

Flow-Oscillating Structure Interactions and the Applications to Propulsion and Energy Harvest

Jifeng Peng¹ & Gang Sheng Chen¹

¹Department of Mechanical Engineering, University of Alaska Fairbanks, Fairbanks, USA

Correspondence: Gang Sheng Chen, University of Alaska Fairbanks, Fairbanks, AK 99775-5905, USA. Tel: 1-907-474-5649. E-mail: gsheng@alaska.edu

Received: March 19, 2012 Accepted: April 4, 2012 Online Published: May 1, 2012

doi:10.5539/apr.v4n2p1

URL: <http://dx.doi.org/10.5539/apr.v4n2p1>

Abstract

This manuscript reviews the advance in understanding of the mechanisms of the interactions between oscillating structures and fluid flows. Many analytical, numerical and experimental approaches to model and to identify the non-stationary, nonlinear interactions between fluid flows and oscillating structures are summarized. The applications of fluid flow-oscillating structure interaction to propulsion and energy harvest are discussed. The issue of the establishment of generalized, parametric, reduced-order models is discussed with an aim at illustrating the perspectives for improving the correlation between test data and physics-based modeling.

Keywords: fluid flows, oscillating structure, interactions, propulsion, energy harvest

1. Introduction

Fluid-structure interaction occurs when fluid flow causes deformation of the structure. This deformation of a solid structure, in turn, changes the boundary condition of the fluid flow. One example is the interaction between fluid flow and an oscillating structure. Functionally many natural and engineering systems require the operation of fluid flow-oscillating structure interaction. For example, many biological and engineering systems use flapping motion of their wings/fins for propulsion. In similar principle but in an inverse way, the similar systems are used to harvest kinetic energy from the fluid motion.

It has been widely recognized that fluid flows can exert many types of forces on a structure, such as viscous force, inertia force, added mass, diffraction force, Froude-Kryloff force, lift force, wave slamming force, etc, just to name a few. Many methods has been used to investigate interactions between oscillating structures and fluid flows to uncover the underlying mechanisms, to reconstruct the coupling forces, and to model critical parameters from coupled physics phenomena.

There has been ample research dedicated to modeling of fluid flow-oscillating structure interaction, with the fluid motion described by Navier-Stokes equations and the structure modeled by elastic continuum, idealized as a rigid body, or simplified by arbitrary Lagrangian-Eulerian formulation. In engineering applications, the majority of the methods use reduced-order models that only model specific cases empirically.

Because the standard assumptions of fluid dynamics associated with most models do not adequately represent the complexity of site boundary behavior in most application cases, it is difficult to accurately model the effects of fluid forces on the non-stationary, nonlinear responses of flexible structure. Moreover, from the perspective of structural dynamics, many empirically established fluid force models have their limitations from the decoupling assumption as the fluid forces are treated as external force to structure.

Therefore, while computational fluid dynamics techniques are increasing in power and sophistication, at the time being they appear to still have a long way to go before they are capable of simulating with convincing accuracy the effect of intricate geometric details as well as structural motions and turbulence, so experimental tests are still likely to remain the most accurate tool.

This review summarizes the basic understanding on fluid flow-oscillator interaction and various models developed in the literature. The review focuses on the models used for the structure analysis in fluid flow-oscillator interaction, and their limitations are discussed. The applications of fluid flow-oscillating structure interaction to propulsion and energy harvest are also discussed.

2. Flow-oscillator Interaction

The most widely known flow oscillator interaction is flow-induced vibration. Flow-induced vibration occurs when structures perform oscillatory motion under the effect of fluid-structure interaction. Varied kinds of flow-induced vibrations such as vortex-induced vibration, flutter, galloping, and buffeting, have been widely studied and the underlying mechanisms have been gradually understood. This review focuses on two widely studied phenomena.

2.1 Vortex-induced Vibration

When a fluid flow with an intermediate and high Reynolds number passes around a structure such as a cylinder, the fluid near the structure starts to oscillate due to vortex shedding. These shedding vortices exert an oscillatory force on the structure in the direction perpendicular to both the flow and the structure. The frequency of oscillation f is related to the velocity of the incoming flow U , and the dimension of structure D by the non-dimensional Strouhal number $St = Df/U$. When the flow passes by a flexibly supported structure that is capable of performing oscillatory motion, the shedding frequency is also controlled by the movement of the structure. When the shedding frequency is close to the first natural frequency of the structure system, the oscillator takes control of the vortex shedding. The vortices will shed at the natural frequency instead of at the frequency determined by the Strouhal number. This is called lock-in or synchronization, which is a result of nonlinear interaction between the oscillation of the structure body and the action of the fluid. Vortex-induced vibration is the subject of many conventional research and surveys (e.g., Ehsan & Scanlan, 1989; Larsen, 1995; Sarpkaya, 1995; Sarpkaya, 2004; Gabbai & Benaroya, 2005; Williamson & Govardhan, 2004; El-Gammal, Hangan, & King, 2007; Williamson & Govardhan, 2008; Morse, Govardhan, & Williamson, 2008).

Vortex formation is a key feature of fluid-structure interaction at intermediate and high Reynolds numbers. A great variety of wakes can be formed by oscillating the cylinder laterally in the free stream (Williamson & Roshko, 1988; Koochesfahani, 1989; Lai & Platzer, 1999). The wakes behind the oscillating cylinder include von Kármán wakes in which two vortices of opposite sign are shed per oscillation period. In propulsion, usually the reverse von Kármán vortex streets are generated in the fluid wakes in which vortices have opposite rotational directions. Whereas the von Kármán street represents a drag wake, the reverse von Kármán wake represents thrust production (von Kármán & Burgers, 1963). As it is described (Schnipper, Andersen, & Bohr, 2009), the reverse von Kármán wakes are observed in the wakes of various flying and swimming animals and are believed to play an important role in biological locomotion (Lighthill, 1969; Sfakiotakis, Lane, & Davies, 1999; Triantafyllou, Triantafyllou, & Yue, 2000). Some animals have more complex vortex structures in their wakes (Muller, Smit, Stamhuis, & Videler, 2001; Muller, van den Boogaart, & van Leeuwen, 2008). These vortex structures can also be observed in the wakes of a flapping foil. Visualization of a variety of wakes, including von Kármán vortex street, reverse von Kármán vortex street, and other complex wake structures were studied by varying the frequency and amplitude of the oscillation of a symmetric pitching foil (Ringuette, Milano, & Gharib, 2007). More complicated three-dimensional vortex wake structures are observed behind an oscillating plate with low aspect ratio (Buchholz & Smits, 2008; Godoy-Diana, Aider, & Wesfreid, 2008).

Many efforts have been made to investigate the underlying mechanism of the vortex-induced vibration. Empirical, numerical and theoretical approaches have been used in these studies. Empirical modeling of vortex-induced vibration has been widely reported in books and articles. For many engineering applications such as vortex-induced vibration of cylinder oscillator, the empirical models can be classified into two groups: the forced decomposition model and the wake oscillator model. In forced decomposition model, fluid force is decomposed into two components, a fluid inertia force and a fluid damping force related to structure displacement and velocity, respectively. The fluid force has also been treated as an excitation part and a reaction part; the latter included all motion-dependent force components. More generally, unsteady flow theory is used, and the fluid force is assumed to be dependent on the displacement, velocity, and acceleration of the structure. In the modeling, data collected from free and forced vibration experiments was used to determine the fluid force components. In a wake-oscillator approach, a van der Pol-type equation has been developed as the governing equation of the lift force. This equation was coupled to the structure dynamic equation through one or several terms related to the structure dynamics.

For flexible structures, hydrodynamic forces from the interactions might cause deformation of the structures, leading to more complex structure responses. The vortex-induced vibration of a flexible circular cylinder has been investigated (Williamson, 1996; Khalak & Williamson, 1997a, b and 1999; Jauvtis, & Williamson, 2004; Xu, Wu, Zeng, Zhong, & Yu, 2010; Huera-Huarte & Bearman, 2011). The comprehensive flow-elastic continuum models have been simplified as reduced-order model with multiple degree-of-freedom. For example,

Zhao & Cheng investigated two-degree-of-freedom vortex-induced vibration model close to a plane boundary (Zhao & Cheng, 2011). The Reynolds-Averaged Navier-Stokes equations were solved using the Arbitrary Lagrangian Eulerian scheme with a turbulence model. Different vortex shedding modes were identified. Bearman presented a selective review of recent research on vortex-induced vibrations of isolated circular cylinders (Bearman, 2011). There have been debates about whether the flows generated by freely oscillating and forced oscillated cylinders can be the same. Controlled-vibration experiments demonstrated that under carefully controlled conditions there was a very close correspondence between these flows (Morse & Williamson, 2009). Li, Zhang, & Zhang presented a study to discuss in detail the vortex-induced vibration of a cylinder oscillator (Li, Zhang, & Zhang, 2011). The 2D incompressible Navier-Stokes equations were solved with the space-time finite element method. For the situation of low mass damping and low Reynolds, the locked in and beat phenomena were captured. The nonlinear phenomena, such as the limit cycle and bifurcation of lift coefficient and displacement, are analyzed. Another study showed the mono-frequency as well as multi-frequency vortex-induced vibration of a tensioned beam immersed in a linear shear flow and free to move in both the in-line and cross-flow directions, using direct numerical simulation (Bourguet, Lucor, & Triantafyllou, 2012). A reduced-order analytical model of nonlinear fluid-structure interactions was also developed by using the Hamilton's principle and Navier-Stokes equations (Benaroy & Gabbia, 2008; Gabbia & Benaroy, 2008). A similar study built a general low-order fluid-structure interaction model capable of evaluating the multi-mode interactions in vortex-induced vibration of flexible curved/straight structures (Srin, 2010). A conservative fourth-order central finite differencing scheme for all the viscous terms of compressible Navier-Stokes equations to simulate the vortex-induced vibration was also developed (Shen, Zha, & Chen, 2009).

There are many models for studying the interactions between flexible plates and fluid flows. A nice summary can be found in Shelley & Zhang (2010). A model was developed using a quasi-steady version of Bernoulli's equation on the flapping plate, and neglects the presence of a shed wake (Fitt & Pope, 2001). A further study (Argentina & Mahadevan, 2005) retained the effect of added mass, modeled the effect of vortex shedding from the trailing end, and avoided calculation of a velocity potential by using an analytical approximation from slender airfoil theory (Milne-Thompson, 1960). This model was adapted to study the effect of boundary conditions and investigated sound production by a flapping plate (Manela & Howe, 2009). A linearized model was developed to encompass a finite-length flag coupled to a vortex sheet (Alben, 2008). The study showed that as the rigidity of the plate is reduced, an increasing number of high spatial-frequency modes become unstable, and there is a correlation between the number of unstable linear modes and the complexity of nonlinear dynamics. A closely related approach built a simpler, but fully nonlinear model wherein the continuous vortex sheet shed by the flexible flag is replaced by the shedding of discrete point vortices with unsteady strengths (Michelin, Llewellyn-Smith, & Glover, 2008). There are other numerical models that include the viscosity of fluid. One of the most popular numerical approaches to solve flow-induced vibration is the Immersed Boundary Method (Peskin, 2002). It is a hybrid method in which the fluid is represented in an Eulerian coordinates frame and the structures in a Lagrangian coordinate frame. Forces acting on Lagrangian immersed boundary points are transformed to Eulerian fluid grids to solve the Navier-Stokes equations. The coupling is also applied to the velocity of the immersed boundary points, which is determined by fluid velocity on neighboring grid points. The method has been applied to the problem of flapping plates (Zhu & Peskin, 2002; Kim & Peskin, 2008). Another widely used hybrid computational approach integrates the Lattice Boltzmann Model (LBM) for the dynamics of incompressible viscous fluids and the Lattice Spring Model (LSM) for the mechanics of elastic solids (Masoud & Alexeev, 2010). In this approach, the two models are coupled through appropriate boundary conditions at the movable solid-fluid interface. Briefly, the LBM is a lattice method that is based on the time integration of a discretized Boltzmann equation for particle distribution functions. In three dimensions, LBM is characterized by a set of 19 distribution functions, describing the mass density of fluid particles at a lattice node and time propagating in the direction with a constant velocity. The hydrodynamic quantities are calculated as moments of the distribution functions (Succi, 2001).

2.2 Flow-induced Flutter

Another classic example of flow-induced vibrations is the flow-induced flutter (Chen, He, & Xiang, 2002; Li, Liao, & Qiang, 2003; Dowell, 2004; Paidoussis, 2004; Gu & Qin, 2004; Chen & Kareem, 2008). An everyday example of this phenomenon is the waving motion of flags in the wind. A cantilevered plate immersed in an otherwise uniform axial flow may lose stability at high enough flow velocity by flutter. It is now generally understood that the flutter of the fluid-structure system is a self-excited phenomenon. Flutter occurs as a result of the fluid-structural interaction and is usually associated with complicated phenomena such as the boundary layer interaction, flow separation, nonlinear limit cycle oscillations, etc. Flutter predictions using a 2D or 3D

Navier-Stokes model with fully coupled iteration are very challenging due to the perplexing physical phenomena and the large amount of computation work.

Plate flutter has been studied for a long time. When a cantilevered plate lies in an axial flow, it is known to exhibit self-sustained oscillations once a critical flow velocity is reached. This flutter instability has been investigated theoretically, numerically and experimentally by different studies. An early monograph on this topic was reported (Dowell, 1975). A comprehensive review is also available in the books (Dowell, 2004; Paidoussis, 2004). Flag flutter was investigated in a series of carefully conducted experiments (Taneda, 1968). Similar experiments on strip flutter was conducted to give theoretical predictions of the critical flow velocity in terms of strip thickness and length, in which the strip was modeled as a cantilevered beam (Datta & Gottenberg, 1975). The slender wing theory was used in the evaluation of the aerodynamic loads (Katz & Plotkin, 2001). Hanging strips were recently studied (Yadykin, Tenetov, & Levin, 2001). A nonlinear beam model and slender wing theory was used for the aerodynamics (Semler, Li, & Paidoussis, 1992). The latest work on strip flutter focused on the possible independence of the critical flow velocity on strip length (Lemaitre, Hemon, & de Langre, 2005). After the conventional work (Shayo, 1980), cantilevered plates in axial flow were investigated (Huang, 1995; Balint & Lucey, 2005). An analytical model using Theodorsen's theory combined with a linear beam model was developed based on experiments to predict the critical flow velocity and frequency. A linear beam model was coupled with a Navier-Stokes solver which examined the plates in axial flow with different upstream/downstream structural boundary conditions (Guo & Paidoussis, 2000). It used a linear beam model and obtained the fluid loads through a direct solution of the potential flow surrounding the plate. Cantilevered plates in axial flow were also studied. Both sets of researchers separately conducted a large number of experiments to explore the relation between the critical flow velocity and certain system parameters. In the theoretical work, they adopted a linear beam model for the structure. Studies (Yamaguchi, Yokota, & Tsujimoto, 2000; Yamaguchi, Sekiguchi, Yokota, & Tsujimoto, 2000) used a linearly varying vortex model together with a shedding wake to solve the lifting surface problem; whereas others used Theodorsen's theory (Watanabe, Suzuki, Sugihara, & Sueoka, 2002; Watanabe, Isogai, Suzuki, & Sugihara, 2002). Moreover, a study (Watanabe, Isogai, Suzuki, & Sugihara, 2002) coupled their structural model with a two-dimensional compressible Navier-Stokes solver to obtain a few reference results for their analysis. A nonlinear structural model with inextensibility condition was used to study cantilevered plates in axial flow (Tang, Yamamoto, & Dowell, 2003). They used a vortex lattice model to calculate the aerodynamic lift over the plate. This work was extended theoretically to take into account nonlinearities in the vortex lattice model (Attar, Dowell, & Tang, 2003). Experiments were conducted in water flow and predicted the flutter boundary by means of a linear beam model and the localized excitation theory (Shelley, Vandenbergh, & Zhang, 2005). Some studies dealt with the flutter of a cantilevered plate subject to axial flow on both surfaces (Tang & Paidoussis, 2007; Doare, Sauzade, & Eloy, 2011). A nonlinear equation of motion of the plate is developed using the inextensibility condition and an unsteady lumped vortex model was used to calculate the pressure difference across the plate. Both the instability and the post-critical behavior of the system were studied.

3. Applications

3.1 Propulsion

Knowledge of vortex formation and the interactions with structures is critical to understanding many natural and engineering systems ranging from how a swimming fish generates propulsive forces to how an energy harvesting device utilizes vortex formation. In the natural world, biological propulsion systems are found to have flexible structures, such as wings and fins. Both the driven and intrinsic flapping of these flexible structures are important to understanding flying and swimming (Lighthill, 1969; Childress, 1981; Vogel, 1994; Huber, 2000; Liao, Beal, Lauder, & Triantafyllou, 2003). Vortex shedding is widely present, as a means to deliver momentum into the fluid. The shedded vortices in turn cause deformation of flexible structures. The flapping motions used by flying and swimming animals are rather sophisticated and typically involve a combination of pitching and plunging motions. The effects of wing/fin flexibility on flapping fluid dynamics have been explored (e.g., Lighthill, 1960; Katz & Weihs, 1978; Long, Hale, Mchenry, & Westneat, 1996; Triantafyllou, Triantafyllou, & Yue, 2000; Yin & Luo, 2010). If the body is flexible, it is deformed by the fluid forces on it, and its motion is not prescribed but is instead determined together with that of the ambient fluid as a coupled dynamical system. These deformations are important in the locomotion of many swimming and flying organisms and are believed to improve propulsive performance. High-performance computations were used to simulate the performance of three-dimensional flexible flapping wings and found that passive flexibility can delay stall to a higher angles of attack (Lian, Shyy, Viieru, & Zhang, 2003). A three-dimensional vortex panel method was used to study the effect of span-wise flexibility on propulsion (Liu & Bose, 1997). It was found to increase propulsive efficiency

only under a carefully controlled time-dependent motion. Another used a dynamic conformal mesh to study a flexible airfoil in a heaving motion (Miao & Ho, 2006). It found that efficiency increased relative to a rigid foil for certain values of the flapping Strouhal number.

3.2 Energy Harvest

The applications of vortex-induced vibration for energy harvesting have been exploited (Meliga, Chomaz, & Gallaire, 2011; Raghavan & Bernitsas, 2011). These studies include using high-damping vortex-induced vibration to convert hydrokinetic energy from ocean/river currents to electricity. For system design, the empirical model has been used to quantify the harvested energy power and the vortex-induced vibration amplitude, lift coefficient flow velocity. The flow induced flutter also has been exploited for energy harvester. Energy transfer and the concept of flutter-mill by using cantilevered flexible plates in axial flow were discussed (Tang, Paidoussis, & Jiang, 2009). Cantilevered flexible plates in axial flow lose stability and exhibit flutter at sufficiently high flow velocity. The equations of motion of the plate are used by incorporating aero/hydrodynamic loads that are calculated using the unsteady lumped vortex model. The flow velocity is supposed to be low enough when flutter takes place for the fluid to be assumed to be incompressible. The flow can initially be considered to be inviscid; the effect of viscosity is incorporated in the drag empirically as a surface viscous force. A low-speed wind energy harvesting system was studied that transfers aerodynamically induced flutter energy into electrical energy using a flexible belt and the airflow (Fei, Mai, & Li, 2012). An electromagnetic resonator with copper coils and a permanent magnet is designed to efficiently harvest electrical energy from the induced mechanical vibrations. Different groups of springs are compared at various wind conditions to maximize the power output. The energy harvested from the flutter of a plate in an axial flow by making use of piezoelectric materials was demonstrated (Doare & Michelin, 2012). The equations for fully coupled linear dynamics of the fluid-solid and electrical systems are derived.

4. Previous Models and Their Limitations

How to efficiently predict flow-induced vibrations of structures with reliable accuracy remains largely a difficult task. The oscillation of a structure interacting with fluid flow is an inherently nonlinear, self-regulated, continuum elasticity phenomenon. Vortex shedding gives rise to complex forces. This is only one of the factors that make vortex-induced vibration prediction in industrial applications far from a standard procedure.

Direct numerical simulations of flow-oscillator interaction solve the Navier-Stokes equations for the fluid around the structure and compute the hydrodynamic loads on it. Empirical models, on the other hand, apply hydrodynamic coefficients or aero-elastic coefficients to represent the fluid forces on the structure. A popular empirical approach is to use phenomenological model or reduced-order model, which is combined with analytical considerations and able to reveal the underlying physical nature. The reduced-order model possesses original kernel of van der Pol or Rayleigh equation. Because of its significant applications, the reduced-order models have been extensively developed.

The reduced-order models of multiple-degree-of-freedom with van der Pol-type equations have been widely used in engineering to investigate vortex-induced vibration (Marra, Mannini, & Bartoli, 2011). A typical case of using multiple-degree-of-freedom reduced-order model is given (Violette, de Langre, & Szydlowski, 2010), in which the motion induced by vortex shedding on slender flexible structures subjected to cross-flow was studied. Vortex-induced vibration was analyzed by considering the linear stability of a coupled system that includes the structure dynamics and the wake dynamics. The latter was modeled by a continuum of wake oscillators, distributed along the span of the structure under the assumption of uniform or non-uniform flows.

The description of vortex-induced vibration using reduced-order model requires that one weighs the relative magnitudes of each of the model parameters and then tries to predict their contribution to the structural response. Part of the problem is that different models for vortex-induced vibration give different results. As an example, a study once found large discrepancies in the predicted response of slender marine structures to vortex shedding when seven different models were applied to the same structures under the same environmental conditions (Larsen & Halse, 1997). Some of these discrepancies can be attributed to the fact that many of these models use experimentally obtained values for the flow inputs. This approach remains hindered by the fact that Reynolds numbers of most industrial applications cannot be simulated. Moreover, the existing empirical models are limited in their applications because they are not able to predict the response oscillation amplitude for values of the mass and damping away from those at which their aero-elastic parameters were estimated.

Three different types of coupling effects (displacement, velocity and acceleration) of the cylinder structure movement on the lift fluctuation were investigated (Facchinetti, Delangre, & Biolley, 2004). It was found that by the displacement and velocity couplings only, one fails to predict the lift phase observed in

experiments of vortex shedding from cylinders that were forced to oscillate. By the displacement coupling alone, the lift magnification at lock-in and almost all important features of vortex-induced vibrations at low values of the Skop Griffin parameter cannot be predicted, while by the velocity coupling alone, the range of lock-in for low values of cannot be determined.

General reduced-order, analytical models of nonlinear flow-oscillator interactions were developed by using Hamilton's variational formulation coupling Navier-Stokes equations (Benaroy & Gabbai, 2008; Gabbai & Benaroy, 2008). Many wake-body models are shown to be recoverable from the more general model derived by explicit assumptions. However, this general model still suffers from unifying failure to unify some cases, such as relatively larger dissipations due to the inherent limit of Hamilton's principle, as tools for approximation analysis.

Despite the research dedicated to vortex-induced vibration, and the resulting development of qualitative understanding, the realization of techniques for accurate prediction of structure response has been scarce. This is mainly because these models were based on limited empirical results with many assumptions. Most of the research is confined to linear system parameter identification due to the complexity of the problems. In a study, the nonlinear motion equilibrium between the flow-induced excitation forces and the structural dynamics was estimated and characterized by varying amplitude and phase along the structure, which were complex modes, mixtures of traveling and standing waves (Lucora, Mukundanb, & Triantafyll, 2006). This could provide some insight to characterize structure motion pattern, but it cannot quantify system parameters. A linear instability theory and identification approach was developed (Violette, de Langrea, & Szydlowski, 2010), which could be used to efficiently estimate the threshold of instability, but it cannot predict nonlinear response of system. The linear modal identification of steel riser under sheared current was investigated by employing a combination of signal filtering and least-squares fitting (Lie & Kaasen, 2006) and another study (Allan, 1995) used analysis-experiments response match approach to identify the parameters in van der Pol oscillator of single-degree-of-freedom. The direct response match approach suffers from the shortcoming of unreliability. The direct response match approach is sensitive to certain parameters and it may lead to multiple solutions. Response match method is also used to identify system parameters (Wun & Chang, 2011).

There were numerous researches on the flow-induced flutter. Conventionally, most flutter models were linear, focusing on instability threshold determination. For example, the nonlinear higher order harmonics appeared in the experiments of an aero-elastic energy harvester in aerodynamic flows (Dunnmon, Stanton, Mann, & Dowell, 2012), which are not represented in by linear models.

Determining flutter models for use in design simulators requires the model to be valid over a wide range of testing data for design conditions. There are many research projects dedicated to the identification of flutter parameters, flutter derivatives or the linear aerodynamic stiffness and damping (e.g., Brownjohn & Bogunovic, 2001; Chen, He, & Xiang, 2002; Gu & Qin, 2004; Chen & Kareem, 2008; Perez & Fossen, 2009). Flutter derivatives and aerodynamic admittances provide a basis for predicting the critical flow speed in flutter analysis. But almost all of the research is confined to linear system parameter identification. For example, in a recent work (Chen, Han, Luo, & Hua, 2010), the equations are formulated about mass center of the system using the Lagrangian approach. The subsection extended-order iterative least square algorithm was developed in the state space for direct identification of system matrices from free vibration data of a model obtained from wind tunnel experiments. The flutter derivatives were extracted straightforwardly from the difference in the system matrices identified at zero wind velocity and at a specific wind velocity, respectively. By making use of complex modal decomposition technique, a procedure was employed to correct the system matrix at zero wind velocity considering both eccentricities. Only recent work used local model networks approach to identify flutter derivatives with nonlinearity (Seher-Weiss, 2011). The author built a global model through a weighted superposition of local simple models. The location of the local is determined automatically as part of the algorithm. This approach allows to identify influencing parameters for locate nonlinearities. The shortcoming of this approach is that the globally valid model is needed.

The modeling of the nonlinear response of structures for given excitation forces is a matured mechanical engineering problem, which can be solved using finite element method or even semi-analytical solution. But the inverse problem, the force and boundary conditions identification through response, has been a challenging one. The advances of modern nonlinear dynamics identification techniques offer many opportunities to implement response-based system identification. The identification of nonlinear dynamics through the use of experimental data has received considerable attention (e.g., Huang et al., 1998; Krauss & Nayfeh, 1999; Yasuda & Kamiya, 1999; Nelles, 2002). Many nonlinear identification methods have been proposed, which include: Volterra and Wiener series, spectral analysis and the reverse-path formulation, nonlinear auto-regressive moving

average models, the restoring force method, the describing function methods, direct parameter estimation, Hilbert transforms, wavelet transforms and neural networks, etc. A comprehensive review of nonlinear identification of structural dynamics can be found (Worden & Tomlinson, 2001). The most commonly used nonparametric methods include the higher order frequency response function method, and the restoring force-surface or force-state mapping method. Most of the parametric identification methods are time-domain based, which have the advantages of requiring less time and effort for data acquisition than some frequency-domain techniques and being suitable for the identification of strongly nonlinear systems. Frequency-domain techniques avoid the efforts of differentiation and observability of small terms, but require more theoretical effort and are generally applicable to weak nonlinear systems. Conventionally, Fourier analysis based FFT, power spectrum density (PSD), time-frequency analysis (TFA), and wavelet transformation (WT) have been used to characterize vibration signal. Due to the fundamental assumption of linearity in Fourier analysis, FFT, PSD and TFA are not suitable to deal with non-stationary and nonlinear signal in principle. The wavelet methods may also prove inadequate because its non-locally adaptive approach causes leakage. In the last decade, Hilbert-Huang transform (HHT) has been well developed for processing non-linear and non-stationary signals, which could be used to effectively process non-stationary, nonlinear vibration signals and pinpoint dynamics features through its two elements, empirical mode decomposition (EMD) and Hilbert spectral analysis (Huang et al., 1998; Huang & Attoh-Okine, 2005). In dealing with dynamics of fluid-structure interaction system, on one hand, all of the existing simulations have used nonlinear physics models with some assumed or empirical parameters. The existing modeling and simulation research had qualitatively characterized the nonstationary, nonlinear dynamics of the system, based conventional models and parameters that were established or extrapolated from experimentally observed fluid mechanics phenomena and structure phenomena under specific tested conditions with specific scale. However, there has been a lack of detailed and direct validation of the models and simulated results by using experimental results. In the conventional modeling, the integration of empirical model and numerical simulation and testing have been used. But the contemporary nonlinear science identification technology has not been applied. Moreover, all of the experimental investigations have used FFT (Bourguet, Lucor, & Triantafyllou, 2012), PSD, TFA (Hangana, Koppa, Vernetb, & Martinuzzi, 2001), or WT (Wanga, Soa, & Xie, 2007; Lewalle, 2010) to process flow/structure vibration signals from measured data. This is not proper as the responses of flow-induced vibrations are usually non-stationary and strong nonlinear. Therefore, the further work on experiment-based identification is highly needed to quantify real system and to identify or “calibrate” key parameters in reduced-order model, so as to obtain validated, generalized reduced-order model for design simulator.

In addition to the above-mentioned problems, the conventional reduced-order models have many other shortcomings. For example, it was found that the traditional labels of “high mass-damping” and “low mass-damping” are incomplete with regard to predicting a large or small-amplitude response profile in certain situations (Klamo, Leonard, & Roshko, 2006). Also, the damping due to fluid interaction has been found to be frequency dependent. But this has not been addressed by existing models (e.g. Zhang, Zhou, So, Mignolet, & Wang, 2003), though the accurate modeling of damping is of crucial importance for the prediction of response amplitude. It was illustrated that flow-oscillator model must be improved properly by including the effect of frequency dependent coupling; otherwise the model of wake oscillator with a van der Pol equation cannot accurately model the results of vortex-induced vibration measurements (Ogink & Metrikine, 2010).

5. Further Study and Conclusive Remarks

New, transformative flow-oscillator models require that different types of oscillating structures can be efficiently and effectively analyzed for their fluid-structure interactions without phenomenological assumptions. Studies should focus on understanding the underlying mechanism of fluid flow-oscillating structure interaction by exploring new methodology to model and identify system, aiming to better quantify the coupled nature of fluid-structure that may lead to instability of systems; to model the effect of nonlinear fluid damping and stiffness on the response and stability of oscillating structure.

A feasible methodology to improve the existing empirical models is to establish generalized reduced-order models by directly using physics with the assistance of fluid-structure numerical analysis under standard assumptions. Further flow-oscillator models need to include the fundamental presence of non-stationary and strong nonlinear vibrations of structure with parameter/frequency-dependent stiffness and damping mechanism. To develop new models, one approach is to integrate theories in oscillatory structure and fluid dynamics to establish generalized reduced-order models through parametric Hamilton's Law, so as to comprehensively unify existing models. The generalized reduced-order models should be able to unify existing models and consist of undetermined parameters which could be calibrated for special applications. The test-based nonlinear system identification technique can be used to calibrate these parameters so as to attain validated

generalized reduced-order models. After the models are established, it is necessary to use nonlinear system identification methodologies, based on experimental data, to identify the undetermined parameters in the models to substantially improve the fidelity. This in-situ calibrating could use criteria such as higher order frequency response functions, Hilbert transform, bifurcation diagrams, phase portraits and Lyapunov exponents.

The following questions need to be answered to develop generalized reduced-order models:

- What is the most feasible and effective approach to establish generalized, parametric, reduced-order models to unify existing models? How can we substantially improve the fidelity of the models by parameter identification through tested data or through comprehensive numerical analysis results?
- How can we effectively characterize the non-stationary and nonlinear dynamics of fluid-structure interaction from recorded response signal and flow field data? What is the general spectral signature beyond Fourier transform format? How does the spectral signature vary with respect to interface parameters' changes?
- How can we extract coupling dynamics and interaction information and re-construct coupling forces with high time and frequency resolution from tested response signals? How can we effectively synthesize model parameters based on identification? Does the vortex-induced vibration or flutter have one-on-one relationship in terms of its output and input for all cases?
- How can we make use of the direct numerical simulation to identify the generalized reduced-order model, under the situation that experimental data is not available? If we have had validated, generalized reduced-order models from experiment-based identification, how can we make use of it to improve direct numerical simulation by developing higher performance scheme or improving boundary assumptions?
- How can we make use of the identified models for prediction and optimal design? How can we make use of the identification technique to develop in-situ calibration technique for other empirical models or reduced-order models?

Obviously, the general approaches should be developed and unified to advance the analytical models for the complex fluid-structure interaction problems that are present in many engineering designs, providing also a fundamental tool for a better understanding of the underlying physics. This would yield validated, generalized reduced-order models that can be used for optimization of oscillatory structure in fluid flows for locomotion propulsion or energy-harvesting devices with exceptional efficiency.

Reference

- Alben, S. (2008). Optimal flexibility of a flapping appendage in an inviscid fluid. *Journal of Fluid Mechanics*, 614, 355-380. <http://dx.doi.org/10.1017/S0022112008003297>
- Allan, L. (1995). A generalized model for assessment of vortex-induced vibrations of flexible structures. *Journal of Wind Engineering and Industrial Aerodynamics*, 57, 281-294. [http://dx.doi.org/10.1016/0167-6105\(95\)00008-F](http://dx.doi.org/10.1016/0167-6105(95)00008-F)
- Argentina, M., & Mahadevan, L. (2005). Fluid-flow-induced flutter of a flag. *Proceedings of National Academy of Science*, 102, 1829-34. <http://dx.doi.org/10.1073/pnas.0408383102>
- Attar, P. J., Dowell, E. H., & Tang, D. M. (2003). Modeling aerodynamic nonlinearity for two aeroelastic configurations: delta wing and flapping flag, Proceedings of the 44th AIAA/ASME/ASCE/AHS Structures, Dynamics, and Materials Conference, 7-10, April, Norfolk, VA, 1-12.
- Balint, T., & Lucey, A. D. (2005). Instability of a cantilevered flexible plate in viscous channel flow. *Journal of Fluids and Structures*, 20, 893-912. <http://dx.doi.org/10.1016/j.jfluidstructs.2005.05.005>
- Bearman, P. W. (2011). Circular cylinder wakes and VIV. *Journal of Fluids and Structures*, 27, 648-658. <http://dx.doi.org/10.1016/j.jfluidstructs.2011.03.021>
- Benaroy, H., & Gabbai, R. D. (2008). Modelling vortex-induced fluid-structure interaction. *Transaction of Royal Society A*, 366, 1231-1274. <http://dx.doi.org/10.1098/rsta.2007.2130>
- Bourguet, R., Lucor, D., & Triantafyllou, M. (2012). Mono- and multi-frequency vortex-induced vibrations of along tensioned beam in shear flow. *Journal of Fluids and Structures*. In Press.
- Brownjohn, J. M. W., & Bogunovic, J. (2001). Strategies for aeroelastic parameter identification from bridge deck free vibration data. *Journal of Wind Engineering and Industrial Aerodynamics*, 89, 1113-1136. [http://dx.doi.org/10.1016/S0167-6105\(01\)00091-5](http://dx.doi.org/10.1016/S0167-6105(01)00091-5)

- Buchholz, J. H. J., & Smits, A. J. (2008). The wake structure and thrust performance of a rigid low-aspect-ratio pitching panel. *Journal of Fluid Mechanics*, 603, 331-365. <http://dx.doi.org/10.1017/S0022112008000906>
- Chen, Z. Q., Han, Y., Luo, Y. Z., & Hua, X. G. (2010). Identification of aerodynamic parameters for eccentric bridge section model. *Journal of Wind Engineering and Industrial Aerodynamics*, 98, 202-214. <http://dx.doi.org/10.1016/j.jweia.2009.10.016>
- Chen, X. Z., & Kareem, A. (2008). Identification of critical structural modes and flutter derivatives for predicting coupled bridge flutter. *Journal of Wind Engineering and Industrial Aerodynamics*, 96, 1856-1867. <http://dx.doi.org/10.1016/j.jweia.2008.02.025>
- Chen, A. R., He, X. F., & Xiang, H. F. (2002). Identification of 18 flutter derivatives of bridge decks. *Journal of Wind Engineering and Industrial Aerodynamics*, 90, 2007-2022. [http://dx.doi.org/10.1016/S0167-6105\(02\)00317-3](http://dx.doi.org/10.1016/S0167-6105(02)00317-3)
- Childress, S. (1981). *Mechanics of Swimming and Flying*. Cambridge University Press. <http://dx.doi.org/10.1017/CBO9780511569593>
- Chowdhury, A. G., & Sarkar, P. P. (2003). A new technique for Identification of eighteen flutter derivatives using a three-degree-of-freedom section model. *Engineering Structures*, 25, 1763-1772. <http://dx.doi.org/10.1016/j.engstruct.2003.07.002>
- Datta, S. K., & Gottenberg, W. G. (1975). Instability of an elastic strip hanging in an airstream. *Journal of Applied Mechanics*, 42, 195-198. <http://dx.doi.org/10.1115/1.3423515>
- Doare, O., & Michelin, S. (2012). Piezoelectric coupling in energy-harvesting fluttering flexible plates: linear stability analysis and conversion efficiency. *Journal of Fluids and Structures*. In Press.
- Doare, O., Sauzade, M., & Eloy, C. (2011). Flutter of an elastic plate in a channel flow: Confinement and finite-size effects. *Journal of Fluids and Structures*, 27, 76-88. <http://dx.doi.org/10.1016/j.jfluidstructs.2010.09.002>
- Dowell, E. H. (2004). *A Modern Course in Aeroelasticity*, fourth ed. Kluwer Academic Publishers, Boston.
- Dowell, E. H. (1975). *Aeroelasticity of Plates and Shells* (1st ed.). Noordhoff International Publishing, Leyden.
- Dunnmon, J. A., Stanton, S. C., Mann, B. P., & Dowell, E. H. (2012). Power extraction from aeroelastic limit cycle oscillations. *Journal of Fluids and Structures*. In press.
- Ehsan, F., & Scanlan, R. H. (1989). Vortex-induced vibrations of flexible ridges. *ASCE Journal of Engineering Mechanics*, 116(15), 1392-1411.
- El-Gammal, M., Hangan, H., & King, P. (2007). Control of vortex shedding-induced effects in a sectional bridge model by spanwise perturbation method. *Journal of Wind Engineering and Industrial Aerodynamics*, 95, 663-678. <http://dx.doi.org/10.1016/j.jweia.2007.01.006>
- Facchinetti, M. L., Delangre, E., & Biolley, F. (2004). Coupling of structure and wake oscillators in vortex-induced vibrations. *Journal of Fluids and Structures*, 19, 123-140. <http://dx.doi.org/10.1016/j.jfluidstructs.2003.12.004>
- Fei, F., Mai, J. D., & Li, W. J. (2011). A Wind-flutter energy converter for powering wireless sensors. *Sensors and Actuators A*, 21, 76-88. <http://dx.doi.org/10.1016/j.sna.2011.06.015>
- Fitt, A., & Pope, M. (2001). The unsteady motion of two-dimensional flags with bending stiffness. *Journal of Engineering Mathematics*, 40, 227-248. <http://dx.doi.org/10.1023/A:1017595632666>
- Gabbaia, R. D., & Benaroy, H. (2008). A first-principles derivation procedure for wake-body models in vortex-induced vibration: Proof-of-concept. *Journal of Sound and Vibration*, 312, 19-38. <http://dx.doi.org/10.1016/j.jsv.2007.07.086>
- Gabbaia, R. D., & Benaroya, H. (2005). An overview of modeling and experiments of vortex-induced vibration of circular cylinders. *Journal of Sound and Vibration*, 282, 575-616. <http://dx.doi.org/10.1016/j.jsv.2004.04.017>
- Godoy-Diana, R., Aider, J. L., & Wesfreid, J. E. (2008). Transitions in the wake of a flapping foil. *Physics Review E*, 77, 016308. <http://dx.doi.org/10.1103/PhysRevE.77.016308>
- Gu, M., & Qin, X. R. (2004). Direct Identification of flutter derivatives and aerodynamic admittances of bridge decks. *Engineering Structures*, 26, 2161-2172. <http://dx.doi.org/10.1016/j.engstruct.2004.07.015>

- Guo, C. Q., & Paidoussis, M. P. (2000). Stability of rectangular plates with free side-edges in two-dimensional inviscid flow. *Journal of Applied Mechanics*, 67, 171-176. <http://dx.doi.org/10.1115/1.321143>
- Hangana, H., Koppa, G. A., Vernetb, A. R., & Martinuzzi, A. (2001). A wavelet pattern recognition technique for identifying flow structures in cylinder generated wakes. *Journal of Wind Engineering and Industrial Aerodynamics*, 89, 1001-1015. [http://dx.doi.org/10.1016/S0167-6105\(01\)00095-2](http://dx.doi.org/10.1016/S0167-6105(01)00095-2)
- Huang, N. E., & Attoh-Okine, N. O. (2005). *The Hilbert-Huang Transform in Engineering*, CRC Press. <http://dx.doi.org/10.1201/9781420027532>
- Huang, N. E., Shen, Z., Long, S. R., Wu, M. C., Shih, H. H., Zheng, Q., Yuen, N. C., Tung, C. C., & Liu, H. H. (1998). The empirical mode decomposition and the Hilbert spectrum for nonlinear and non-stationary timeseries analysis. *Proceedings of the Royal Society of London*, 454, 903-995. <http://dx.doi.org/10.1098/rspa.1998.0193>
- Huang, L. X. (1995). Flutter of cantilevered plates in axial flow. *Journal of Fluids and Structures*, 9, 127-147. <http://dx.doi.org/10.1006/jfls.1995.1007>
- Huber, G. (2000). Swimming in Flatsea. *Nature*, 408, 777-778. <http://dx.doi.org/10.1038/35048643>
- Huera-Huarte, F. J., & Bearman, P. W. (2011). Vortex and wake-induced vibrations of a tandem arrangement of two flexible circular cylinders with near wake interference. *Journal of Fluids and Structures*, 27, 193-211. <http://dx.doi.org/10.1016/j.jfluidstructs.2010.11.004>
- Jauvtis, N., & Williamson, C. H. K. (2004). The effect of two degrees of freedom on vortex-induced vibration at low mass and damping. *Journal of Fluid Mechanics*, 509, 23-62. <http://dx.doi.org/10.1017/S0022112004008778>
- Katz, J., & Plotkin, A. (2001). *Low-Speed Aerodynamics* (2nd ed.). Cambridge University Press, New York.
- Katz, J., & Weihs, D. (1978). Hydrodynamic propulsion by large amplitude oscillation of an airfoil with chordwise flexibility. *Journal of Fluid Mechanics*, 88, 485-497. <http://dx.doi.org/10.1017/S0022112078002220>
- Khalak, A., & Williamson, C. H. K. (1999). Motions, forces and mode transitions in vortex-induced vibrations at low mass-damping. *Journal of Fluids and Structures*, 13, 813-851. <http://dx.doi.org/10.1006/jfls.1999.0236>
- Khalak, A., & Williamson, C. H. K. (1997a). Fluid forces and dynamics of a hydroelastic structure with very low mass and damping. *Journal of Fluids and Structures*, 11(8), 973-982. <http://dx.doi.org/10.1006/jfls.1997.0110>
- Khalak, A., & Williamson, C. H. K. (1997b). Investigation of relative effects of mass and damping in vortex-induced vibration of a circular cylinder. *Journal of Wind Engineering and Industrial Aerodynamics*, 69, 341-350. [http://dx.doi.org/10.1016/S0167-6105\(97\)00167-0](http://dx.doi.org/10.1016/S0167-6105(97)00167-0)
- Kim, Y., & Peskin, C. (2008). Penalty immersed boundary method for an elastic boundary with mass. *Physics of Fluids*, 19, 053103. <http://dx.doi.org/10.1063/1.2734674>
- Klamo, J. T., Leonard, A., & Roshko, A. (2006). The effects of damping on the amplitude and frequency response of a freely vibrating cylinder in cross-flow. *Journal of Fluids and Structures*, 22, 845-856. <http://dx.doi.org/10.1016/j.jfluidstructs.2006.04.009>
- Koochesfahani, M. M. (1989). Vortical patterns in the wake of an oscillating airfoil. *AIAA Journal*, 27, 1200-1205. <http://dx.doi.org/10.2514/3.10246>
- Krauss, R. W., & Nayfeh, A. H. (1999). Experimental nonlinear identification of a single mode of a transversely excited beam. *Nonlinear Dynamics*, 18, 69-87. <http://dx.doi.org/10.1023/A:1008355929526>
- Lai, J. C. S., & Platzer, M. F. (1999). Jet characteristics of a plunging airfoil. *AIAA Journal*, 37, 1529-1537. <http://dx.doi.org/10.2514/2.641>
- Larse, C. M., & Halse, K. H. (1997). Comparison of models for vortex induced vibrations of marine structures. *Marine Structures*, 10, 413-441. [http://dx.doi.org/10.1016/S0951-8339\(97\)00011-7](http://dx.doi.org/10.1016/S0951-8339(97)00011-7)
- Larsen, A. (1995). A generalized model for assessment of vortex-induced vibrations of flexible structures. *Journal of Wind Engineering and Industrial Aerodynamics*, 57, 281-294. [http://dx.doi.org/10.1016/0167-6105\(95\)00008-F](http://dx.doi.org/10.1016/0167-6105(95)00008-F)

- Lemaitre, C., Hemon, P., & de Langre, E. (2005). Instability of a long ribbon hanging in axial air flow. *Journal of Fluids and Structures*, 20, 913-925. <http://dx.doi.org/10.1016/j.jfluidstructs.2005.04.009>
- Lewalle, J. (2010). Single-scale wavelet representation of turbulence dynamics: Formulation and Navier-Stokesregularity. *Physica D*, 239, 1232-1235. <http://dx.doi.org/10.1016/j.physd.2009.10.009>
- Li, T., Zhang, J., & Zhang, W. H. (2011). Nonlinear characteristics of VIV at low Reynolds number. *Communications in Nonlinear Science and Numerical Simulation*, 16(7), 2753-2771. <http://dx.doi.org/10.1016/j.cnsns.2010.10.014>
- Li, Y. L., Liao, H. I., & Qiang, S. Z. (2003). Weighting ensemble least-square method for flutter derivatives of bridge decks. *Journal of Wind Engineering and Industrial Aerodynamics*, 91(6), 713-721. [http://dx.doi.org/10.1016/S0167-6105\(03\)00002-3](http://dx.doi.org/10.1016/S0167-6105(03)00002-3)
- Lian, Y., Shyy, W., Viieru, D., & Zhang, B. (2003). Membrane wing aerodynamics for micro air vehicles. *Progress in Aerospace Science*, 39, 425-465. [http://dx.doi.org/10.1016/S0376-0421\(03\)00076-9](http://dx.doi.org/10.1016/S0376-0421(03)00076-9)
- Liao, J. C., Beal, D. N., Lauder, G. V., & Triantafyllou, M. S. (2003). Fish exploiting vortices decrease muscle activity. *Science*, 302, 1566-1569. <http://dx.doi.org/10.1126/science.1088295>
- Lie, H., & Kaasen, K. E. (2006). Modal analysis of measurements from a large-scale VIV model test of a riser in linearly sheared flow. *Journal of Fluids and Structures*, 22, 557-575. <http://dx.doi.org/10.1016/j.jfluidstructs.2006.01.002>
- Lighthill, M. J. (1969). Hydromechanics of aquatic animal propulsion. *Annual Review of Fluid Mechanics*, 1, 413-446. <http://dx.doi.org/10.1146/annurev.fl.01.010169.002213>
- Liu, P., & Bose, N. (1997). Propulsive performance from oscillating propulsors with spanwise flexibility. *Proceedings of the Royal Society of London A*, 453, 1763-1770. <http://dx.doi.org/10.1098/rspa.1997.0095>
- Long, J., Hale, M., Mchenry, M., & Westneat, M. (1996). Functions of fish skin: flexural stiffness and steady swimming of longnose gar, *Lepisosteus osseus*. *Journal of Experimental Biology*, 199, 2139-2151.
- Lucora, D., Mukundanb, H., & Triantafyll, M. S. (2006). Riser modal identification in CFD and full-scale experiments. *Journal of Fluids and Structures*, 22, 905-917. <http://dx.doi.org/10.1016/j.jfluidstructs.2006.04.006>
- Manela, A., & Howe, M. S. (2009). The forced motion of a flag. *Journal of Fluid Mechanics*, 635, 439-454. <http://dx.doi.org/10.1017/S0022112009007770>
- Marra, A. M., Mannini, C., & Bartoli, G. (2011). Van der Pol-type equation for modeling vortex-induced oscillations of bridge decks. *Journal of Wind Engineering and Industrial Aerodynamics*, 99, 776-785. <http://dx.doi.org/10.1016/j.jweia.2011.03.014>
- Masoud, H., & Alexeev, A. (2010). Resonance of flexible flapping wings at low Reynolds number. *Physics Review E*, 81, 056304. <http://dx.doi.org/10.1103/PhysRevE.81.056304>
- Meliga, P., Chomaz, J. M., & Gallaire, F. (2011). Extracting energy from a flow: An asymptotic approach using vortex-induced vibrations and feedback control. *Journal of Fluids and Structures*, 27, 861-874. <http://dx.doi.org/10.1016/j.jfluidstructs.2011.03.005>
- Miao, J. M., & Ho, M. H. (2006). Effect of flexure on aerodynamic propulsive efficiency of flapping flexible airfoil. *Journal of Fluids and Structures*, 22, 401-419. <http://dx.doi.org/10.1016/j.jfluidstructs.2005.11.004>
- Michelin, S., Llewellyn-Smith, S., & Glover, B. (2008). Vortex shedding model of a flapping flag. *Journal of Fluid Mechanics*, 617, 1-10. <http://dx.doi.org/10.1017/S0022112008004321>
- Milne-Thompson, L. (1960). *Theoretical Hydrodynamics*. New York: Macmillan.
- Morse, T. L., & Williamson, C. H. K. (2009). Prediction of vortex-induced vibration response by employing controlled motion. *Journal of Fluid Mechanics*, 634, 5-39. <http://dx.doi.org/10.1017/S0022112009990516>
- Morse, T. L., Govardhan, R. N., & Williamson, C. H. K. (2008). The effect of end conditions on the vortex-induced vibration of cylinders. *Journal of Fluids and Structures*, 24, 1227-1239. <http://dx.doi.org/10.1016/j.jfluidstructs.2008.06.004>

- Muller, U. K., van den Boogaart, J. G. M., & van Leeuwen, J. L. (2008). Flow patterns of larval fish: undulatory swimming in the intermediate flow regime. *Journal of Experimental Biology*, *211*, 196-205. <http://dx.doi.org/10.1016/j.jfluidstructs.2008.06.004>
- Muller, U. K., Smit, J., Stamhuis, E. J., & Videler, J. J. (2001). How the body contributes to the wake in undulatory fish swimming: flow fields of a swimming eel (*Anguilla anguilla*). *Journal of Experimental Biology*, *204*, 2751-2762. <http://dx.doi.org/10.1242/jeb.005629>
- Nelles, O. (2002). *Nonlinear System Identification: from classical approaches to neural networks and fuzzy*. Berlin: Springer.
- Ogink, R. H. M., & Metrikine, A. V. (2010). A wake oscillator with frequency dependent coupling for the modeling of VIV. *Journal of Sound and Vibration*, *329*, 26, 5452-5473. <http://dx.doi.org/10.1016/j.jsv.2010.07.008>
- Paidoussis, M. P. (2004). *Fluid-Structure Interactions. Slender Structures and Axial Flow* (1st ed.). Vol. 2, Elsevier Academic Press, London.
- Perez, T., & Fossen, T. I. (2009). A Matlab Toolbox for Parametric Identification of Radiation-Force Models of Ships and Offshore Structures Modeling. *Identification and Control*, *30*, 1-15. <http://dx.doi.org/10.4173/mic.2009.1.1>
- Peskin, C. (2002). The immersed boundary method. *Acta Numerica*, *34*, 479-517.
- Raghavan, K., & Bernitsas, M. M. (2011). Experimental investigation of Reynolds number effect on vortex induced vibration of rigid circular cylinder on elastic supports. *Ocean Engineering*, *38*, 719-731. <http://dx.doi.org/10.1016/j.oceaneng.2010.09.003>
- Ringuette, M. J., Milano, M., & Gharib, M. (2007). Role of the tip vortex in the force generation of low aspect-ratio normal flat plates. *Journal of Fluid Mechanics*, *581*, 453-468. <http://dx.doi.org/10.1017/S0022112007005976>
- Sarpkaya, T. (2004). A critical review of the intrinsic nature of vortex-induced vibrations. *Journal of Fluids and Structures*, *19*, 389-447. <http://dx.doi.org/10.1016/j.jfluidstructs.2004.02.005>
- Sarpkaya, T. (1995). Hydrodynamic damping, flow-induced oscillation, and biharmonic response. *ASME Journal of Offshore Mechanics and Arctic Engineering*, *117*, 232-238. <http://dx.doi.org/10.1115/1.2827228>
- Semler, C., Li, G. X., & Paidoussis, M. P. (1992). The non-linear equations of motion of pipes conveying fluid. *Journal of Sound and Vibration*, *165*, 577-599. <http://dx.doi.org/10.1006/jsvi.1994.1035>
- Schnipper, T., Andersen, A., & Bohr, T. (2009). Vortex wakes of a flapping foil. *Journal of Fluid Mechanics*, *633*, 411-423. <http://dx.doi.org/10.1017/S0022112009007964>
- Seher-Weiss, S. (2011). Identification of nonlinear aerodynamic derivatives using classical and extended local model networks. *Aerospace Science and Technology*, *15*, 33-44. <http://dx.doi.org/10.1016/j.ast.2010.06.002>
- Sfakiotakis, M., Lane, D. M., & Davies, J. B. C. (1999). Review of fish swimming modes for aquatic locomotion. *IEEE Journal Oceanic Engineering*, *24*, 237-252. <http://dx.doi.org/10.1109/48.757275>
- Shayo, L. K. (1980). The stability of cantilever panels in uniform incompressible flow. *Journal of Sound and Vibration*, *68*, 341-350. [http://dx.doi.org/10.1016/0022-460X\(80\)90391-0](http://dx.doi.org/10.1016/0022-460X(80)90391-0)
- Shelley, M., & Zhang, J. (2010). Flapping and Bending Bodies Interacting with Fluid Flows. *Annual Review of Fluid Mechanics*, *43*, 449-465. <http://dx.doi.org/10.1146/annurev-fluid-121108-145456>
- Shelley, M., Vandenberghe, N., & Zhang, J. (2005). Heavy flags undergo spontaneous oscillations in flowing water. *Physical Review Letters*, *94*, 094302. <http://dx.doi.org/10.1103/PhysRevLett.94.094302>
- Shen, Y. Q., Zha, G., & Chen, X. Y. (2009). High order conservative differencing for viscous terms and the application to vortex-induced vibration flows. *Journal of Computational Physics*, *228*, 8283-8300. <http://dx.doi.org/10.1016/j.jcp.2009.08.004>
- Srini, N. (2010). Multi-mode interactions in vortex-induced vibrations of flexible curved/straight structures with geometric nonlinearities. *Journal of Fluids and Structures*, *26*, 1098-1122. <http://dx.doi.org/10.1016/j.jfluidstructs.2010.08.005>
- Succi, S. (2001). *The Lattice Boltzmann Equation for Fluid Dynamics and Beyond*. Oxford University Press, Oxford.

- Taneda, S. (1968). Waving motions of flags. *Journal of the Physical Society of Japan*, 24, 392-401. <http://dx.doi.org/10.1143/JPSJ.24.392>
- Tang, L., Paidoussis, M. P., & Jiang, J. (2009). Cantilevered flexible plates in axial flow: Energy transfer and the concept of flutter-mill. *Journal of Sound and Vibration*, 326, 263-276. <http://dx.doi.org/10.1016/j.jsv.2009.04.041>
- Tang, L., & Paidoussis, M. P. (2007). On the instability and the post-critical behavior of two-dimensional cantilevered flexible plates in axial flow. *Journal of Sound and Vibration*, 305, 97-115. <http://dx.doi.org/10.1016/j.jsv.2007.03.042>
- Tang, D. M., Yamamoto, H., & Dowell, E. H. (2003). Flutter and limit cycle oscillations of two-dimensional panels in three-dimensional axial flow. *Journal of Fluids and Structures*, 17, 225-242. [http://dx.doi.org/10.1016/S0889-9746\(02\)00121-4](http://dx.doi.org/10.1016/S0889-9746(02)00121-4)
- Triantafyllou, M. S., Triantafyllou, G. S., & Yue, D. K. P. (2000). Hydrodynamics of fishlike swimming. *Annual Review of Fluid Mechanics*, 32, 33-53. <http://dx.doi.org/10.1146/annurev.fluid.32.1.33>
- Violette, R., de Langre, E., & Szydlowski, J. (2010). A linear stability approach to vortex-induced vibrations and waves. *Journal of Fluids and Structures*, 26, 442-466. <http://dx.doi.org/10.1016/j.jfluidstructs.2010.01.002>
- Vogel, S. (1994). *Life in Moving Fluids*. Princeton. (2nd ed.). NJ: Princeton Univ. Press.
- von Karman, T., & Burgers, J. M. (1963). *General aerodynamic theory - perfect fluids (1935)*. In *Aerodynamic Theory II*, 280-310 (ed. by W. F. Durand). Dover Publications, 1963.
- Wanga, X. Q., Soa, R. M. C., & Xie, W. C. (2007). Features of flow-induced forces deduced from wavelet analysis. *Journal of Fluids and Structures*, 23, 249-268. <http://dx.doi.org/10.1016/j.jfluidstructs.2006.09.002>
- Watanabe, Y., Suzuki, S., Sugihara, M., & Sueoka, Y. (2002). An experimental study of paper flutter. *Journal of Fluids and Structures*, 16, 529-542. <http://dx.doi.org/10.1006/jfls.2001.0435>
- Watanabe, Y., Isogai, K., Suzuki, S., & Sugihara, M. (2002). A theoretical study of paper flutter. *Journal of Fluids and Structures*, 16, 543-560. <http://dx.doi.org/10.1006/jfls.2001.0436>
- Williamson, C. H. K., & Govardhan, R. (2008). A brief review of recent results in vortex-induced vibrations. *Journal of Wind Engineering and Industrial Aerodynamics*, 96, 713-735. <http://dx.doi.org/10.1016/j.jweia.2007.06.019>
- Williamson, C. H. K., & Govardhan, R. (2004). Vortex-induced vibrations. *Annual Review of Fluid Mechanics*, 36, 413-455. <http://dx.doi.org/10.1146/annurev.fluid.36.050802.122128>
- Williamson, C. H. K. (1996). Vortex dynamics in the cylinder wake. *Annual Review of Fluid Mechanics*, 28, 477-539. <http://dx.doi.org/10.1146/annurev.fl.28.010196.002401>
- Williamson, C. H. K., & Roshko, A. (1988). Vortex formation in the wake of an oscillating cylinder. *Journal of Fluids and Structure*, 2, 355-381. [http://dx.doi.org/10.1016/S0889-9746\(88\)90058-8](http://dx.doi.org/10.1016/S0889-9746(88)90058-8)
- Worden, K., & Tomlinson, G. R. (2001). *Nonlinearity in structural dynamics: detection, identification, and modeling*. IOP Publishing. <http://dx.doi.org/10.1887/0750303565>
- Wun, J. H., & Chang, F. J. (2011). Aerodynamic parameters of across-wind self-limiting vibration for square sections after lock-in in smooth flow. *Journal of Sound and Vibration*, 330, 4328-4339. <http://dx.doi.org/10.1016/j.jsv.2011.04.026>
- Xu, W. H., Wu, Y. X., Zeng, X. H., Zhong, X. F., & Yu, J. X. (2010). A new wake oscillator model for predicting VIV of a circular cylinder. *Journal of Hydrodynamics, Series B*, 22, 381-386. [http://dx.doi.org/10.1016/S1001-6058\(09\)60068-8](http://dx.doi.org/10.1016/S1001-6058(09)60068-8)
- Yadykin, Y., Tenetov, V., & Levin, D. (2001). The flow-induced vibration of a flexible strip hanging vertically in a parallel flow, part I: temporal aeroelastic instability. *Journal of Fluids and Structures*, 15, 1167-1185. <http://dx.doi.org/10.1006/jfls.2001.0400>
- Yamaguchi, N., Yokota, K., & Tsujimoto, Y. (2000). Flutter limits and behaviors of a flexible thin sheet in high speed flow-I: analytical method for prediction of the sheet behavior. *ASME Journal of Fluids Engineering*, 122, 65-73. <http://dx.doi.org/10.1115/1.483242>

- Yamaguchi, N., Sekiguchi, T., Yokota, K., & Tsujimoto, Y. (2000). Flutter limits and behaviors of a flexible thinsheet in high-speed flow-II: experimental results and predicted behaviors for low mass ratios. *ASME Journal of Fluids Engineering*, *122*, 74-83. <http://dx.doi.org/10.1115/1.483228>
- Yasuda, K., & Kamiya, K. (1999). Experimental identification technique of nonlinear beams in time domain. *Nonlinear Dynamics*, *18*, 185-202. <http://dx.doi.org/10.1023/A:1008383603257>
- Yin, B., & Luo, H. (2010). Effect of wing inertia on hovering performance of flexible flapping wings. *Physics of Fluids*, *76*, 111902. <http://dx.doi.org/10.1063/1.3499739>
- Zhang, H. J., Zhou, Y., So, R. M. C. Mignolet, M. P., & Wang, Z. J. (2003). A note on the fluid damping of anelastic cylinder in a cross-flow. *Journal of Fluids and Structures*, *17*, 479-483. [http://dx.doi.org/10.1016/S0889-9746\(02\)00137-8](http://dx.doi.org/10.1016/S0889-9746(02)00137-8)
- Zhao, M., & Cheng, L. (2011). Numerical simulation of two-degree-of-freedom vortex-induced vibration of acircular cylinder close to a plane boundary. *Journal of Fluids and Structures*, *27*, 1097-1110. <http://dx.doi.org/10.1016/j.jfluidstructs.2011.07.001>
- Zhu, L. D., & Peskin, C. (2002). Simulation of a flapping flexible filament in a flowing soap film by the immersedboundary method. *Journal of Computational Physics*, *179*, 452-468. <http://dx.doi.org/10.1006/jcph.2002.7066>