation (8) yields the same results.

(3) Both the well-known Birch-Murnaghan EOS (Birch, 1978) and the Vinet EOS (Vinet, 1987) show that at extreme compression $P \rightarrow \infty$, $V \rightarrow 0$. Equation (6) obviously dissatisfied this condition. We note that for bcc Mo, the maximum pressure is 700 GPa, far below the extreme compression. Therefore, Equation (6) is just used over a given pressure range. Saxena (Saxena, 2004) had also matched Equation (6) to Birch-Murnaghan EOS or Vinet EOS for iron, gold, platinum, bismuth and periclase, the results show a good consistency.

4. Conclusions

In the present work, we presented an explicitly new expression of the pressure dependency Grüneisen parameter γ for bcc Mo while combining the melting curves with thermal equation of state and the Lindemann law. The method is simple and the results yield good agreement with density functional theory and experiments.

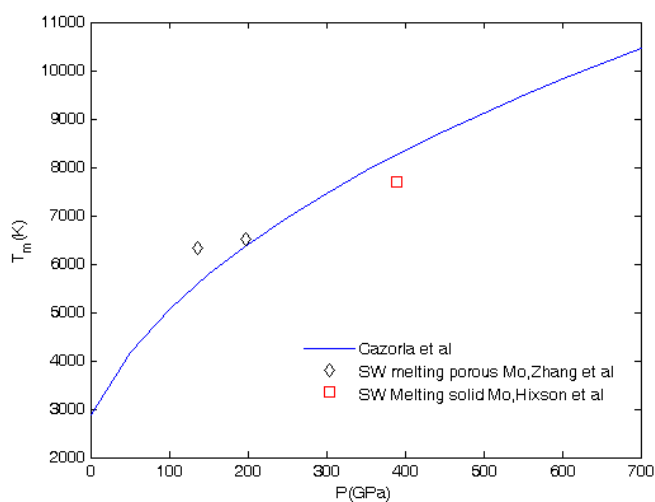


Figure 1. Melting temperature T_m versus P for bcc Mo. The solid line corresponds to Equation (5) (Cazorla et al, 2007); (\diamond) SW data by Zhang et al. (2008); (\square) SW data by Hixson and Fritz (1992)

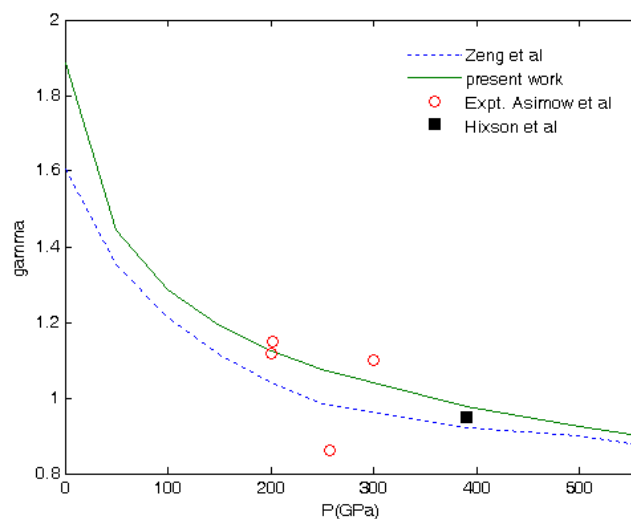


Figure 2. Variations of the Grüneisen parameter γ with pressure P . The dotted line corresponds to theoretical calculations by Zeng, Z. Y., Hu, C.E., Chen, X.R., et al. (2011). (\circ) Experimental data by Asimow, P. D., Sun D. Y. and Ahrens, T. J.. (2009). (\blacksquare) Hixson, R.S. and Fritz, J.N. (1992). Results discussed in the text Equation (8) are illustrated by the solid line

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