Molecular Dynamics Simulations on *trans*- and *cis*-Decalins: The Effect of Partial Atomic Charges and Adjustment of "Real Densities"

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Abstract

A molecular dynamics (MD) simulation of the organic compounds *trans*- and *cis*-decalin is performed with the adjustment of their experimentally observed densities. For a *trans*-decalin model system, the energy and structural properties are studied for different atomic charge distributions. The relationship between the main interaction forces (Coulombic and van der Waals) of the *trans*- and *cis*-decalin systems has been examined, and the status of the molecular forces governing the nature of the processes in the crystal or liquid phases has been established. The obtained results on the density peculiarities are interpreted in terms of a non-uniform charge distribution and van der Waals forces efficiently inhibiting the electrostatic ones. Possible applications of the obtained MD simulations results in magnetic fluid physics are discussed.

Keywords: Molecular dynamics, *trans*- and *cis*-Decalins, Van der Waals forces, Coulombic interactions

1. Introduction

Complex colloidal systems with controlled properties are currently studied in order to determine their specific structural features. Ferrofluids (FFs) are typical representatives of these systems. FFs are colloidal liquids made of nanoscale ferromagnetic or ferrimagnetic particles suspended in a carrier fluid (usually, an organic solvent or water). Their properties are close to those of the homogeneous liquids with a relatively high magnetic susceptibility (Shliomis, M. I., 1974; Rosensweig, R. E., 1985). A unique combination of such properties finds many applications in technology and engineering (Odenbach, S., 2003; Proc. of the 10th Intern. Conference on Magnetic Fluids, 2005). In recent years, possible biomedical applications of FFs have also been discussed with great interest (Fortin, J. P., 2007; Proc. of the 7th Intern. Conference on the Scientific and Clinical Applications of Magnetic Carriers, 2009). The magnetic particles are coated with a surfactant layer that prevents them from sticking together, stabilizing the whole system.

Benzene solutions of carboxylic acids (CAs), which can be used as a surfactant to produce FFs, were studied using the molecular dynamics method; and the results were compared with small-angle neutron scattering (SANS) and high-precision densitometry data. It is known that different CAs have different stabilizing abilities, which can be caused by differences in the solvent–acid interaction (Avdeev, M. V., Kholmurodov, Kh. T., Rus. J. Phys. Chem. A, 2009; Kholmurodov, Kh., Yasuoka, K., Natural Science, 2010). Decahydronaphthalene (decalin) can be used as a solvent for FFs; therefore, such interaction in this solvent is of current interest (Avdeev M. V. et al., 2011).

Decalin – a bicyclic organic compound – is an industrial solvent. It is a colorless liquid with an aromatic odor; it is used as a solvent for a number of organic compounds and polymers. Decalin exists in *cis* and *trans* isomeric forms differing only in the relative positions of the cyclic rings (Figure 1).

The *trans* form is energetically more stable. The boiling and melting points of this form are 185.5 ℃ and -31.5 ℃, respectively. Its density is 0.87 g/cm³ at 20 ℃. As for *cis*-decalin, the boiling and melting points are, respectively, 194.6 ℃ and -43.2 ℃; the density is 0.897g/cm³ at 20 ℃ (Dean, J. A., 1999). In the industry, decalin can be prepared as a mixture of different forms through the naphthalene hydrogenation in the presence of a catalyst (Donaldson, N., 1958).

The density peculiarities of *trans*- and *cis*-decalins described above are supposed to be governed by well-known intermolecular forces. First of all, the relationship between the Coulomb and van der Waals interactions can determine the nature of the processes in the *trans*- and *cis*-decalin systems in their liquid states. Recent theoretical and experimental studies show that van der Waals interactions define a number of critical effects in ion-stabilizing FFs materials (Cerda, J., 2010). On the surface of FFs nanoparticles, the charge distribution can be non-uniform, which causes the residual van der Waals interactions to be strongly dominant. In many aspects, the van der Waals interactions can inhibit the Coulomb one. The competing Coulomb and van der Waals forces in diluted FFs considerably affect the system characteristics obtained by SANS. In this work, we aimed at determining the structural and energy properties of *trans*- and *cis*-decalins. First, using the MD method, we generated various atomic charge distributions (Coulombic interactions) in *trans*-decalin. The *trans*-decalin molecule is more symmetric, and its structural data are more informative than those of the *cis*-decalin one. Next, we estimated the Lennard–Jones parameters (van der Waals potential and forces) to provide the experimentally observed densities for both *trans*- and *cis*-decalins.

2. Materials and Methods

Molecular dynamics (MD) simulations on *trans*- and *cis*-decalin structures have been performed using DL_POLY_2.18 general-purpose code (Smith, W., 1996; Smith, W., 2008; Kholmurodov, K., Smith, W., Yasuoka, K., & Ebisuzaki, T., 2000). Initially, a MD study was fulfilled on a *trans*-decalin system with the crystal structure that had been recently solved and refined with an X-ray powder diffraction technique (Eibl, S., 2009). In our present study, a *trans*-decalin model was constructed by describing each atomic position taking into account the periodic symmetry boundary conditions (Figure 2). The simulation cell consisted of a total of 700 decalin molecules. The system's spatial size was 55 x 53 x 53 angstroms (7 x 5 x 10 cells of the crystal structure). The decalin molecules were considered to be rigid units with constant bond lengths.

The temperature of the system was controlled through the Nose-Hoover (NVT) ensemble. The Verle integration algorithm for the numerical solution of the equations of motion was realized with the time step of 0.001 ps.

The intermolecular interactions were modeled with the Lennard–Jones (LJ) and Coulomb potentials (Allen, M. P., 1989):

$$U = \sum_{ij} 4\varepsilon_{ij}\left[\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12} - \left(\frac{\sigma_{ij}}{r_{ij}}\right)^{6}\right] + \frac{q_i q_j}{r_{ij}}, \tag{1}$$

where the LJ (*12-6*) potential was cut off at 8 Å of the spherical radii; the cutoff radius for the Coulomb interactions (for the charged systems) was 12 Å. For the non-identical atoms, the interaction parameters were found using the Lorentz–Berthelot mixing rule (Lorentz, H. A., 1881; Berthelot, D., 1889):

$$\sigma_{ij} = (\sigma_{ii} + \sigma_{jj})/2,$$
$$\varepsilon_{ij} = \sqrt{\varepsilon_{ii}\varepsilon_{jj}}. \tag{2}$$

As for the statistical data, graphs of the radial distribution functions (RDF) of various atomic pairs (C–C, C–H, H–H) were built at the start and end of the simulations and compared. The RDF behaviors demonstrate the differences between the phase states; in general, the RDF reflects the peculiarities of the liquid and crystal states. The RDF $g(r)$ shows the time average influence of the presence of an atom on the positions of neighboring atoms; it is proportional to the probability of finding two atoms at a distance of $r + \Delta r$ from each other (Allen, M. P., 1989).

$$\rho g(\vec{r}) = \frac{1}{N}\left\langle \sum_{i}^{N} \sum_{j \neq i}^{N} \delta[\vec{r} - \vec{r}_{ij}] \right\rangle \tag{3}$$

where N is the total number of atoms, $\rho = N/V$ is the numerical density of atoms, r_{ij} is the vector between the centers of atoms i and j, and angle brackets denote averaging over time. For distances shorter than one atomic diameter, $g(r) = 0$. At larger distances in a liquid, an atom should not influence the positions of other atoms; that is, $g(r) = 1$.

3. Results

3.1 Intermolecular structure

From the MD simulation data, we first built an RDF graph for the neutral (with zero partial atomic charges) *trans*-decalin system (Figure 3). The RDF $g(r)$ functions in Figure 3 correspond to the atomic pairs C–C, H–H, and C–H at initial and final states of the system under simulation, respectively. In Figure 3, RDF graphs are shown for the initial and relaxed final states of the *trans*-decalin system. The RDF behavior can be related to *trans*-decalin's crystal and liquid phases. From Figure 3, it is seen that the H–H pair's RDF reaches its maximum at a short distance of 1,5 Å, while the C–C pair's RDF, at 3,5 Å. The C–C pair's RDF has two maximums and a small minimum between them at 5 Å.

Next, we generated various artificial charge values in *trans*-decalin molecule (Table 2) corresponding to the C and H atoms – to describe the influence of the decalin charge distribution on the RDF behavior. The choice of the charge values in Table 2 was rather arbitrary, meeting only the molecule electroneutrality requirement. However, the distribution of the charge denoted ch-006 is close to that in real *trans*-decalin which was calculated by the ZINDO/1 semi-empirical method of quantum chemistry (Zerner, M., 1991).

The RDF results for different charge distributions described above were compared with those in Figure 3 for the neutral system. A comparison analysis shows that introducing a charge distribution like the ch-006, ch-01, ch-03, ch03, and ch04 does not almost change the RDF behavior for both crystal and liquid phases. As seen from Fig.4, starting from the ch05 and higher values, the artificial introduction of large partial charges produces visible changes in $g(r)$. This observation remains valid for all C–C, C–H, and H–H atomic pairs. Thus, in the plausible charge ranges, the RDF does not undergo any visible changes, indicating that the electrostatic interactions would not necessarily be dominant over the van der Waals ones. Only increasing the partial atomic charge up to its limit value of 1 (ch08–ch10) leads to a significant change in $g(r)$ behavior (Figure 5).

3.2 Configuration and energy profiles

In Figure 6, configuration snapshots of a *trans*-decalin system are presented for the neutral and maximum partial charge distributions (ch00 and ch10, respectively) in their final relaxed states. For the neutral system (ch00), the average density is uniform; for large partial atomic charges (ch10), the liquid density is increasingly non-uniform as strong charge interactions cause local clusterization. Thus, the fluid of *trans*-decalin molecules with the zero

charge (ch00) has a homogeneous structure; the comparison of its structural shape with the liquid in the case of a high non-zero charge (ch10) is straightforward (Figure 6: ch00 (left), ch10 (right)).

Next, we traced the evolution of the main energy characteristics of *trans*-decalin with an artificial change in the atomic charge distribution in the molecule. In Figure 7 and 8, MD simulation results are presented for the total internal and configuration energies of the system. First, it should be noted that all energy curves tend to constant levels indicating energy conservation irrespective to the charge values. An increase in the charge values leads to an increase in internal energy. Obviously, it can be explained as higher charge values generating stronger electrostatic interactions. Figure 8 shows a graph of the configuration energy of the system.

The configuration energy consists of two main components. The first one is the van der Waals interaction energy. Its behavior does not depend directly on the variation of the charge distributions up to ch05 (Figure 9). However, from the values of ch08 to ch10, the van der Waals energy curves strongly correlate with increasing the charge values. The second main component of the configuration energy is the electrostatic interaction energy (Figure 10), which underlies the fact that the partial atomic charge variations lead to an effective repulsion and attraction between the particles of the system. It is seen from Figure 10 that the electrostatic Coulomb interaction energy decreases and becomes negative with increasing a partial atomic charge. Comparing the behavior of the van der Waals and Coulomb potential energies is straightforward (Figure 9 and 10).

3.3 Adjustment of "real densities"

From the MD results presented above, we conclude that in the reasonable ranges of the partial atomic charge distributions (for example, the charge values obtained by accurate quantum chemistry calculations), the van der Waals interactions seem to be a dominant factor. The van der Waals forces can inhibit here the electrostatics ones. In other words, in the such systems (like *trans*- and *cis*-decalins), the correct description of the van der Waals potential is extremely important. In this section, MD simulation series have been performed aimed at the precise evaluation of the correct range of the LJ potential parameters for *trans*- and *cis*-decalins to ensure a good approximation of the van der Waals interaction in the system. The LJ parameters σ_H and σ_C have been measured with a NPT ensembles. The σ_H and σ_C have been multiply re-estimated in such a way that it is ensured that the densities of both *trans*- and *cis*-decalin are 0.87 and 0.897 g/cm^3, respectively – the values experimentally observed under normal conditions.

MD calculation results are summarized for *trans*- and *cis*-decalins in Figure 11 and 12, respectively, where configuration snapshots are shown along with density profiles defined through relaxations for NPT ensembles. The simulated and experimental values of the parameters σ_H and σ_C are shown in Figure 11 and 12. Crossing the MD-simulated density surfaces by the planes of the experimentally observed values (dotted lines), we find the unique and optimal LJ parameters, e.g. σ_H(sim.) = σ_H(exp.) and σ_C(sim.) = σ_C(exp.).

Thus, from Figure 11 and 12, we found the intersections of the simulated and experimental density planes, where we get the following LJ parameters: σ_H = 2.693 Å and σ_C = 3.221 Å. It should be stressed that these values deviate within an error of less than 4 % from the well-known ones, σ_H = 2.81 Å (Murad, S., 1978) and σ_C = 3.35 Å (Tildesley, D. J., 1981), which are widely used in MD simulation analysis (compare Ref. (Murad, S., 1978): σ_H = 2.81 Å and ε_H/k_B = 8.6 K; Ref. (Tildesley, D. J., 1981): σ_C = 3.35 Å and ε_C/k_B = 51.2 K, where k_B – Boltzmann's constant).

Finally, concerning LJ parameters estimation, it is well known that the parameter σ_C for carbon atom depends on its location within a molecule. As for the decalin molecule, its carbon atoms have to be sp^3-hybridized, forming a tetragonal structure with the nearest atoms. The energy potential parameter ε_C for such carbon atom is 0.06 kcal/mol. Hence, the σ_C value was estimated from the results described before. Again, MD simulations have been performed to estimate the σ_H value of both *trans*- and *cis*-decalin to make sure that the density values are the same as observed experimentally. Calculation results for the σ_H parameter are shown in Figure 13 for *trans*- and *cis*-decalin (top and bottom, respectively). From Figure 13, we found that σ_H is 2.273 Å for *trans*-decalin and 2.242 Å for *cis*-decalin. The comparison of the values σ_H = 2.273 Å and ε_C = 0.06 kcal/mol (sp^3-hybridization) with σ_H = 2.693 Å and ε_C = 0.12 kcal/mol (sp^2-hybridization) is straightforward.

4. Conclusion

This study presents molecular dynamics (MD) models simulating *trans*- and *cis*-decalin solutions. The structural, energy and potential parameters have been defined in multiple series of MD calculations. First, the radial distribution function (RDF) graphs were built for the *trans*-decalin molecule and its behavior traced depending on changes in the artificial partial atomic charge distributions in the molecule. The charge distribution in the *trans*-decalin molecule has no significant effect on the RDF of the C–C atomic pair within the reasonable charge

range (including, the charges that can be predicted using quantum chemistry techniques). The *trans*-decalin fluid corresponding to the system with zero or low partial atomic charges has a homogeneous structure – contrary to the liquid model for a higher non-zero charge distribution. The crystal–liquid transitions are reflected in the RDF behavior for various charge distributions. The relationship between the main interaction forces of the system (Coulombic and van der Waals) has been examined, and the molecular forces governing the nature of the processes in the crystal or liquid phases have been cleared up. The Lennard–Jones (LJ) potential parameters have been precisely defined to ensure the correct description of the dominant van der Waals interactions. The use of the estimated LJ parameters yields the experimentally observed values of the liquid densities of both *trans*- and *cis*-decalin. It seems to be possible to describe the effect of the appearance of differences in the dispersion ability of different CAs in decalin by the MD simulation of these solutions from the structural point of view. For this purpose, the RDF of the atoms of the acid and decalin molecules for different acids should be carefully considered.

Acknowledgments

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Table1. The parameters of the Lennard-Jones potential

	σ, Å	ε, kcal/mol
C-C	3.30	0.12
H-H	1.78	0.02

Table 2. The different charge distributions for *trans*-decalin molecule

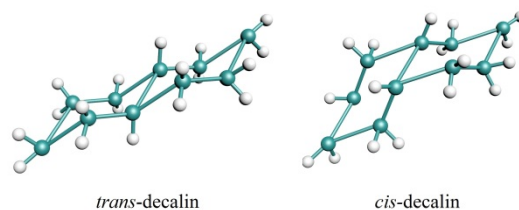| Charge	ch00	ch-006	ch-01	ch-03	ch03	ch04	ch05	ch08	ch09	ch10
C,$|e^-|$	+0.0	-0.06	-0.1	-0.3	+0.3	+0.4	+0.5	+0.8	+0.9	+1.0
H,$|e^-|$	-0.0	+0.03(3)	+0.05(5)	+0.16(6)	-0.16(6)	-0.2(2)	-0.27(7)	-0.4(4)	-0.5	-0.5(5)

trans-decalin　　　　　　*cis*-decalin

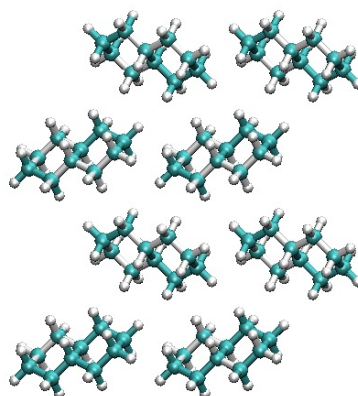Figure 1. The *trans*- and *cis*-decalin configurations

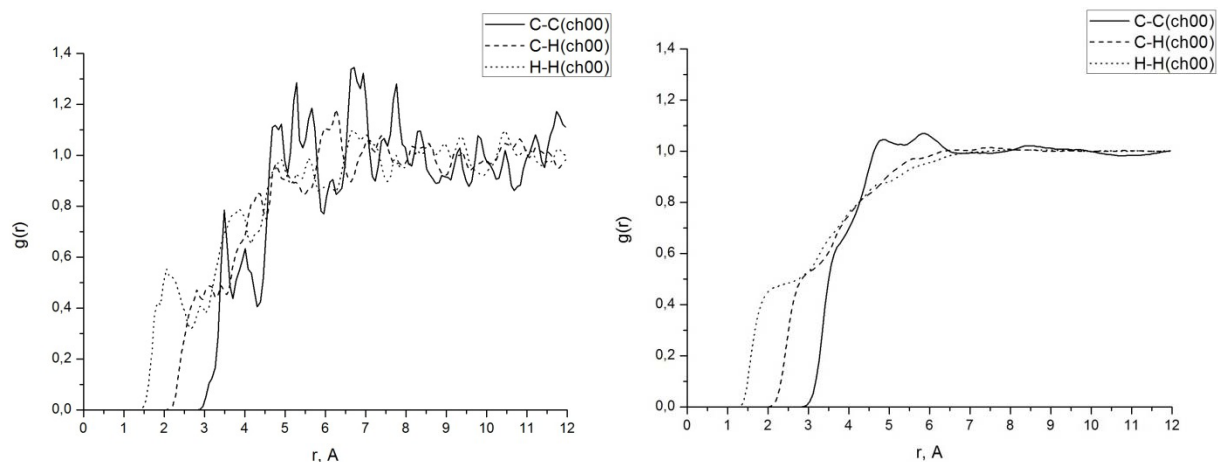Figure 2. The crystal structure of *trans*-decalin

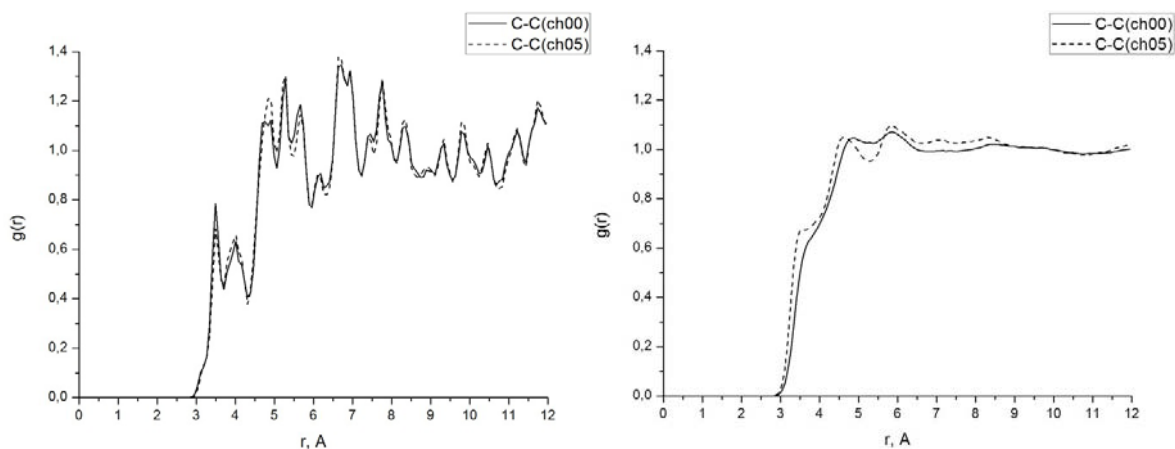Figure 3. A comparison of RDFs for C–C, C–H, and H–H atom pairs at the initial (left) and final (right) states

Figure 4. A comparison of g[C–C] at the initial (left) and final (right) states for a system with ch00 and ch05 charge distributions
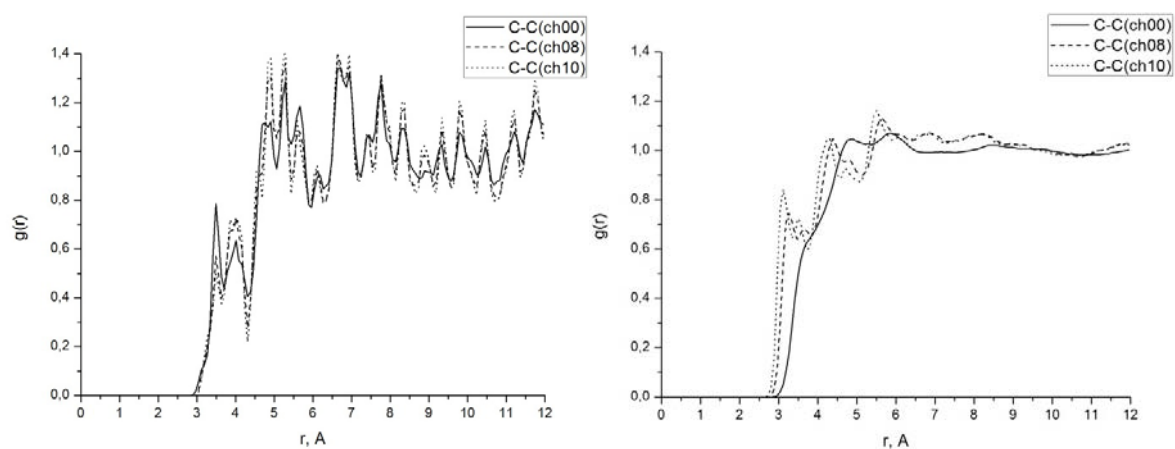

Figure 5. A comparison of g[C–C] at the initial (left) and final (right) states for a system with ch00, ch08, and ch10 charge distributions
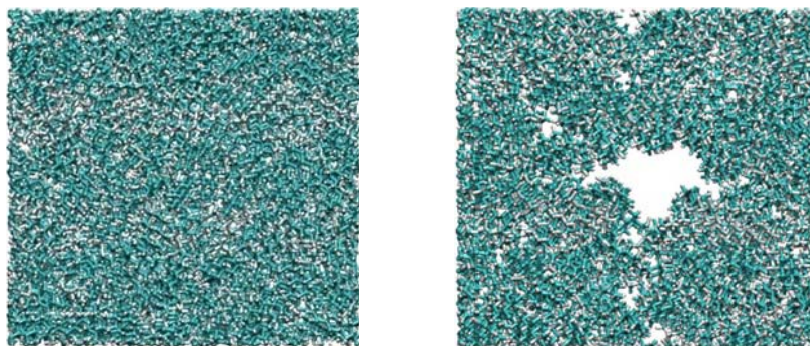
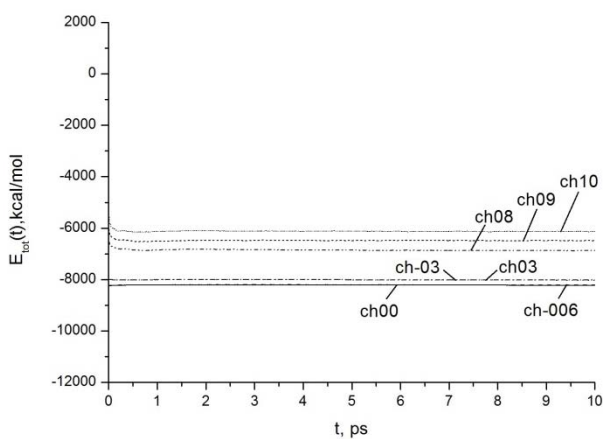Figure 6. Snapshots of the system: ch00 (1) and ch10 (2) at relaxed final states

Figure 7. The total internal energy of the system

Figure 8. The configuration energy of the system

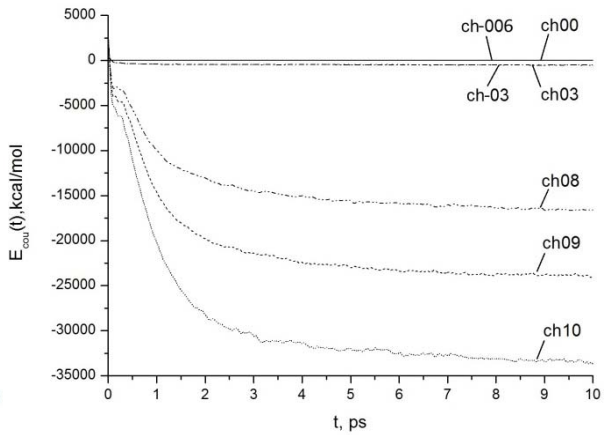Figure 9. The van der Waals interaction energy
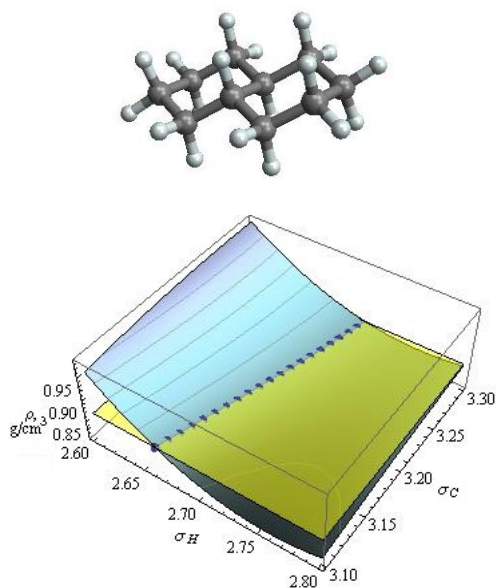

Figure 10. The electrostatic interaction energy

Figure 11. The *trans*-decalin molecule as balls and cylinders (top); the density profile after the system relaxation under normal conditions and a plane of 0.87 g/cm^3 (bottom)
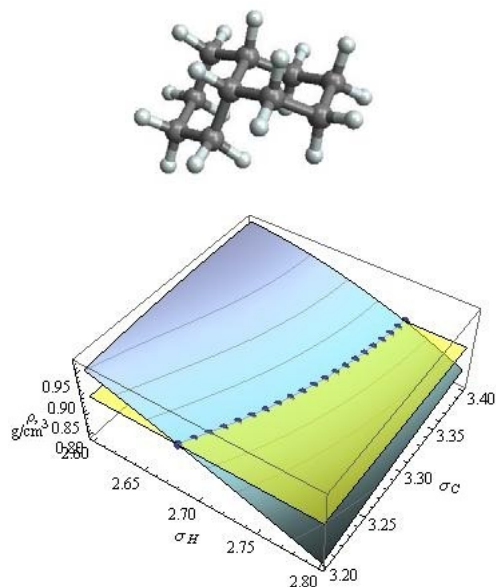

Figure 12. The *cis*-decalin molecule as balls and cylinders (top); the density profile after the system relaxation under normal conditions and a plane of 0.897 g/cm^3 (bottom)
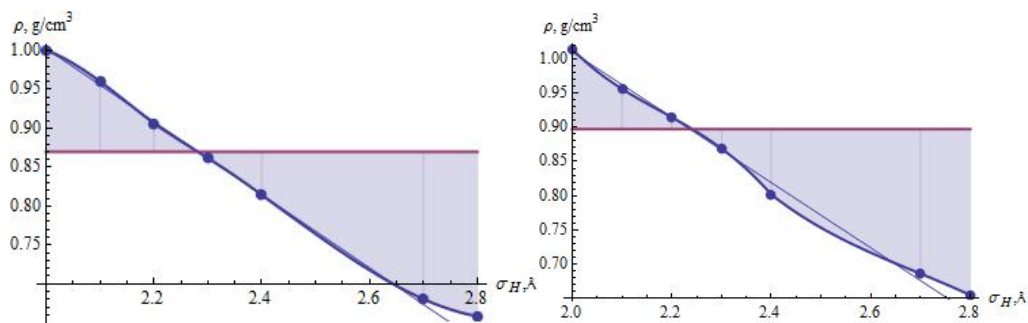

Figure 13. MD simulation results on σ_H for *trans-* (left) and *cis*-decalin (right)